

# Learning about modes and scaling of fault slip from *in situ*, fault-scale observations.

J. Gomberg & Evelyn Roeloffs, Kathleen Hodgkinson, David Schmidt, Paul Bodin, Jeff McGuire,  
Brendon Crowell, Sarah Minson, & many others....

## Talk Topics

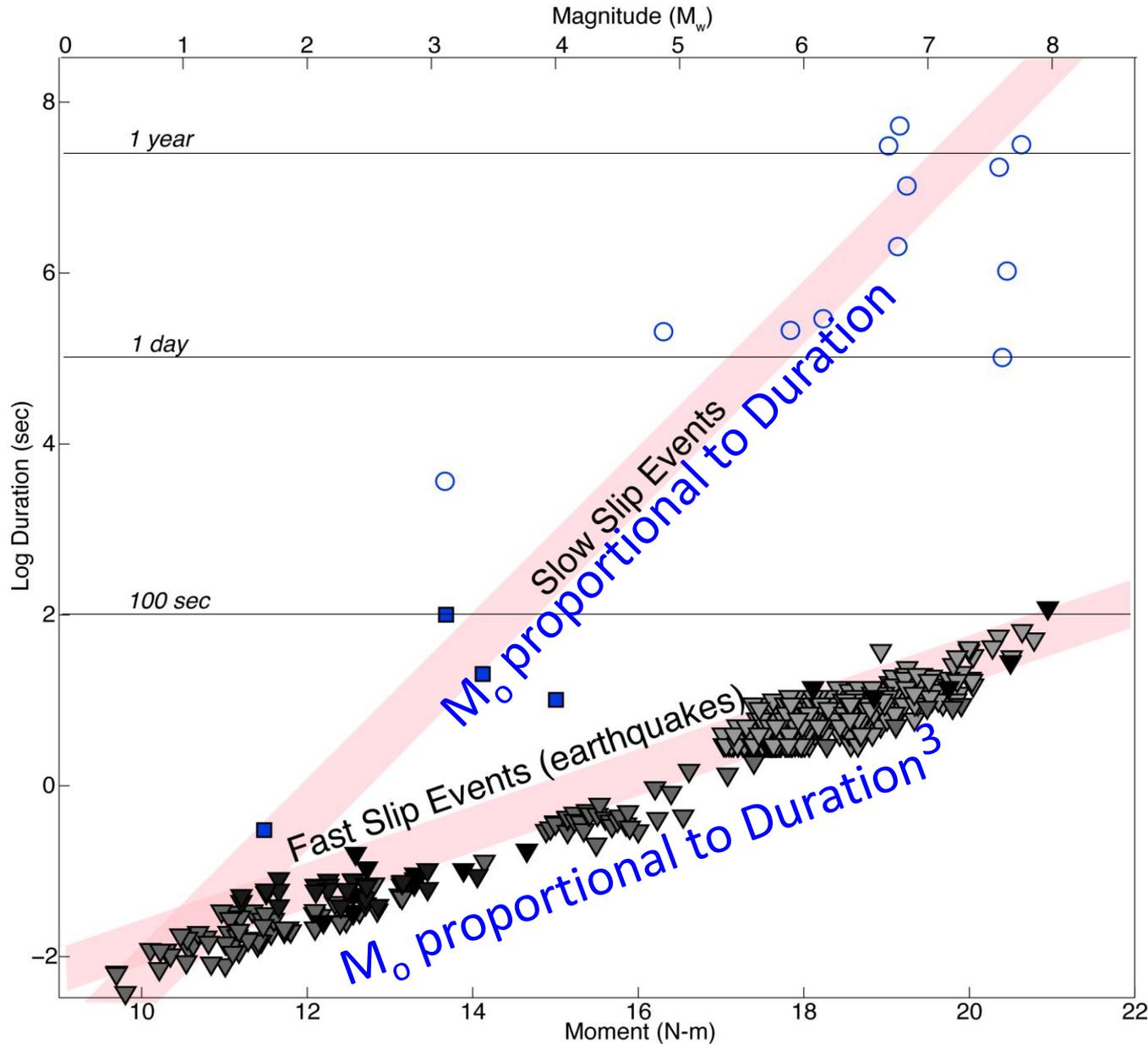
Scaling of slip event duration versus moment – why care?

Assessing what can really observe & its imprint on our understanding.

Gap-filling possibilities (high-rate strainmeter data).

Spectral scaling – assessing not only what we measure, but what it means.

# Moment/duration scaling – key constraint on rupture physics



Ide et al., 2007

# Moment/duration scaling – key constraint on rupture physics

*Moment  $M_0 = \text{rigidity} \times \text{Slip} \times \text{Length}^2$*

*Stress drop  $\Delta\sigma \sim \text{rigidity} \times \text{Slip} / \text{Length}$*

*Length = Rupture Velocity  $V_r \times \text{Duration}$*

$$M_0 = \Delta\sigma \times L^3 = \Delta\sigma \times V_r^3 \times \text{Duration}^3$$

Earthquake data show

$$M_0 = C \times \text{Duration}^3$$

implying

$$C = \Delta\sigma \times V_r^3$$

**$V_r$  &  $\Delta\sigma$  independent of rupture dimension, L**

# Moment/duration scaling – key constraint on rupture physics

*Moment*  $M_0 = \text{rigidity} \times \text{Slip} \times \text{Length}^2$

*Stress drop*  $\Delta\sigma \sim \text{rigidity} \times \text{Slip} / \text{Length}$

*Length* = *Rupture Velocity*  $V_r \times \text{Duration}$

$$M_0 = \Delta\sigma \times L^3 = \Delta\sigma \times V_r^3 \times \text{Duration}^3$$

If  $M_0$  is  $\sim$ proportional to Duration, or

$$M_0 = C \times \text{Duration}$$

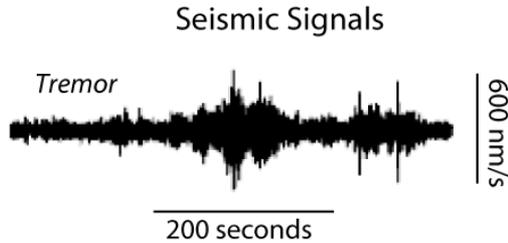
implying

$$C = \Delta\sigma V_r L^2$$

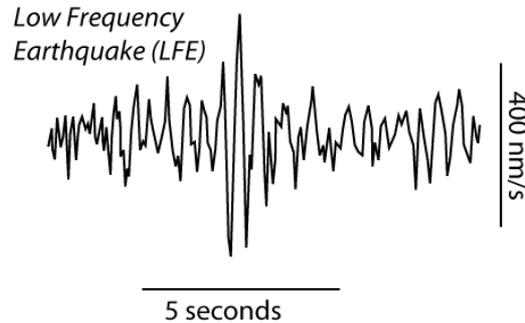
**$V_r$  &  $\Delta\sigma$  decrease as rupture dimension,  $L$ , grows**

# Measurables

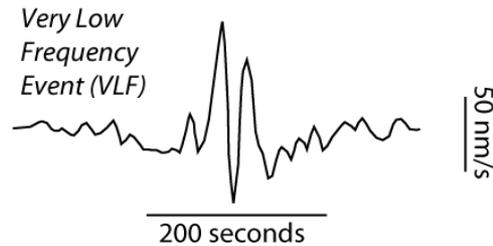
*Sec to hours,  
 $M \leq 1.5$*



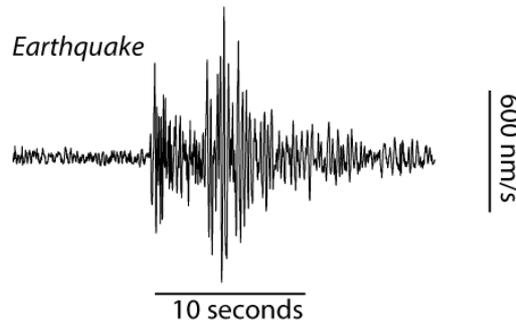
*Few sec,  
 $M \leq 1.5$*



*Tens of sec,  
 $M \leq 4$*



*Few sec to mins,  
 $M \leq 9.5$*

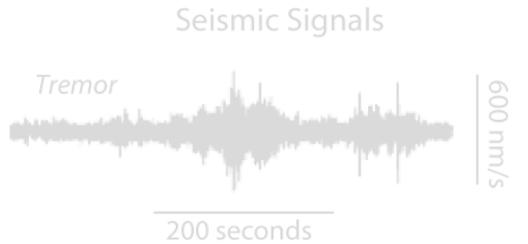


‘Slow’ (low frequency?) seismic signals, with quenched amplitudes regardless of event size.

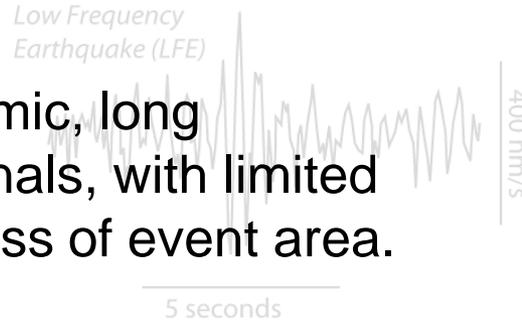
‘Fast’ (higher frequency) seismic signals, with amplitudes that grow with event size; earthquakes!

# Measurables

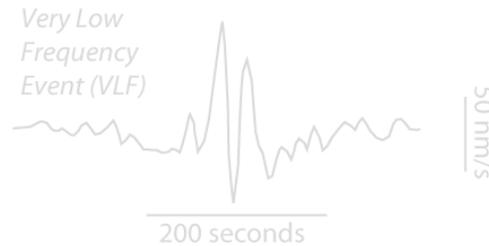
*Sec to hours,  
M<sub>≤1.5</sub>*



*Few* 'Slow' aseismic, long duration signals, with limited slip regardless of event area.  
*M<sub>≤1.5</sub>*



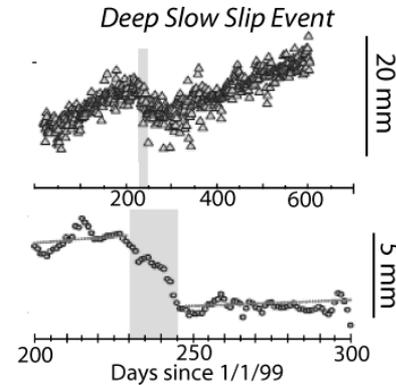
*Tens of sec,  
M<sub>≤4</sub>*



*Few sec to mins,  
M<sub>≤9.5</sub>*

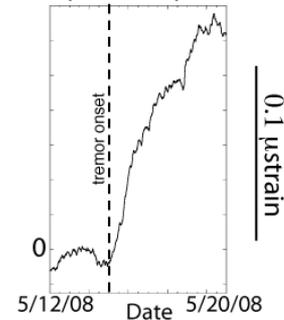


## Geodetic Signals

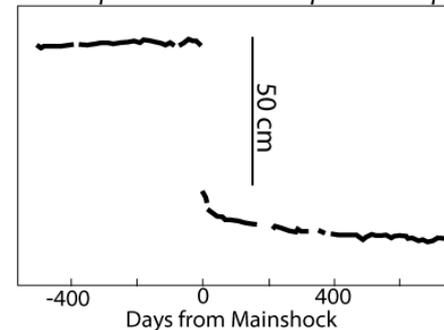


*Hours to days,  
≤ few cm*

## Deep Slow Slip Event



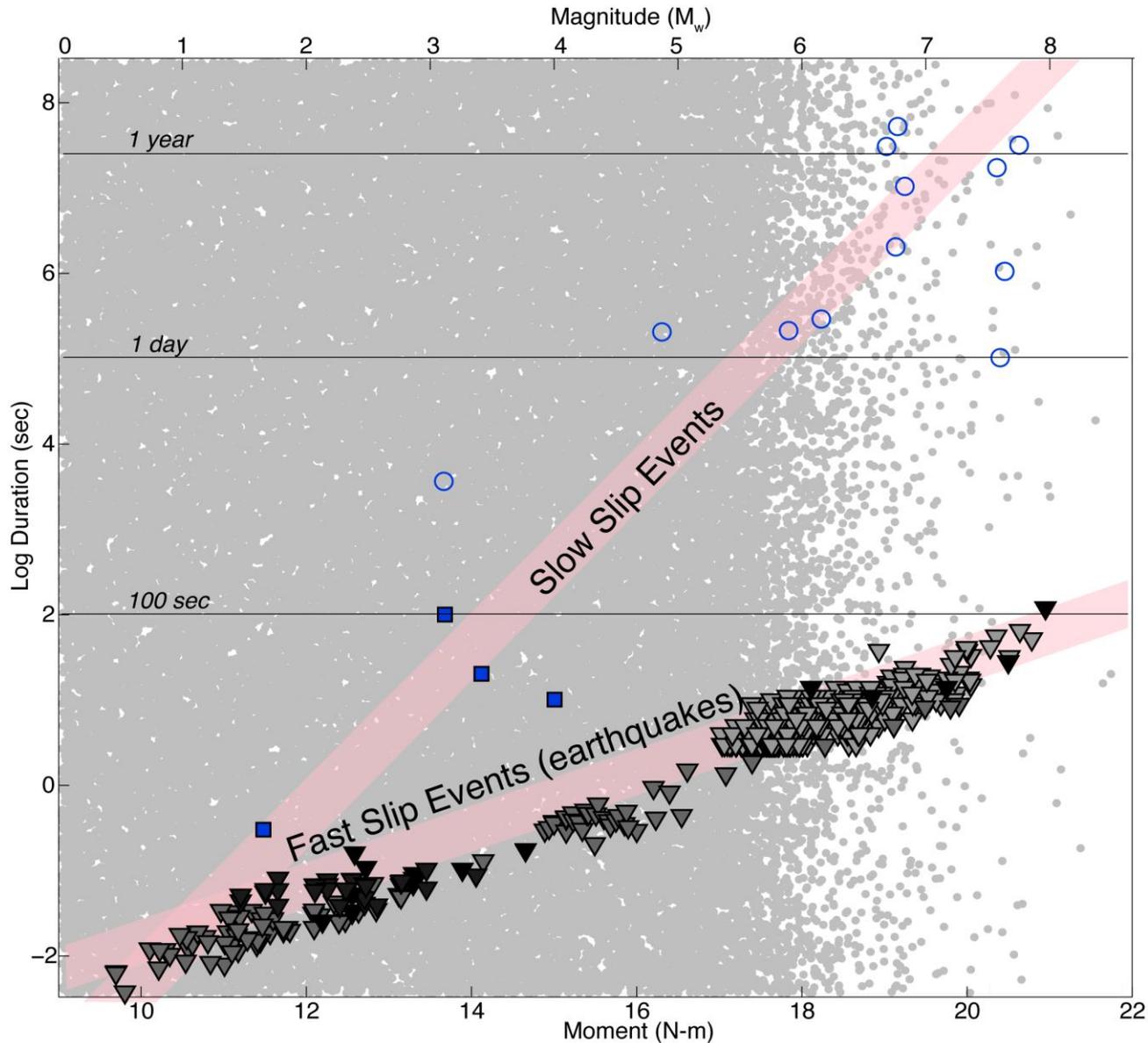
## Earthquake Coseismic Slip & Afterslip



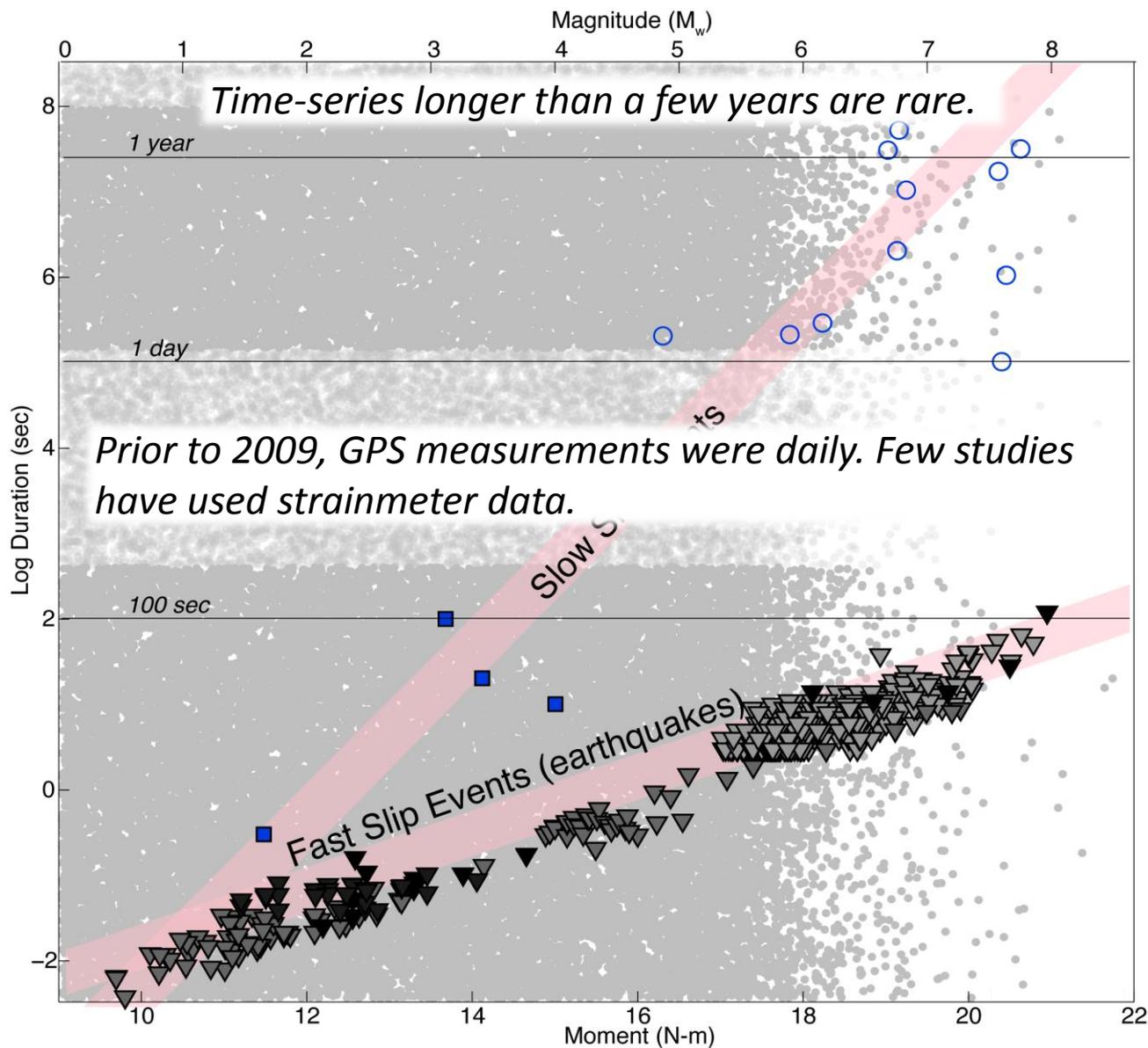
*Few to 100s  
of sec,  
≤ 10s of m*

# Assessing what we can observe: Natural recurrence rates affect apparent scaling

(smaller events are more frequent).



# Sampling rate & longevity of measurements affect apparent scaling.



# Consider measurement detection thresholds

Agnew (UNAVCO Course, 2014)

Displacement,  $u(t)$ , at a distance,  $r$ , from a moment-tensor source,  $M_0(t)$

$$u(t) = u_N + u_F = \frac{G_N(\theta, \phi)}{4\pi\rho c^2} \frac{1}{r^2} M_0(t - r/c) + \frac{G_F(\theta, \phi)}{4\pi\rho c^3} \frac{1}{r} \frac{dM_0(t - r/c)}{dt}$$

near-field term,  $r^{-2}$  decay                      far-field term,  $r^{-1}$  decay

If  $u(t)$  has time constant  $t_s$ ,

$$u(t) \sim \frac{G(\theta, \phi)}{4\pi\rho c^2} \frac{1}{r^2} \left[ M_0 + \frac{r}{c} \frac{dM_0}{dt} \right]$$

distance dependence

$u(t)$  has Fourier amplitude spectrum  $U(f)$  & noise power spectrum  $N(f)$ .

The signal-to-noise ratio is

$$\text{SNR} = \left[ \int \frac{|U(f)|^2}{N(f)} df \right]^{\frac{1}{2}} \sim \frac{u_{RMS}}{B(t_s)}$$

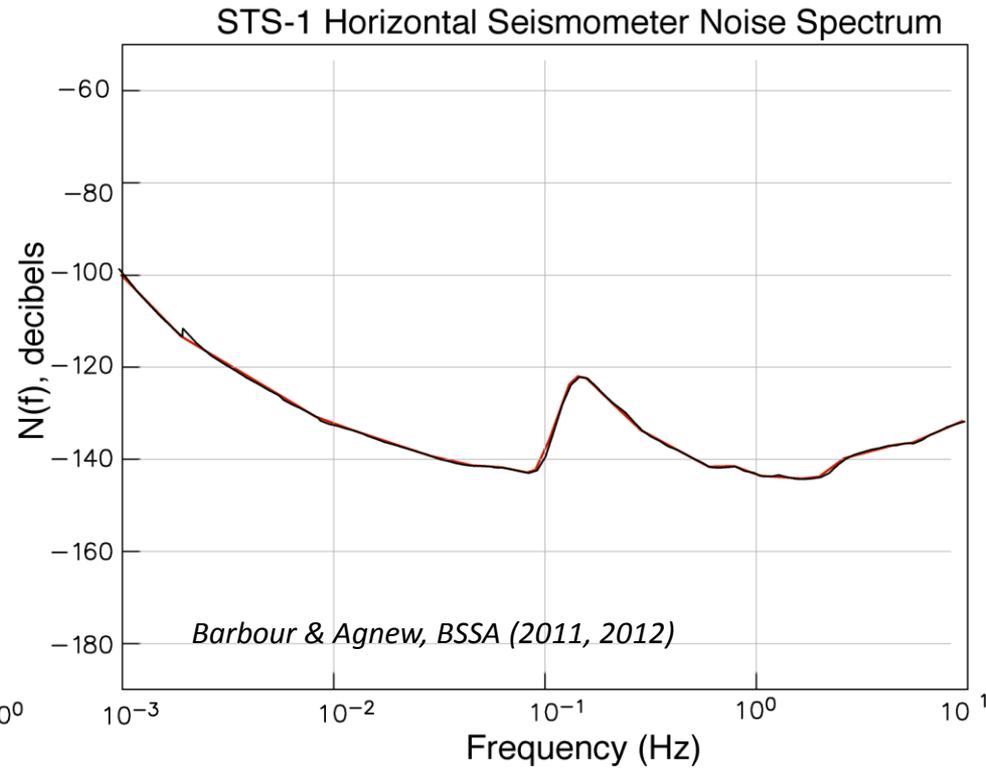
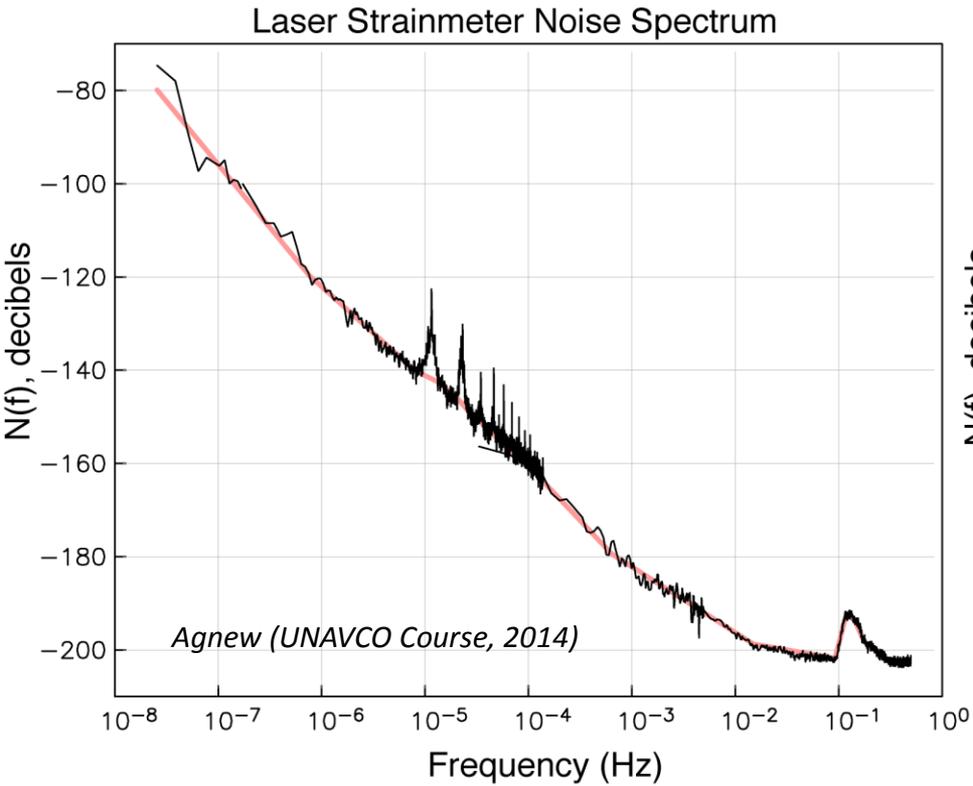
$B(t_s)$  is the RMS noise over a one-octave band,

$$B(t_s) = \left[ \int_{\frac{1}{\sqrt{2}t_s}}^{\frac{\sqrt{2}}{t_s}} N(f) df \right]^{\frac{1}{2}}$$

Detection requires  $\text{SNR} > 1$  or  $u_{RMS} > B(t_s)$ . Detection threshold,  $M_0$ , for a value of  $t_s$  is

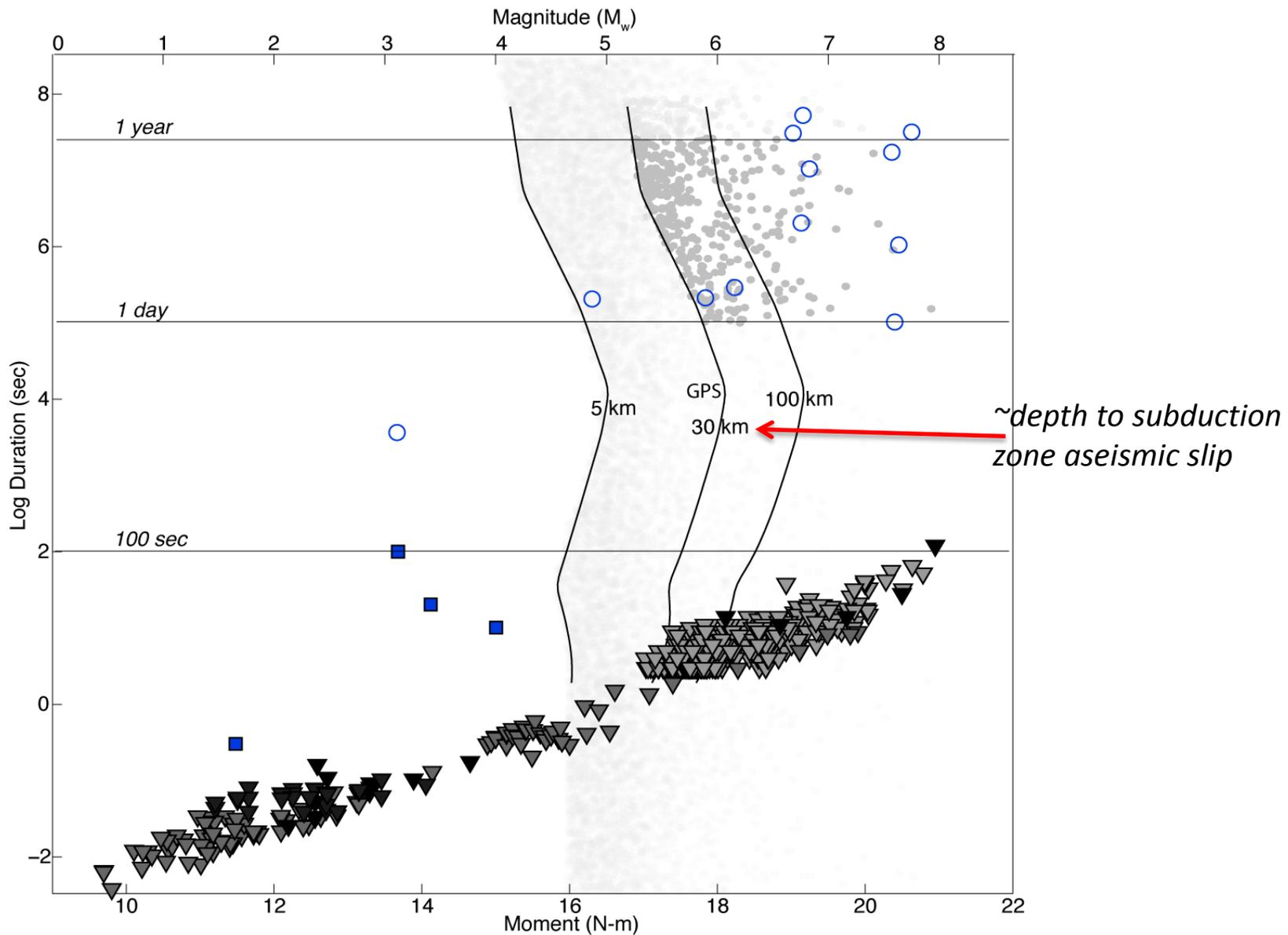
$$B(t_s) \sim \frac{G}{4\pi\rho c^2} \frac{1}{r^2} \left[ 1 + \frac{r}{ct_s} \right] M_0$$

# Measurement detection thresholds.

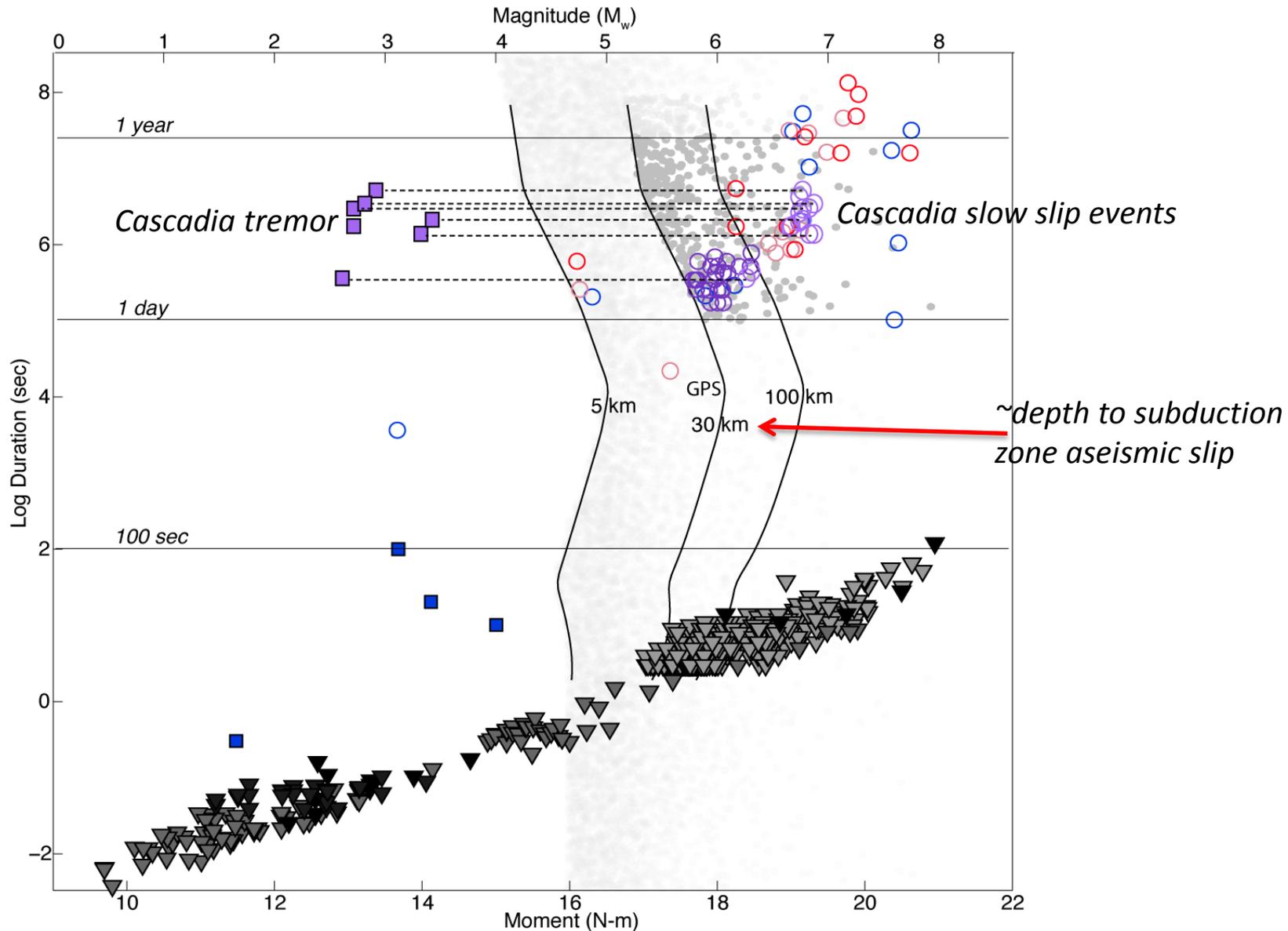


Compute  $B(t_S) = \left[ \frac{\int_1^{\sqrt{2}t_S} N(f) df}{\sqrt{2}t_S} \right]^{\frac{1}{2}}$

# GPS detection thresholds

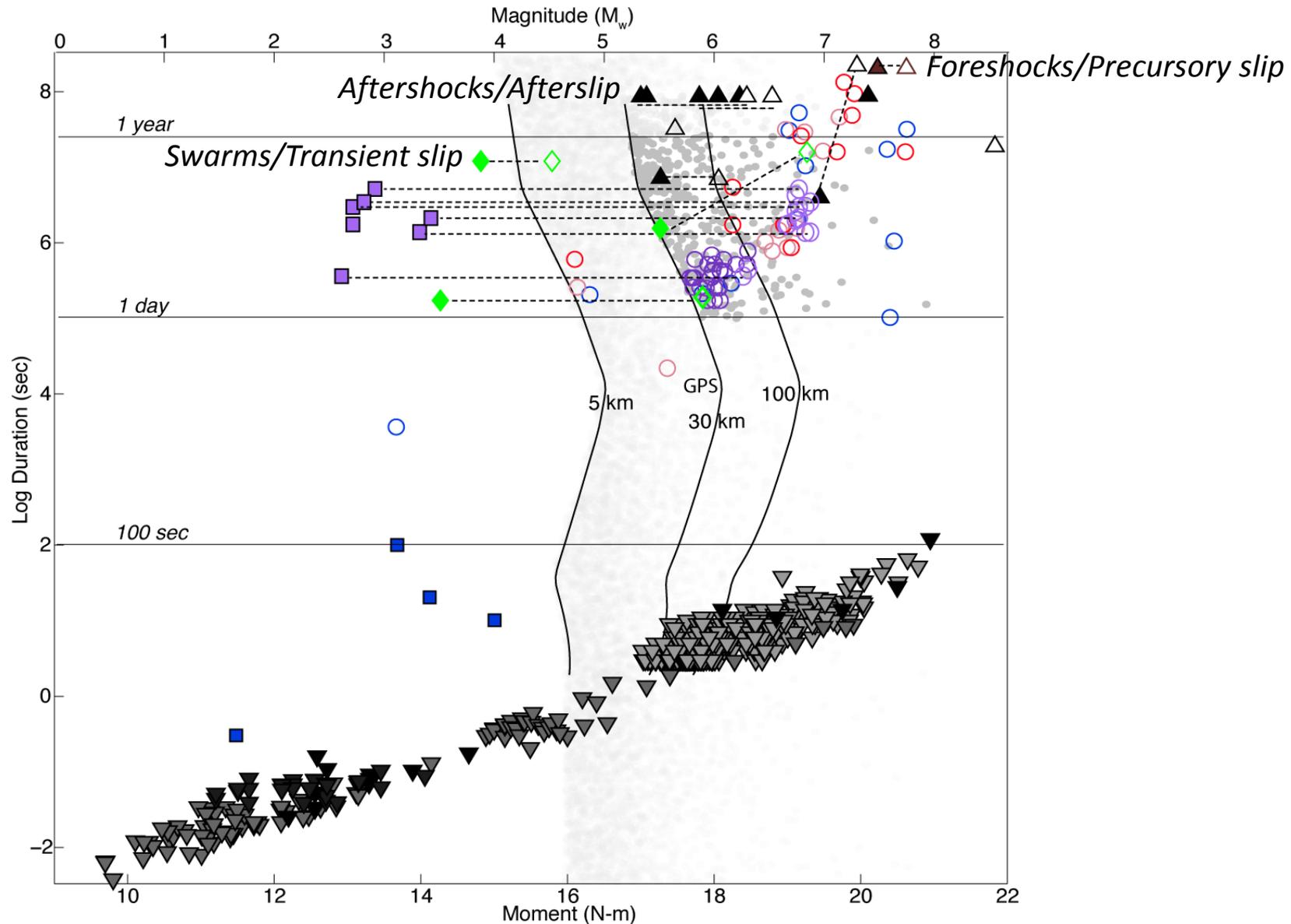


# More GPS measurements of spontaneous slip events. The Earth also imposes sampling limitations.

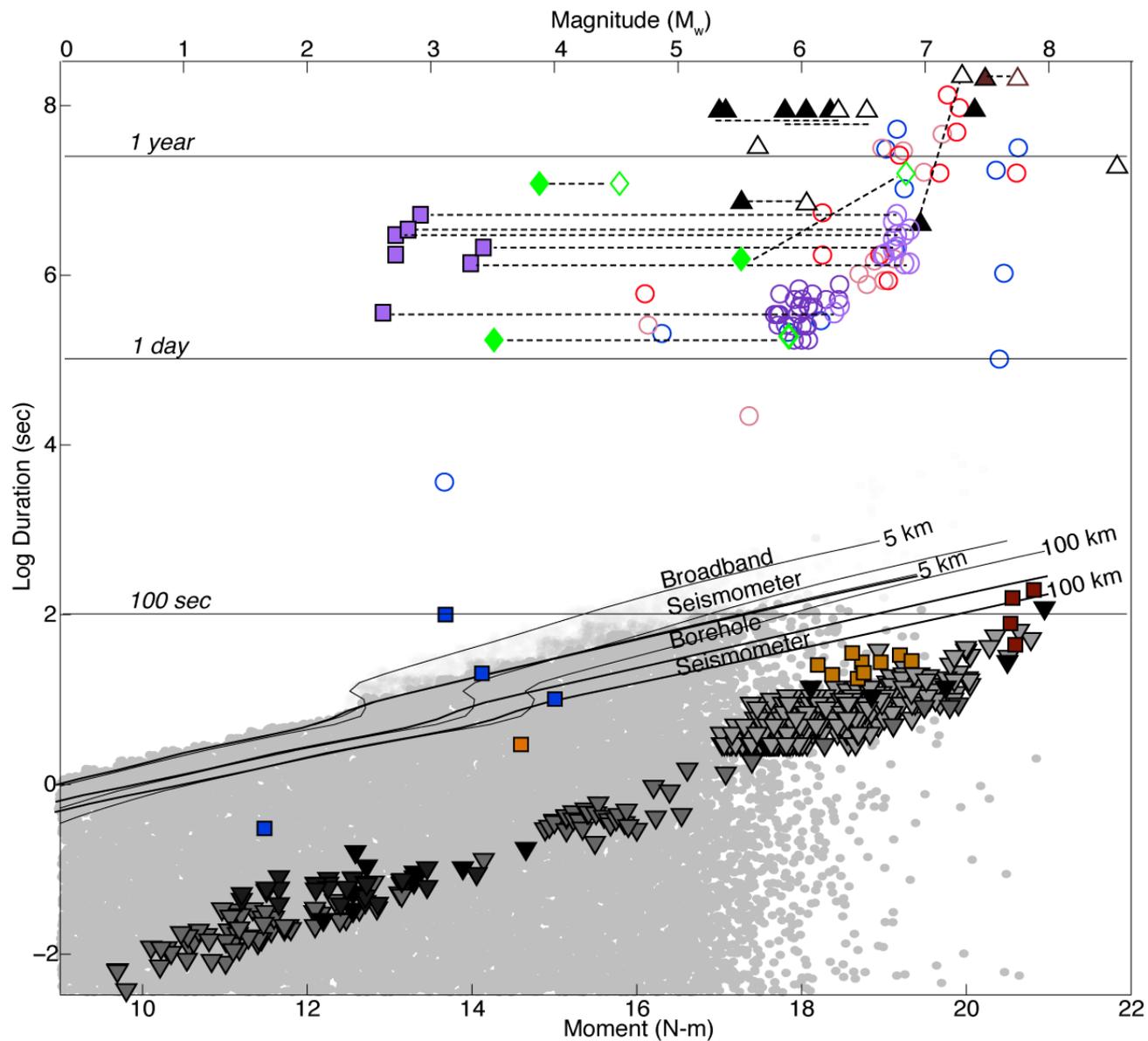


# Coupled seismic & aseismic slip event measurements.

We begin to fill the GPS detectable region. Aseismic moment > seismic moment always!

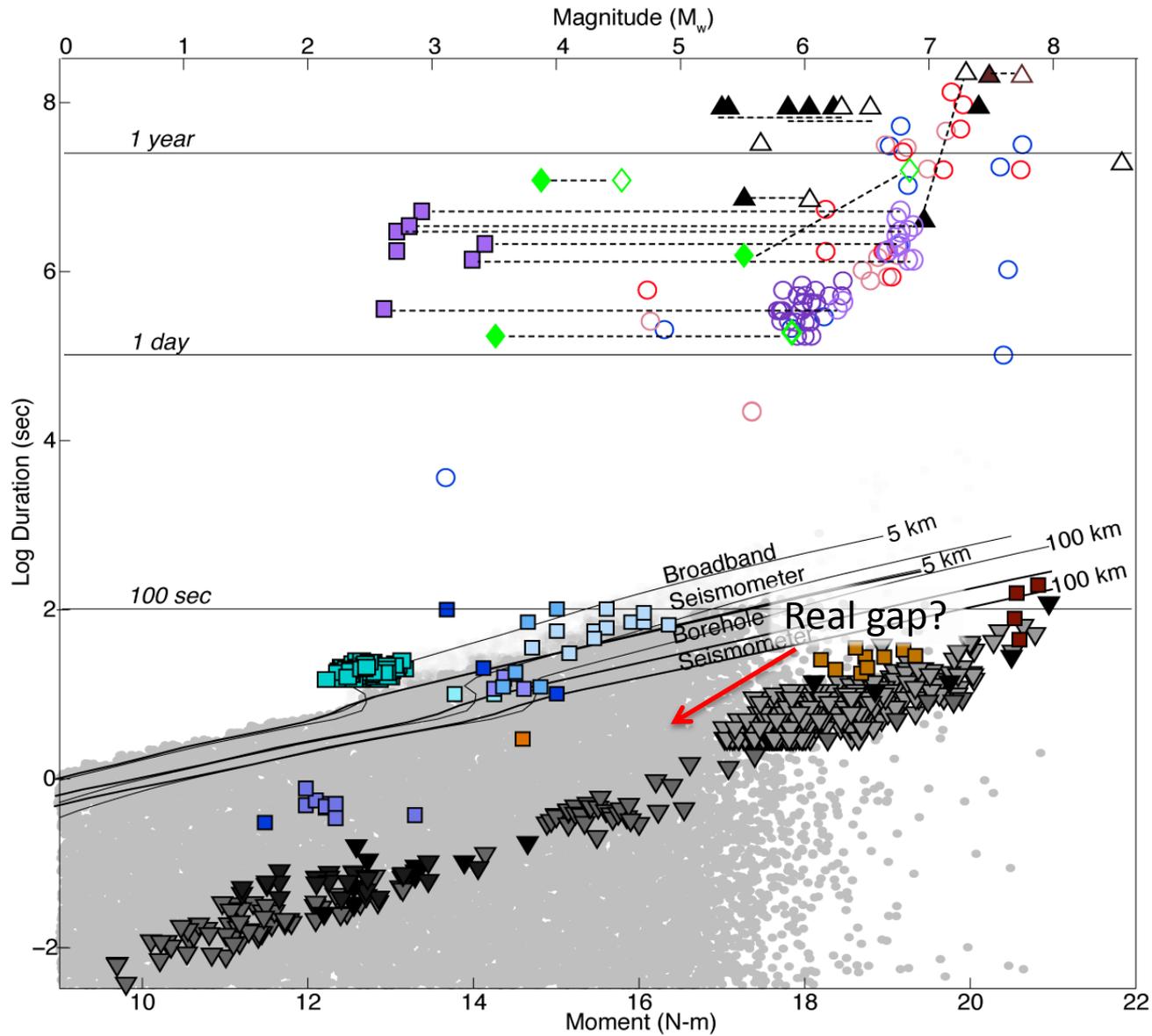


# Seismic detection thresholds.

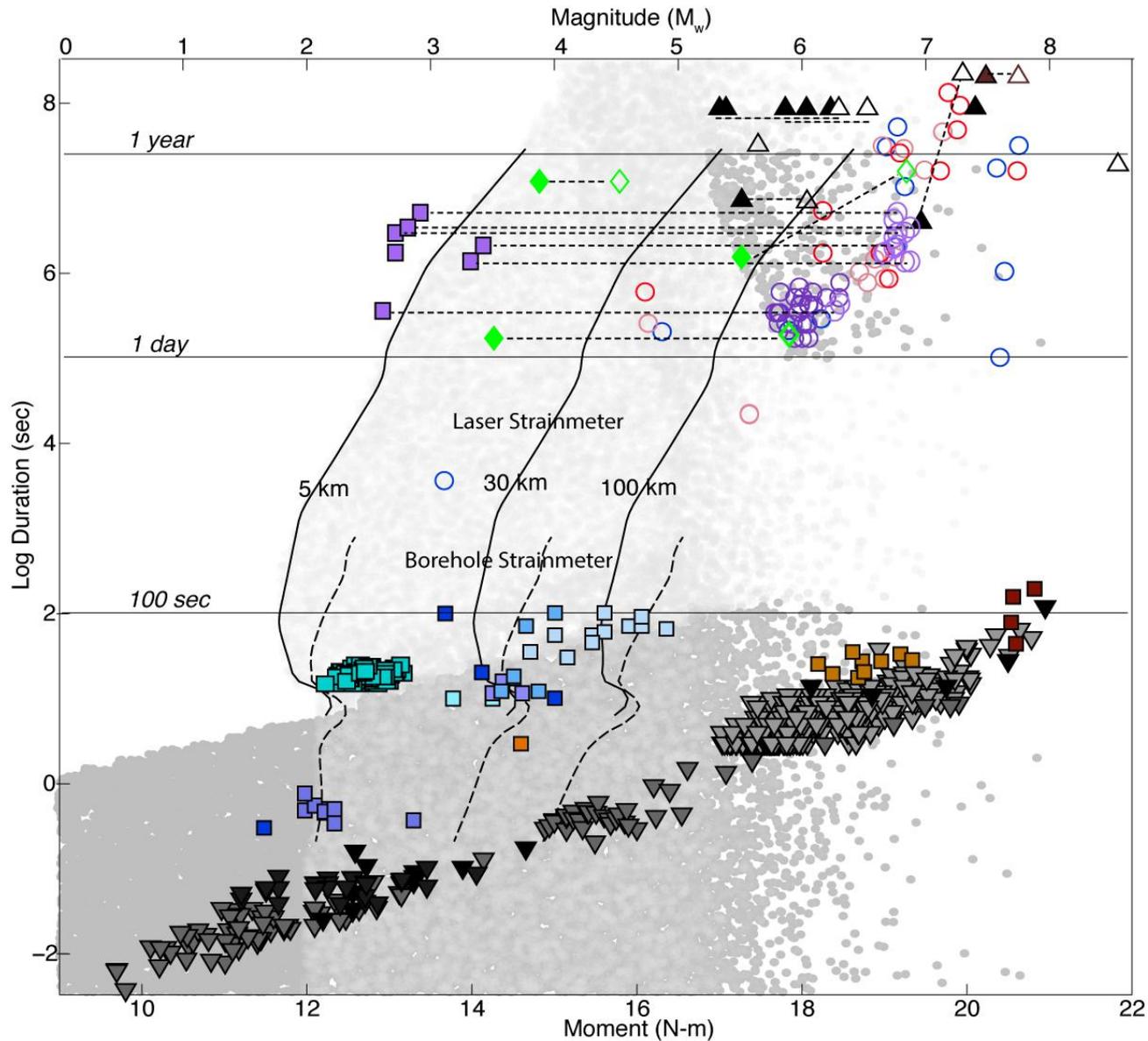


# Seismic detection thresholds.

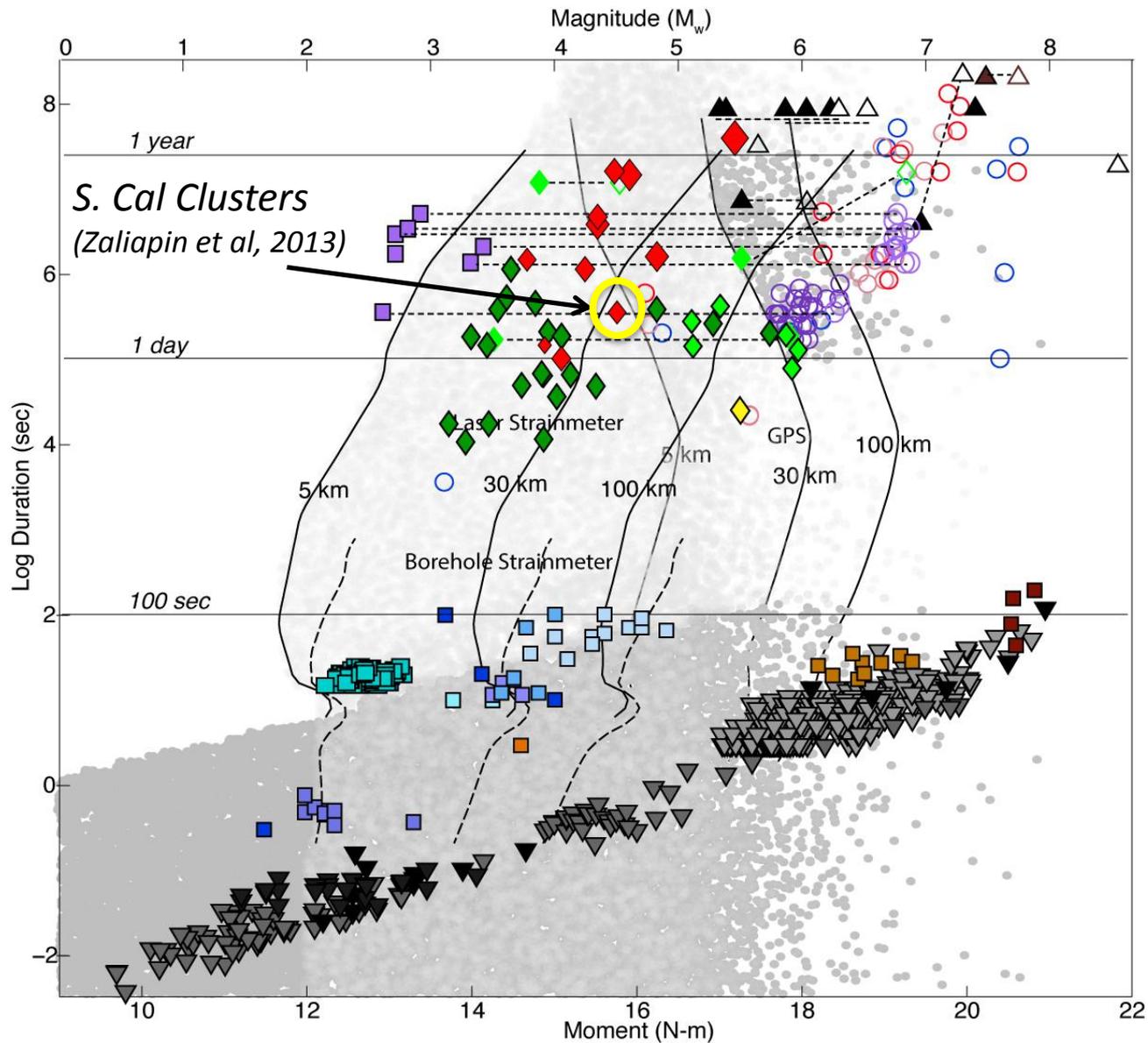
A real gap exists?



# Strainmeter detection thresholds – promising!

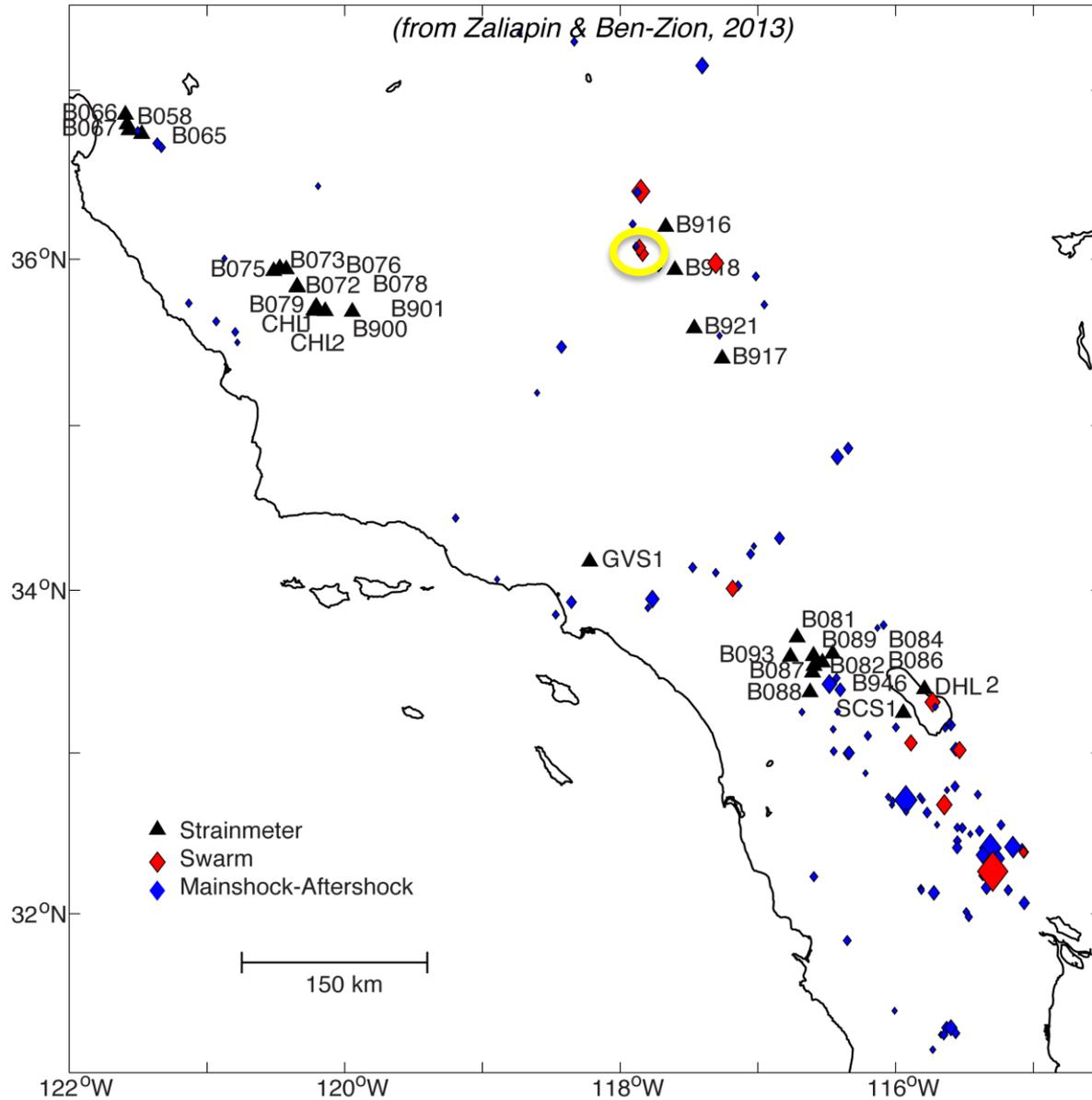


# Shallow swarms (proxies for shallow slow slip) & strainmeters hold most promise to fill in gaps.

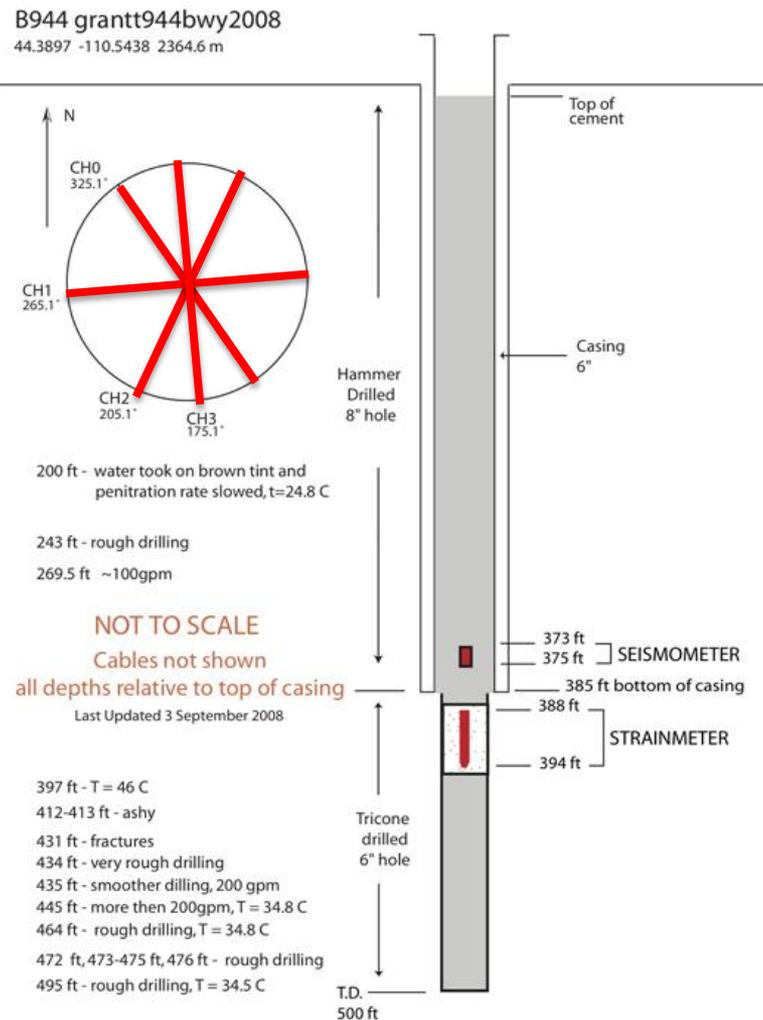


# Clustered strainmeters help discriminate Earthly signals?

## Southern California Earthquake Clusters

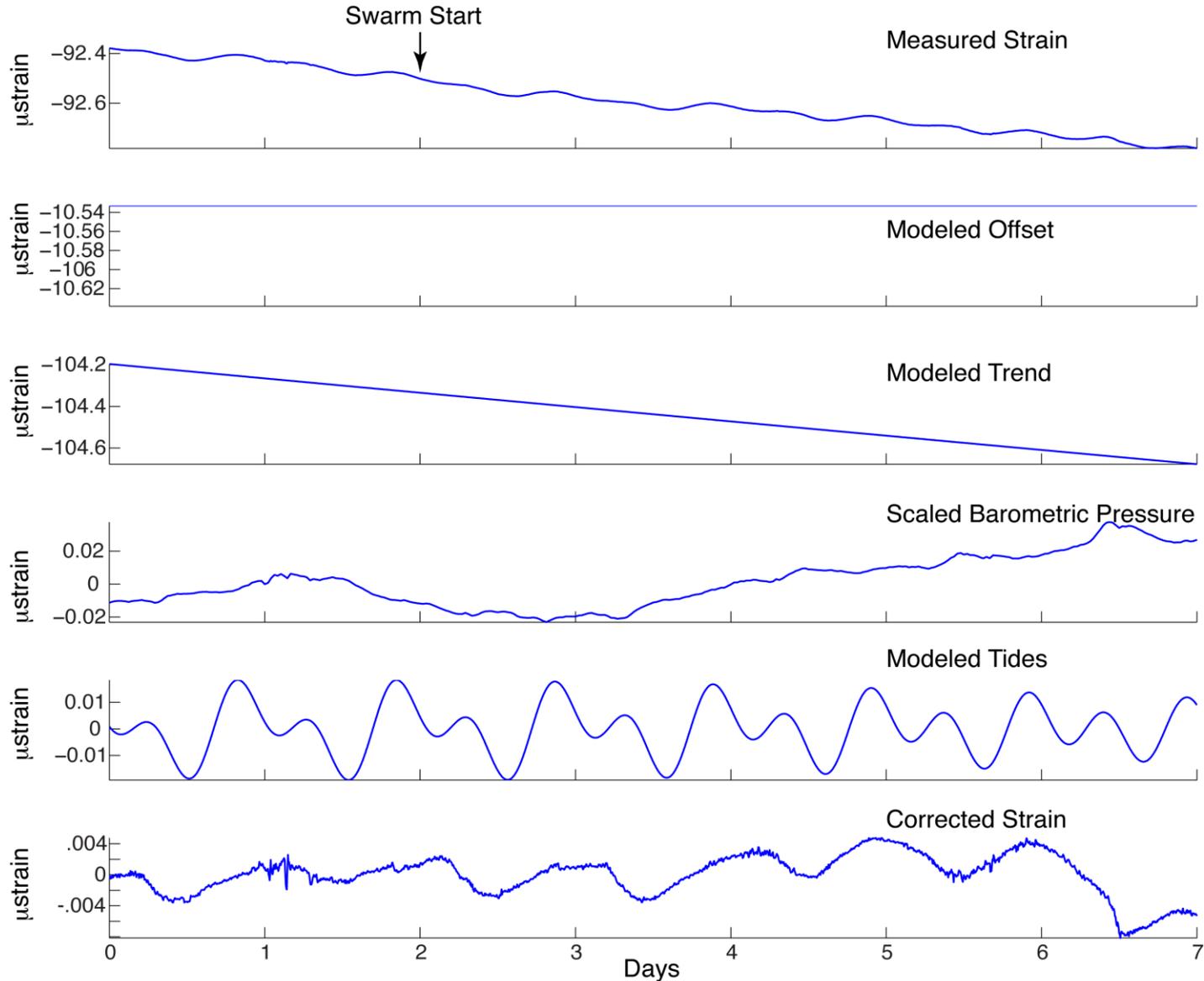


# Know thy data: 1) 4 measurements combined

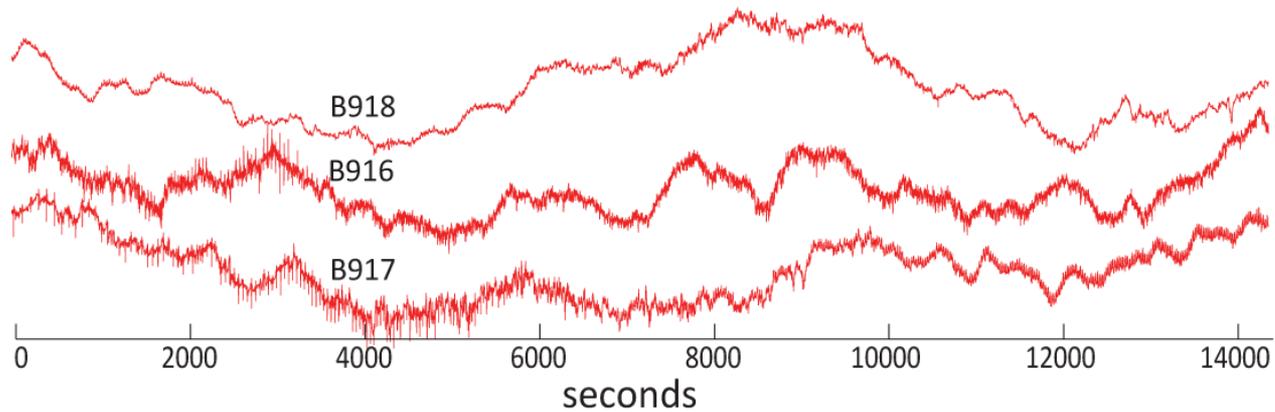
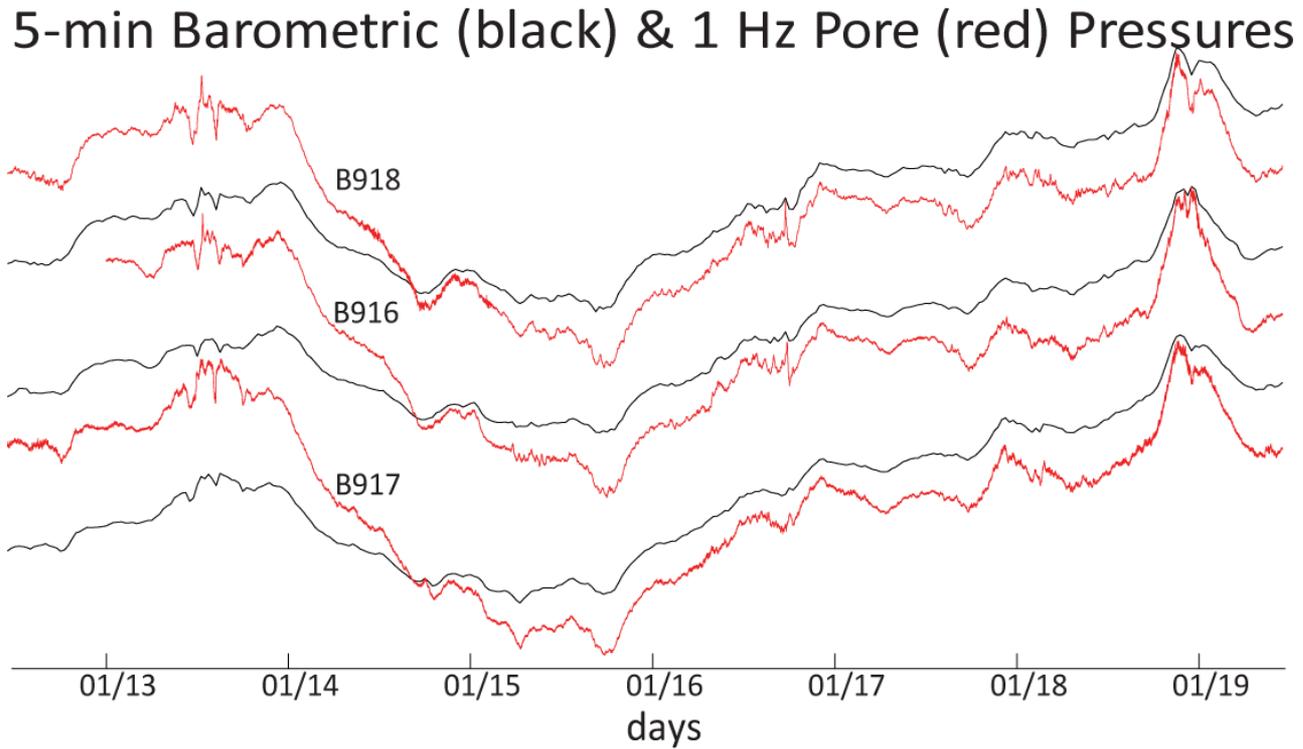


# Know thy data: 2) Low detection threshold = high deterministic noise levels (5 min data)

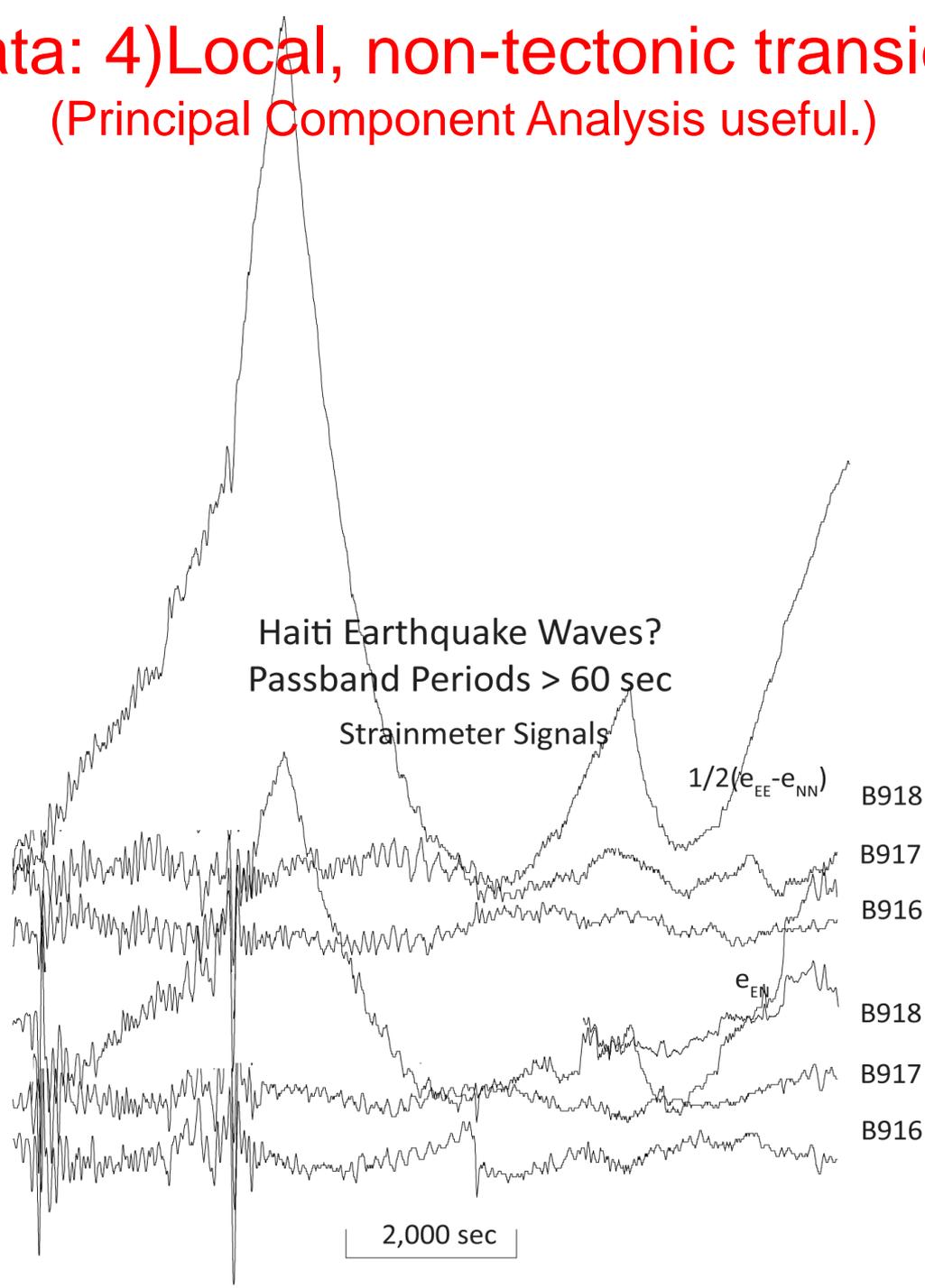
B916 Strainmeter Data (Gage 0) & Corrections



# Know thy data: 3) Coherent noise (pressures).

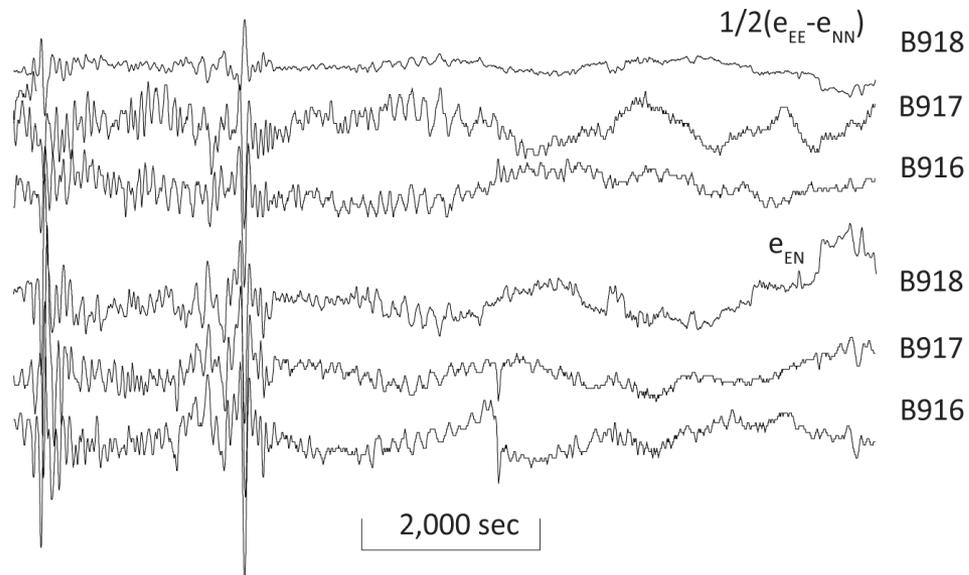


# Know thy data: 4) Local, non-tectonic transient sources. (Principal Component Analysis useful.)



# Know thy data: 1<sup>st</sup> Principal Component Removed

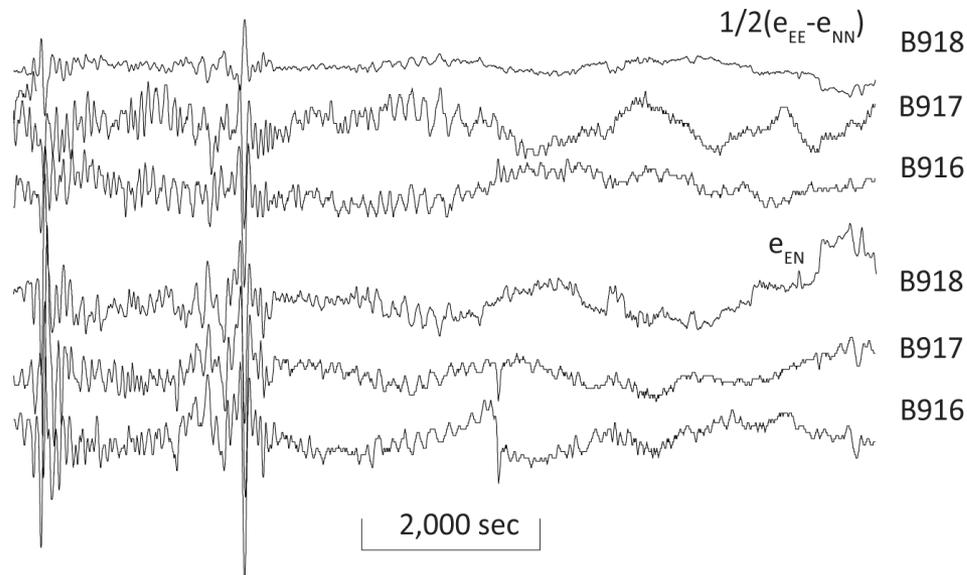
Haiti Earthquake Waves?  
Passband Periods > 60 sec  
Strainmeter Signals



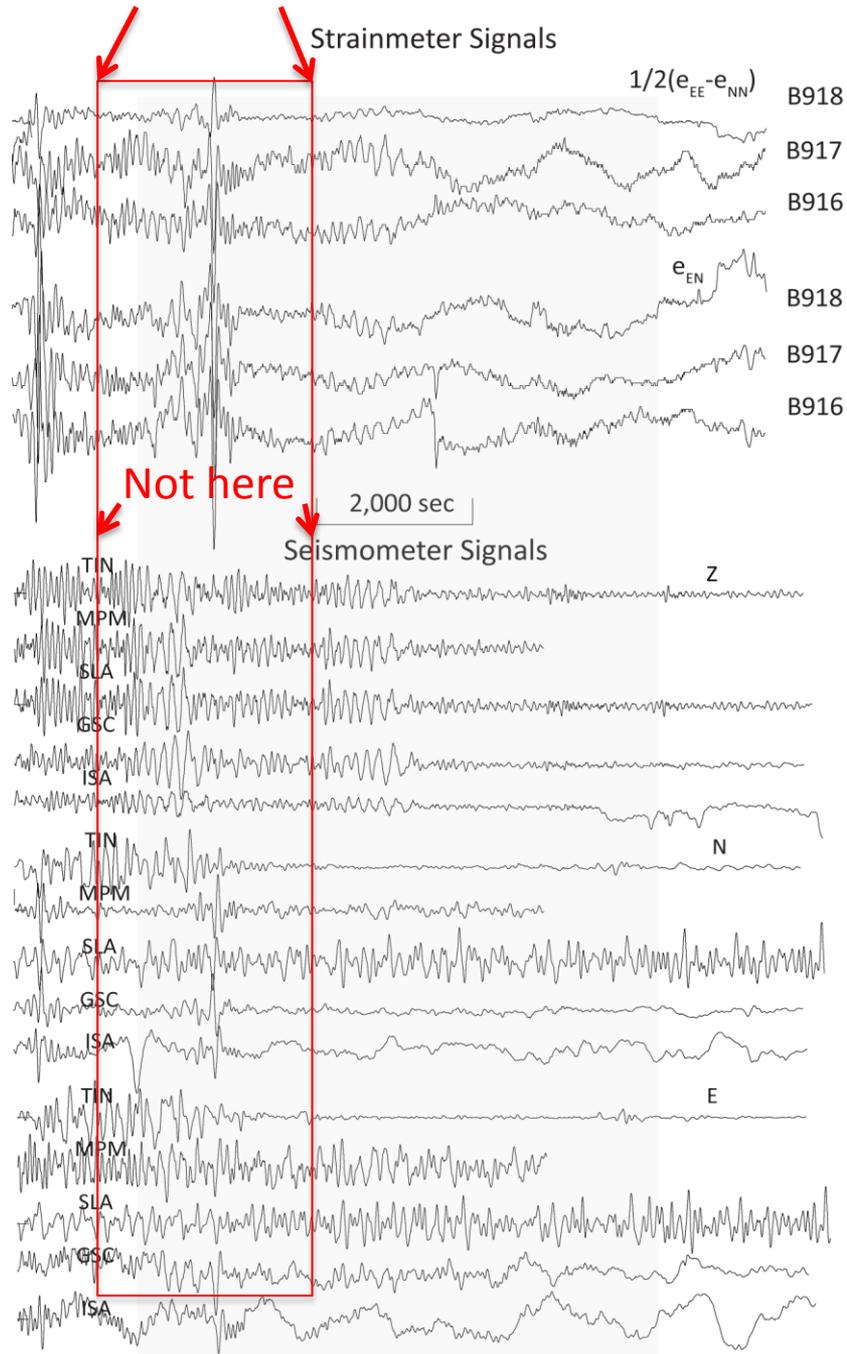
# Only Earthly coherent signals during 2 swarm intervals from distant earthquake waves.

Haiti Earthquake Waves?  
Passband Periods > 60 sec

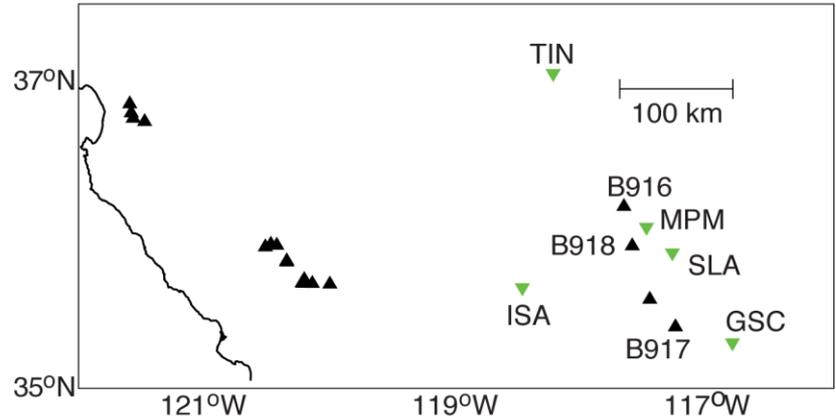
Strainmeter Signals



Coherent long period energy here

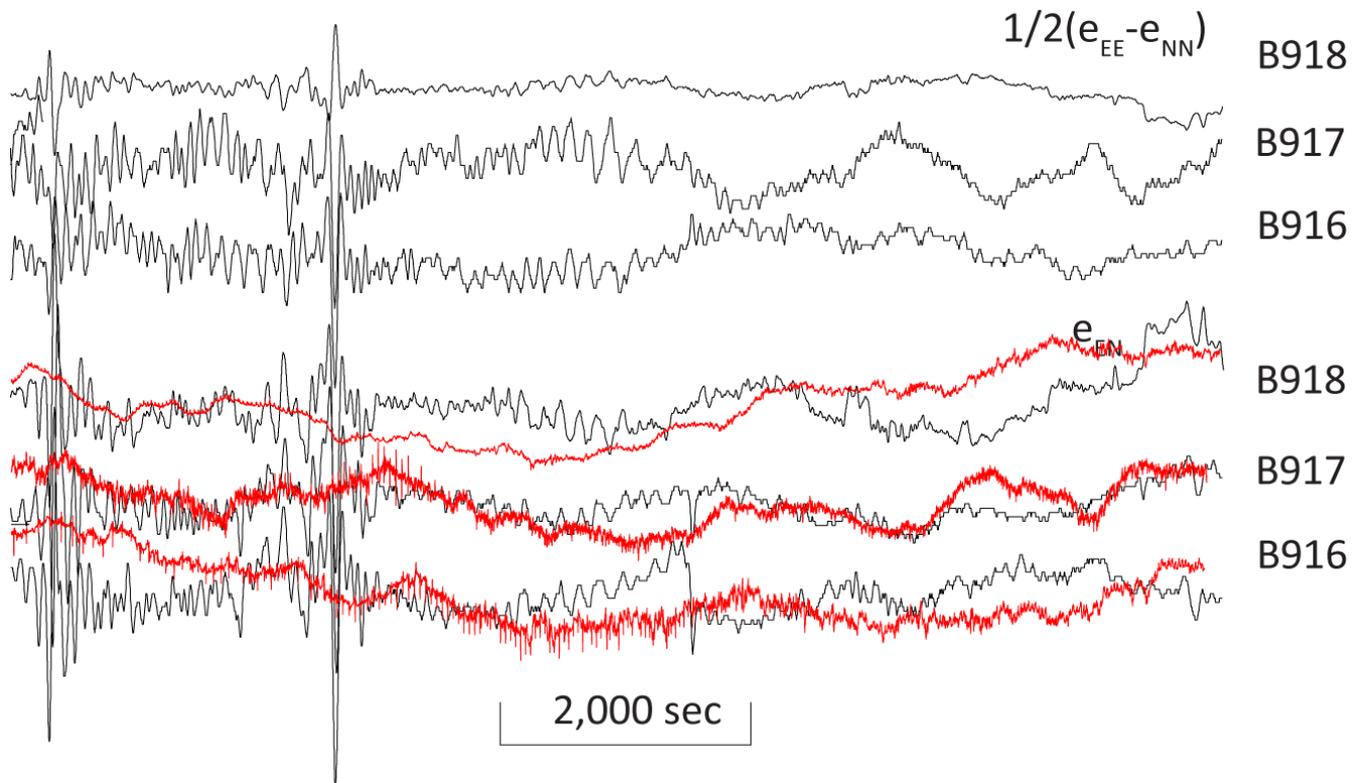


Strainmeter signals may fill duration gap not possible with seismic data, but...

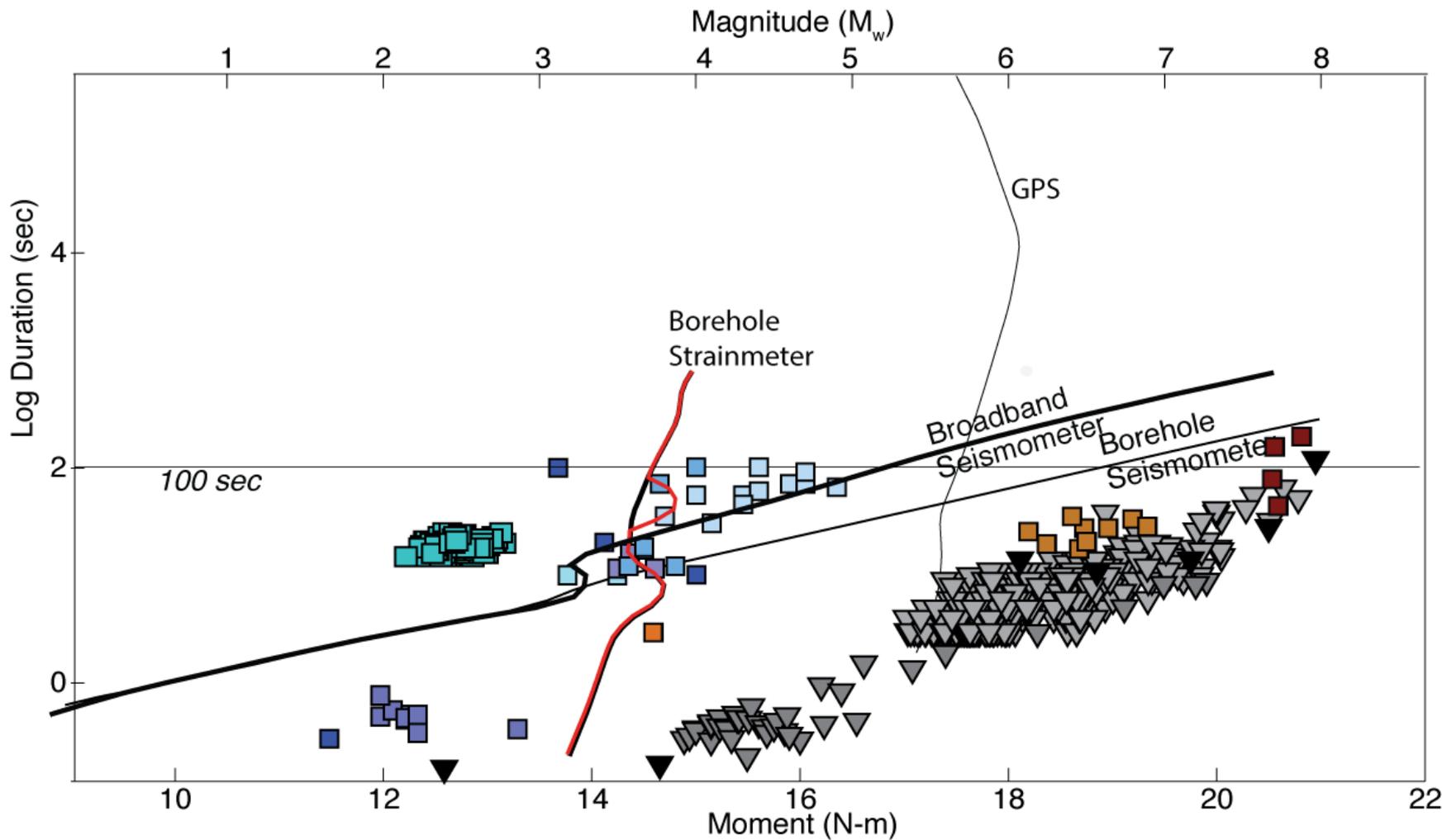


...beware the coherent noise (pressures)?

Haiti Earthquake Waves?  
Passband Periods > 60 sec  
Strainmeter Signals



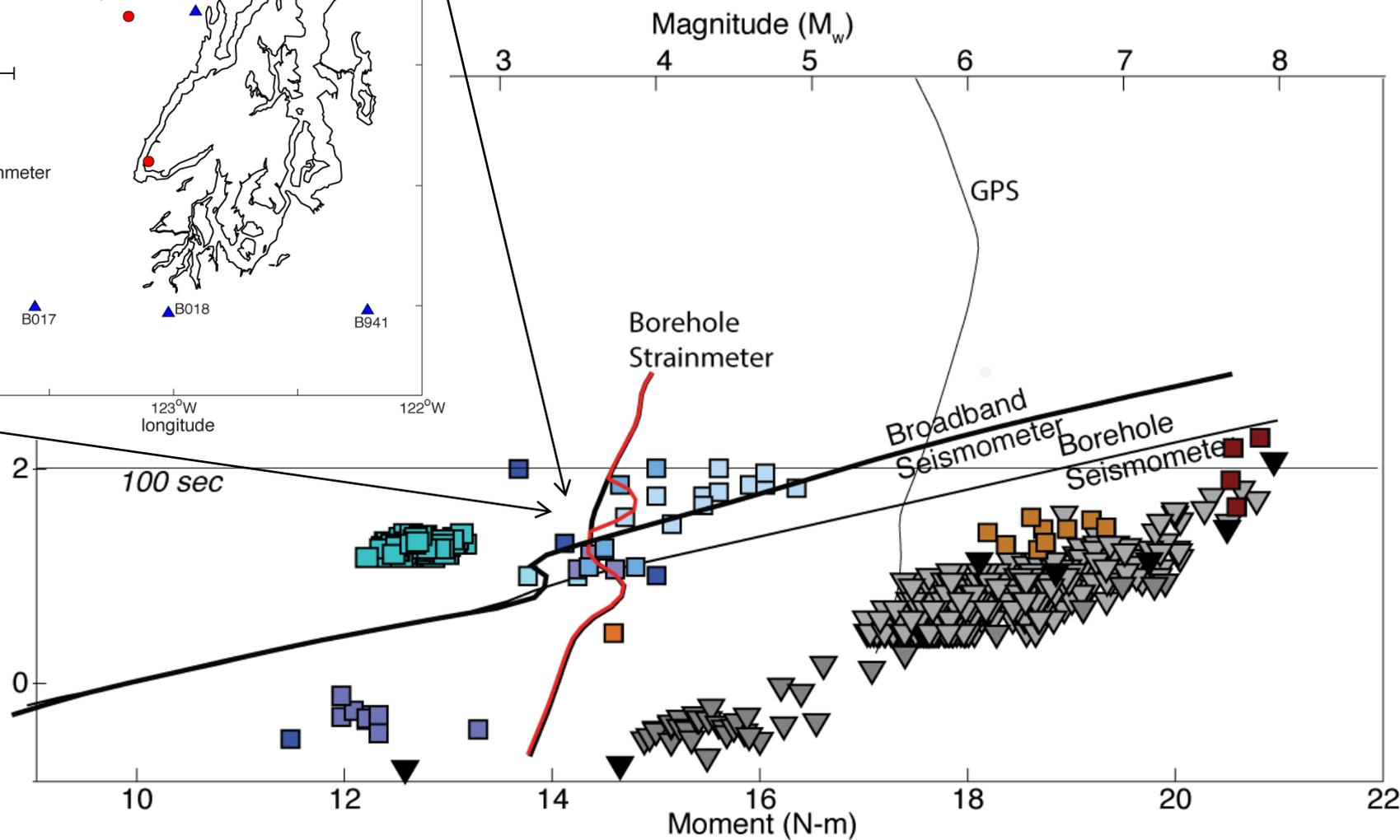
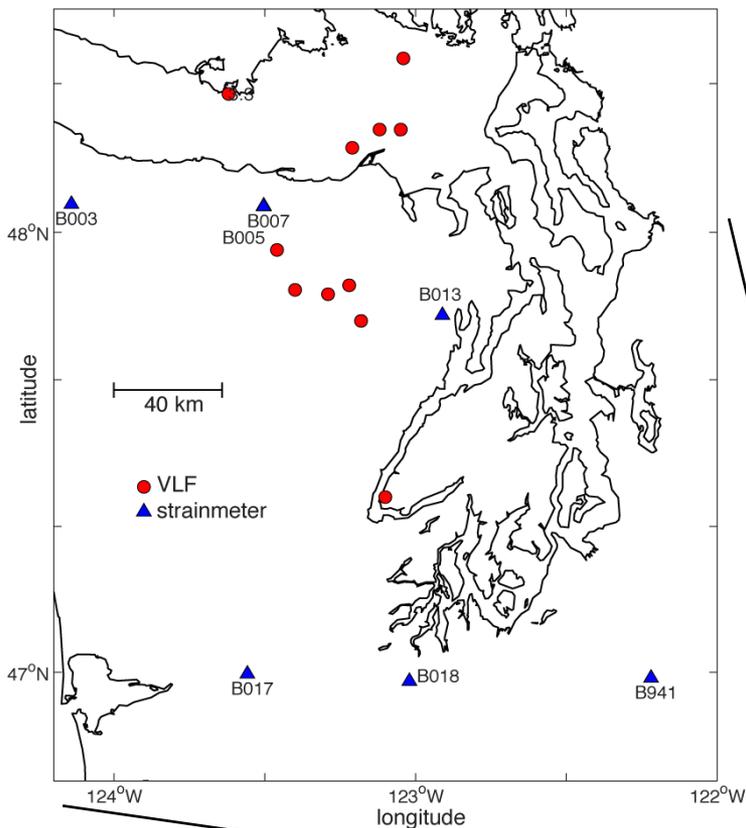
# Another possibility - 'Very Low Frequency' (VLF) Events Observable on strainmeters?



from Akiko Takeo

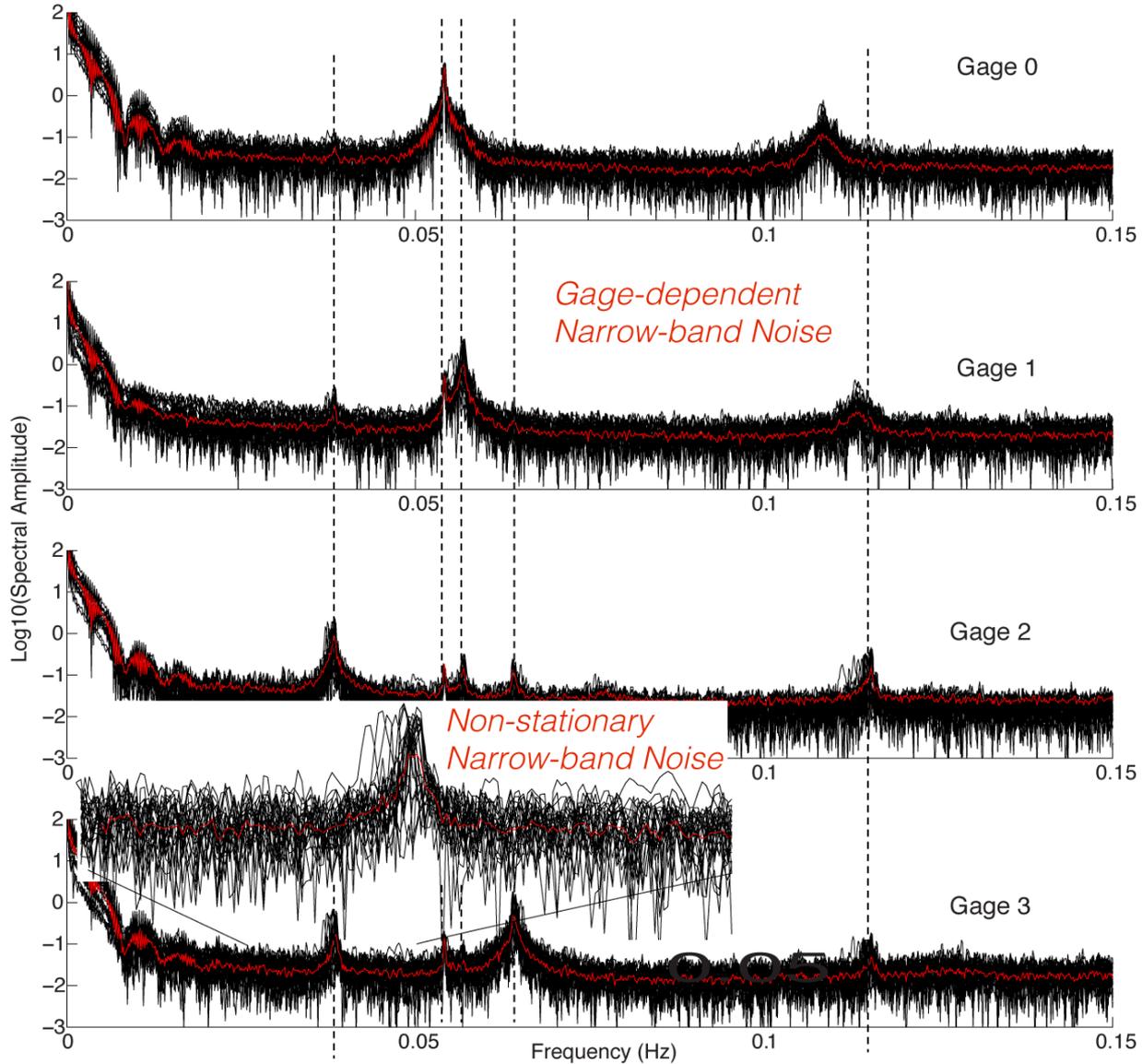
# Another possibility - VLF Events

'Observed' in stacked seismic data.

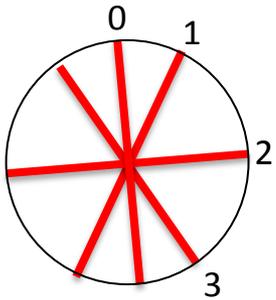


# Know thy data: 5) Non-stationary, narrow band electronic noise.

Gage Hourly Spectra, Station B013



Strainmeter  
= 4 gages

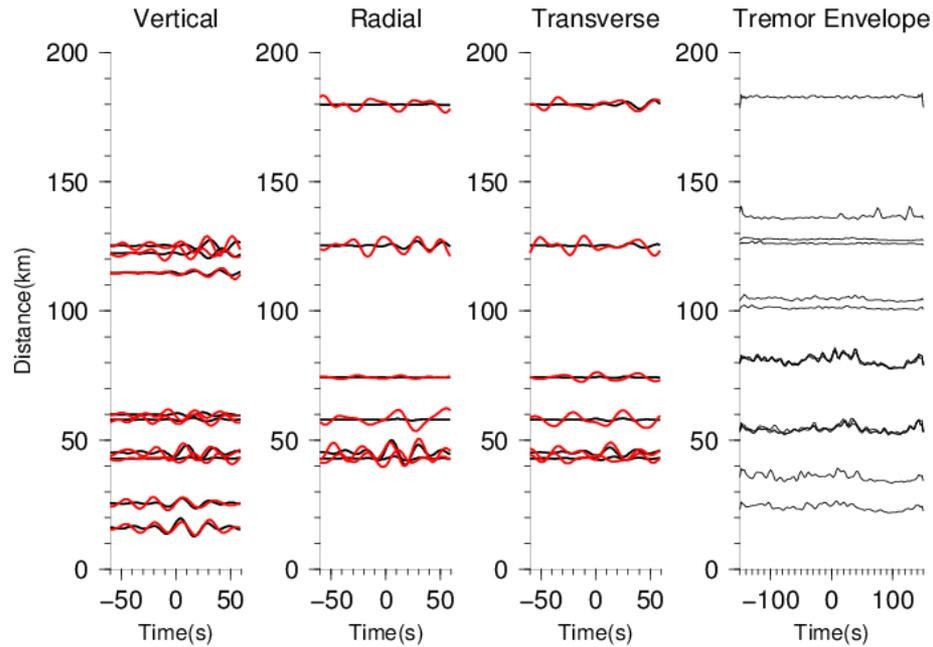
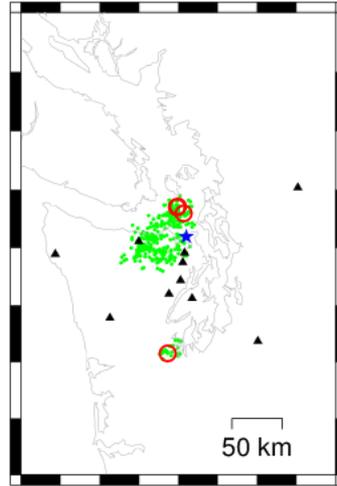


# Seismically Observed VLF Event

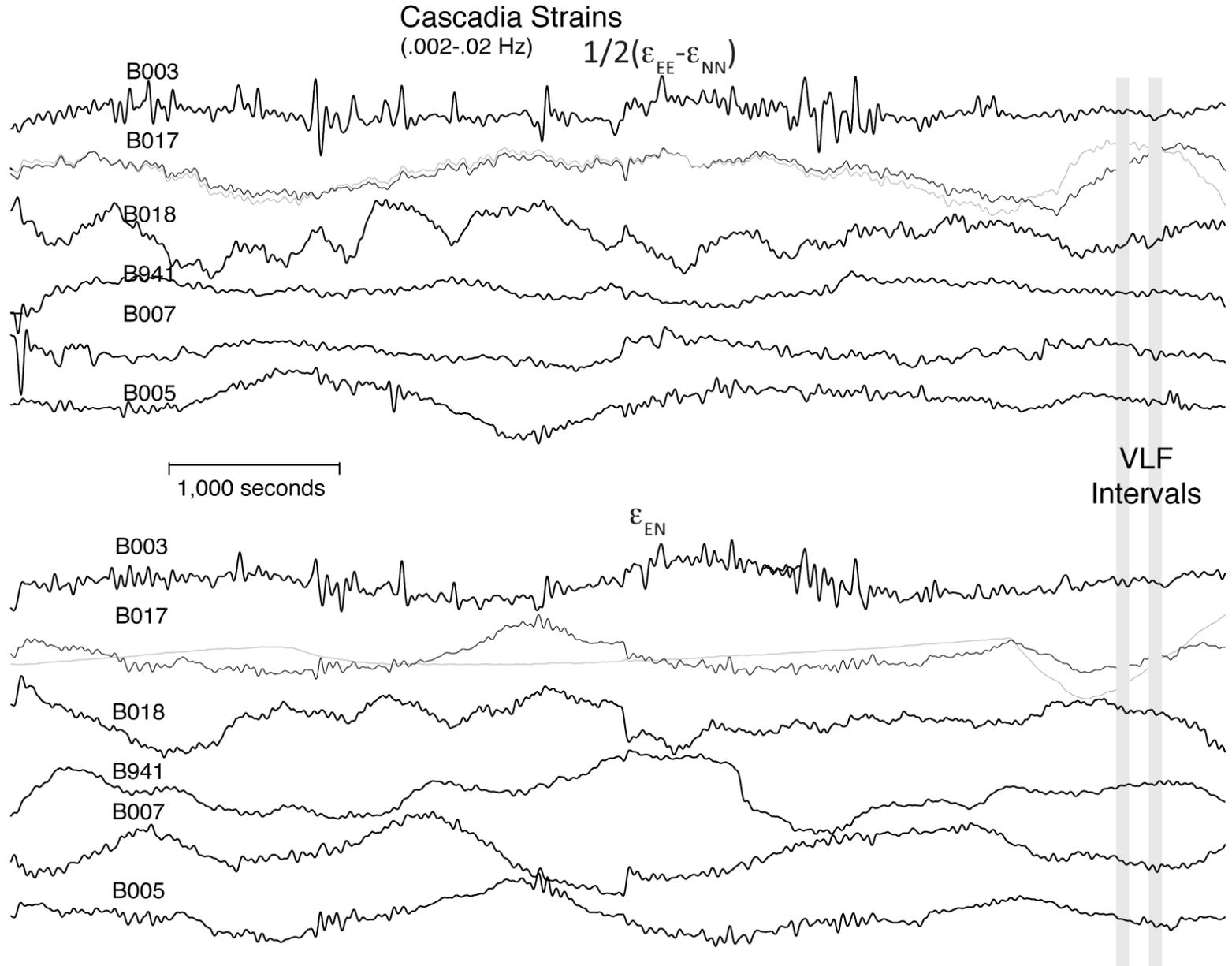
from Akiko Takeo



t0 30155.8 +/- 0.8  
Lon -123.05 +/- 0.07  
Lat 48.23 +/- 0.11  
Dep 35.00 +/- 0.00  
str1 332 +/- 17  
dip1 24 +/- 8  
rak1 74 +/- 12  
str2 170 +/- 63  
dip2 67 +/- 24  
rak2 97 +/- 98  
VR 37%  
Mw 3.3 +/- 0.0



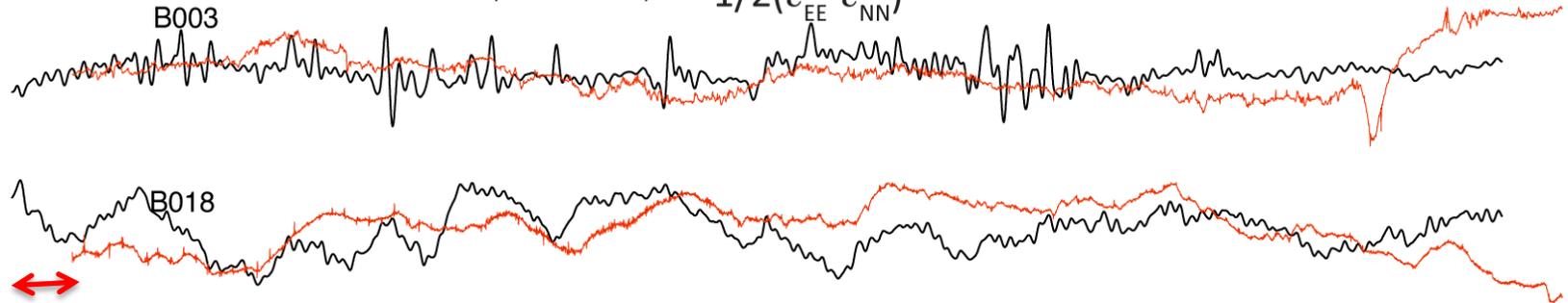
# Preliminary Strainmeter VLF Search – Nothing Found (as anticipated)



# Preliminary Strainmeter VLF Search – Strains drive pore pressure changes?

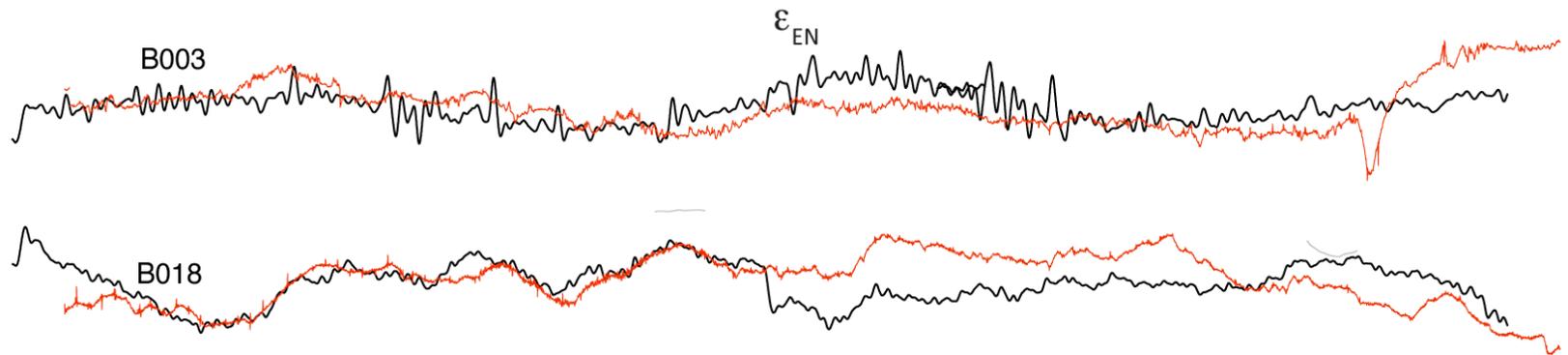
Cascadia Strains & Pore Pressures

(.002-.02 Hz)  $1/2(\epsilon_{EE} - \epsilon_{NN})$



Pore pressures  
lag strains

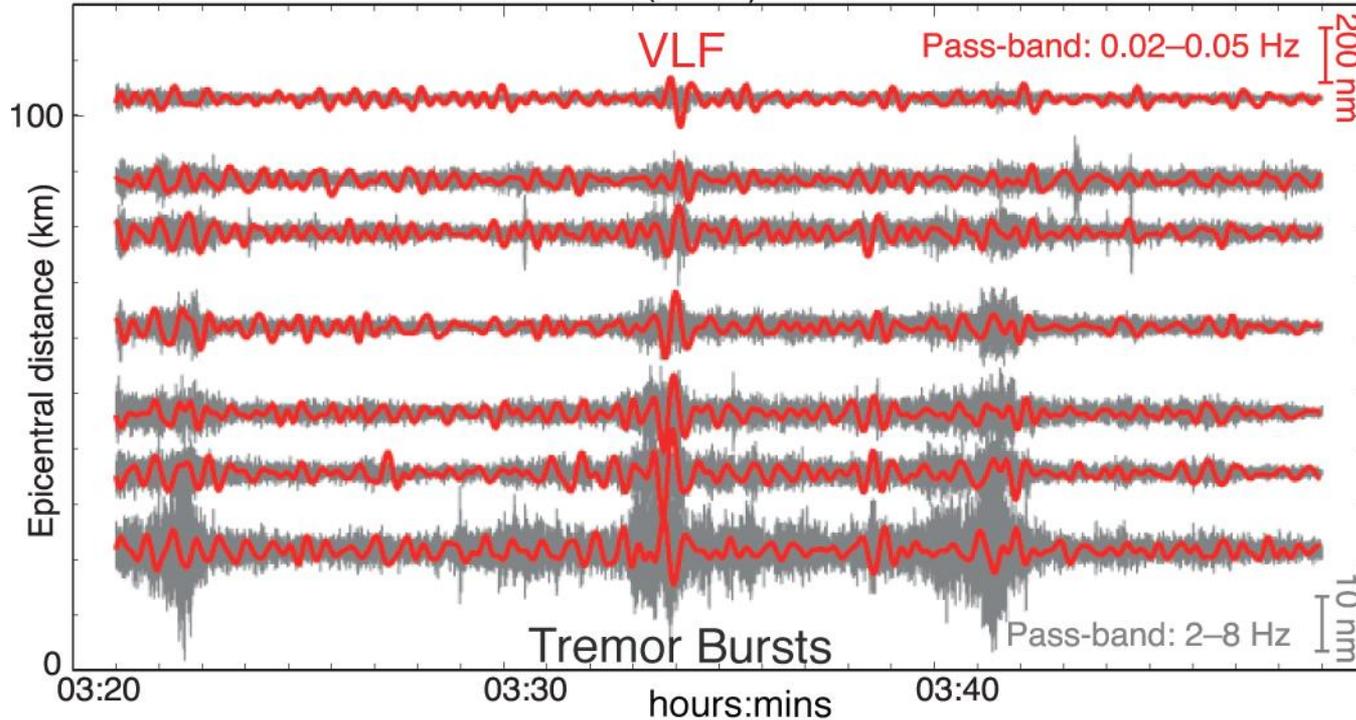
1,000 seconds



# What are these Very Low Frequency events?

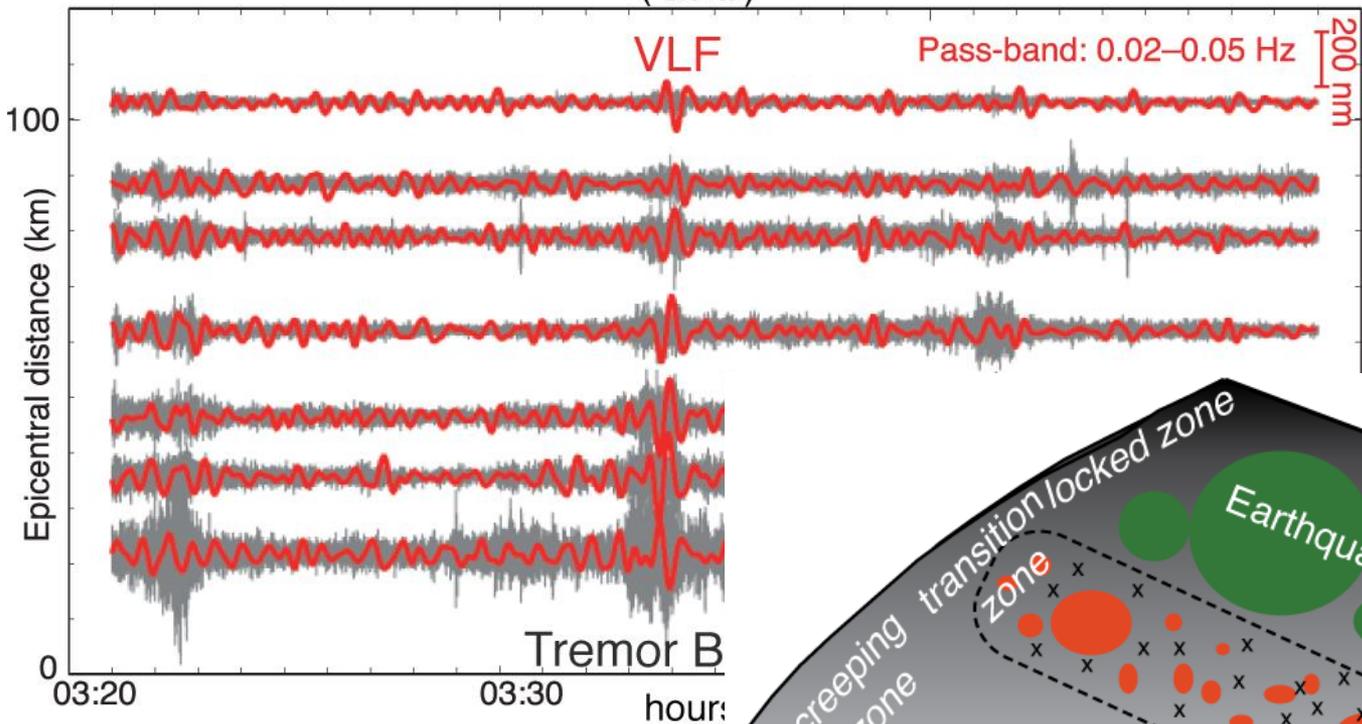
Always observed with tremor bursts.

Hi-net Tiltmeter Displacements  
(radial)

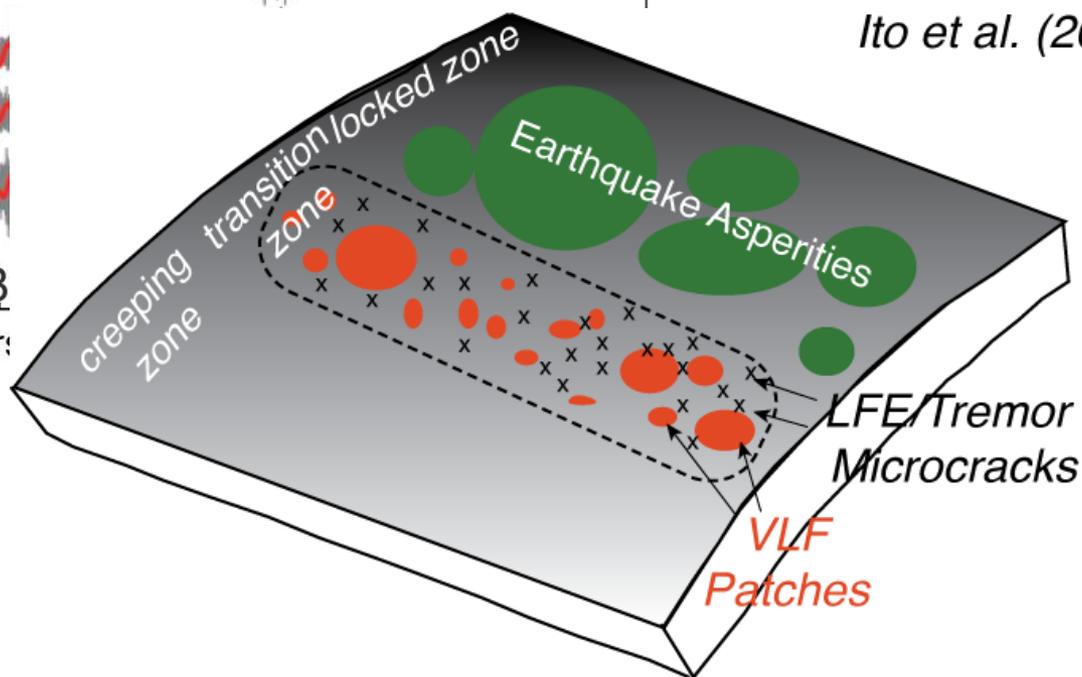


# Inferred 'slow', M3-4, seismic sources.

Hi-net Tiltmeter Displacements  
(radial)



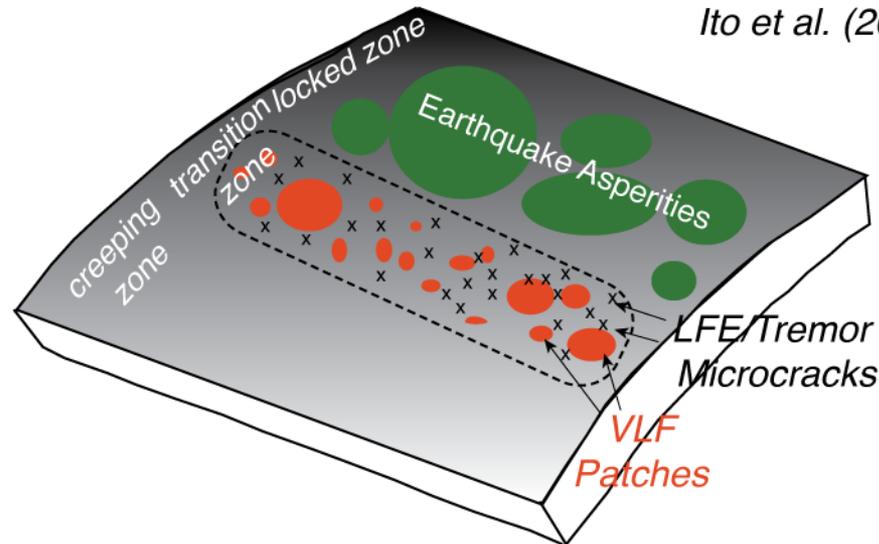
*Ito et al. (2007)*



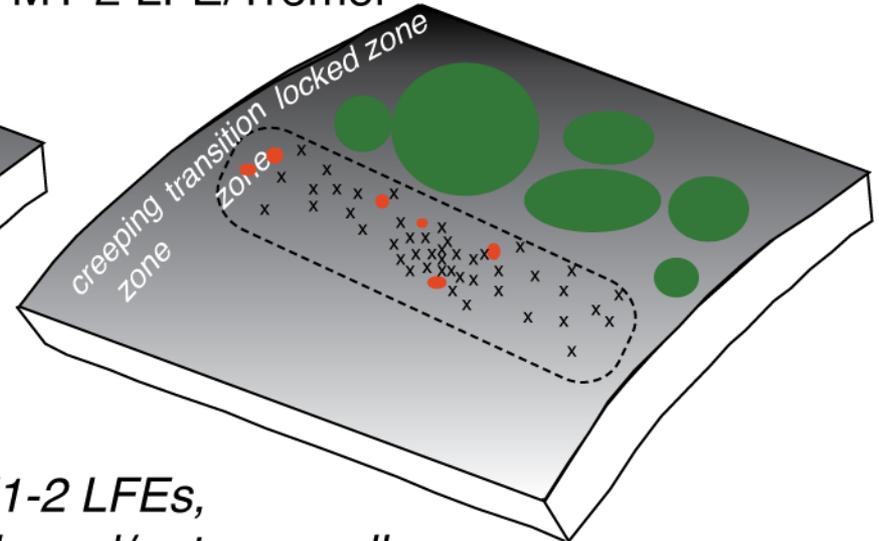
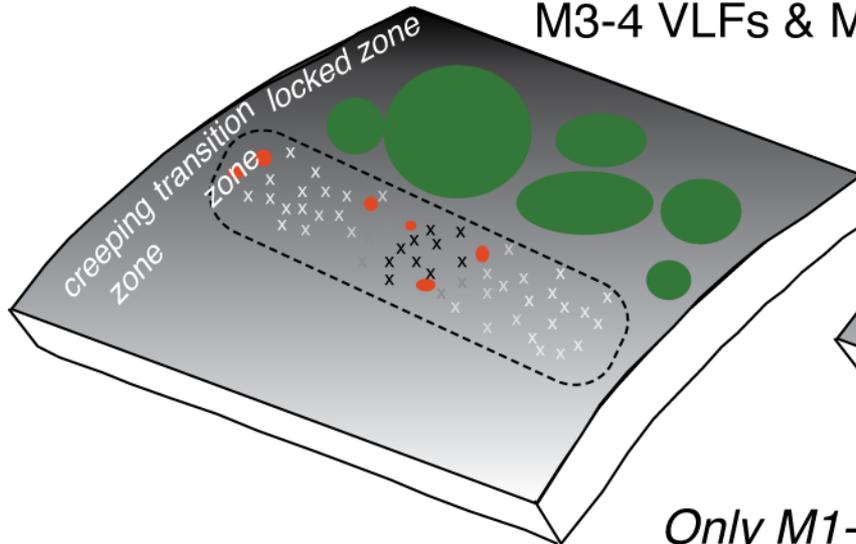
# Are VLFs really distinct M3-4 sources?

Consider what is being measured & alternative interpretations -

*Ito et al. (2007)*

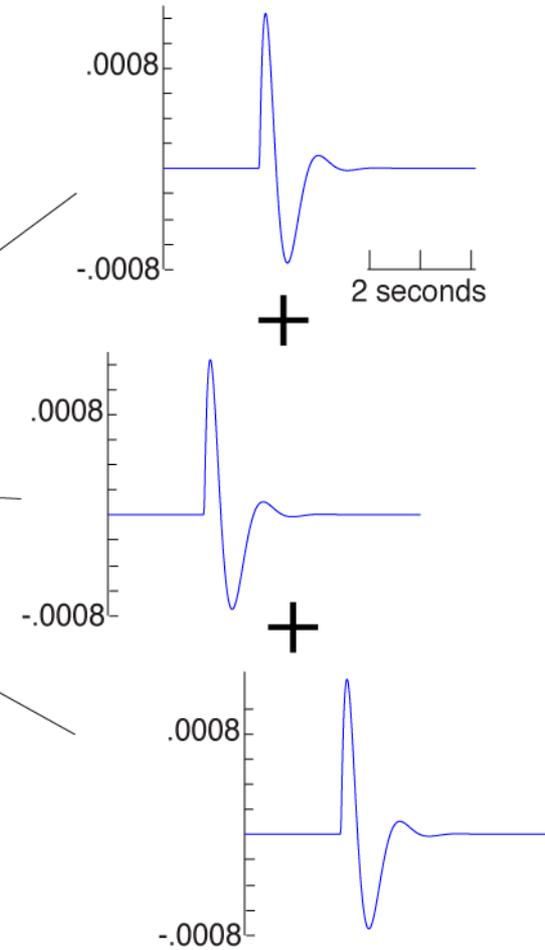
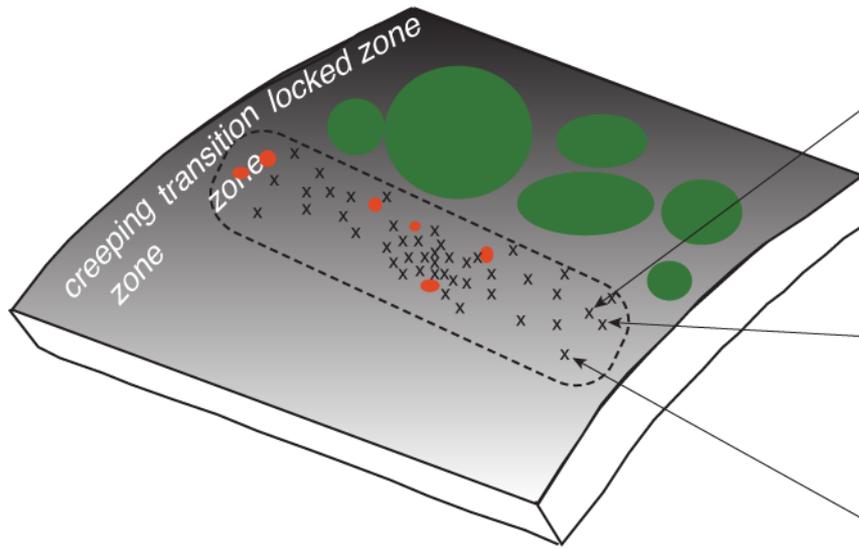


M3-4 VLFs & M1-2 LFE/Tremor

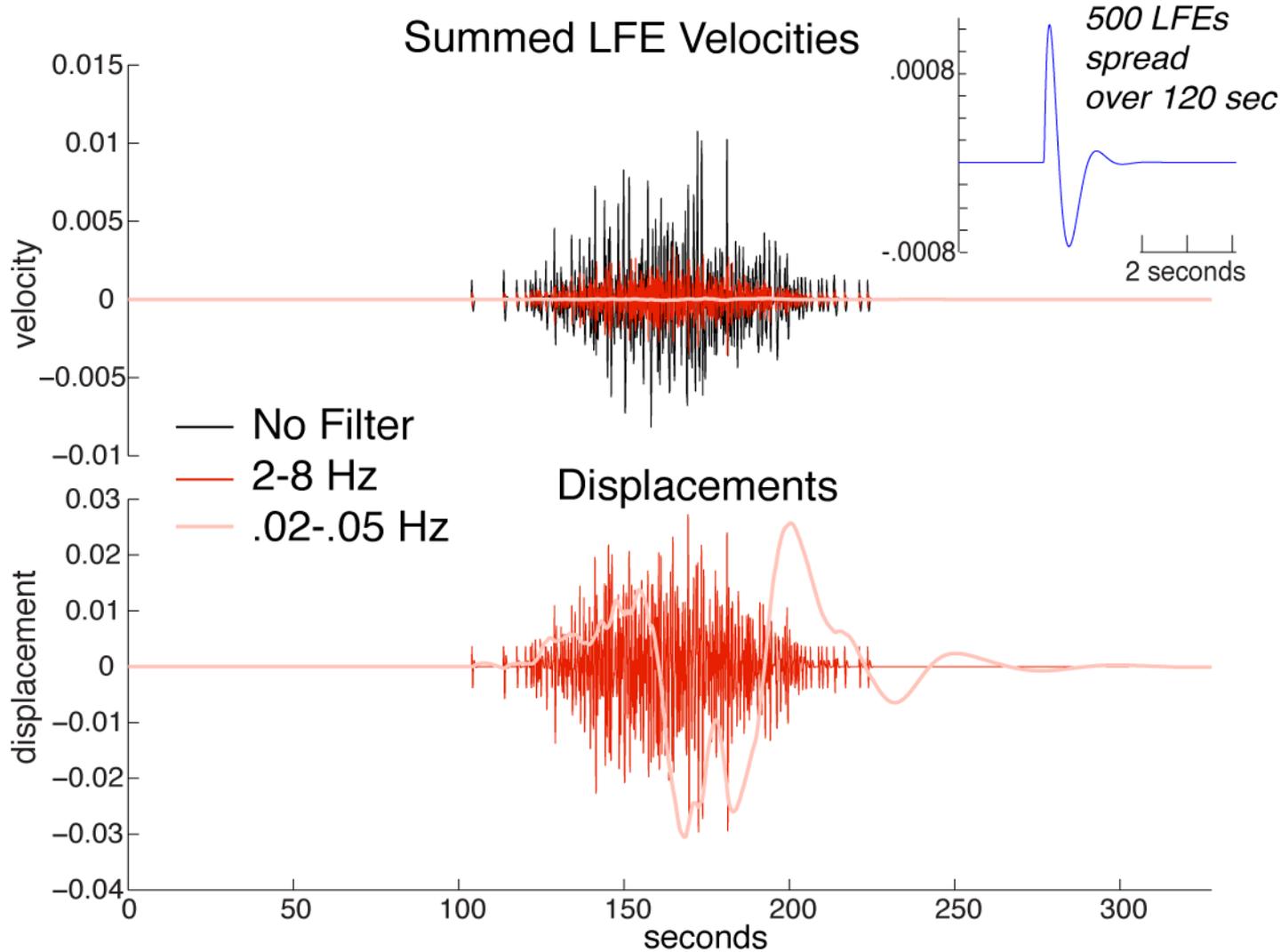


*Only M1-2 LFEs,  
clustered spatially and/or temporally*

# Alternative VLF interpretation –summed LFEs? Synthetic example.



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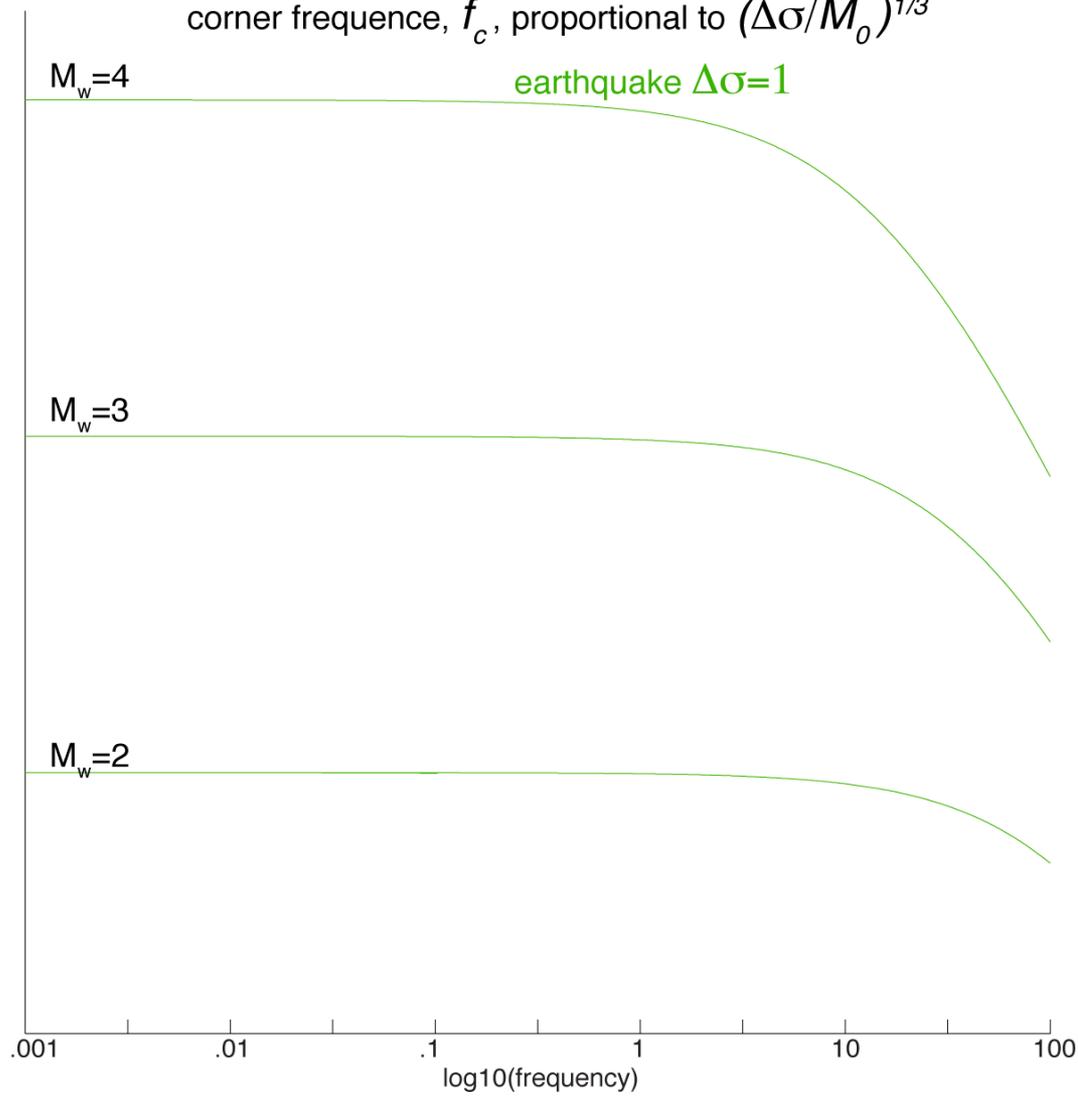


# Quick Primer on Source Spectral Scaling

## Spectral Scaling

$$\text{spectral amplitude} = \frac{M_0}{(1+f/f_c)^2}$$

corner frequency,  $f_c$ , proportional to  $(\Delta\sigma/M_0)^{1/3}$

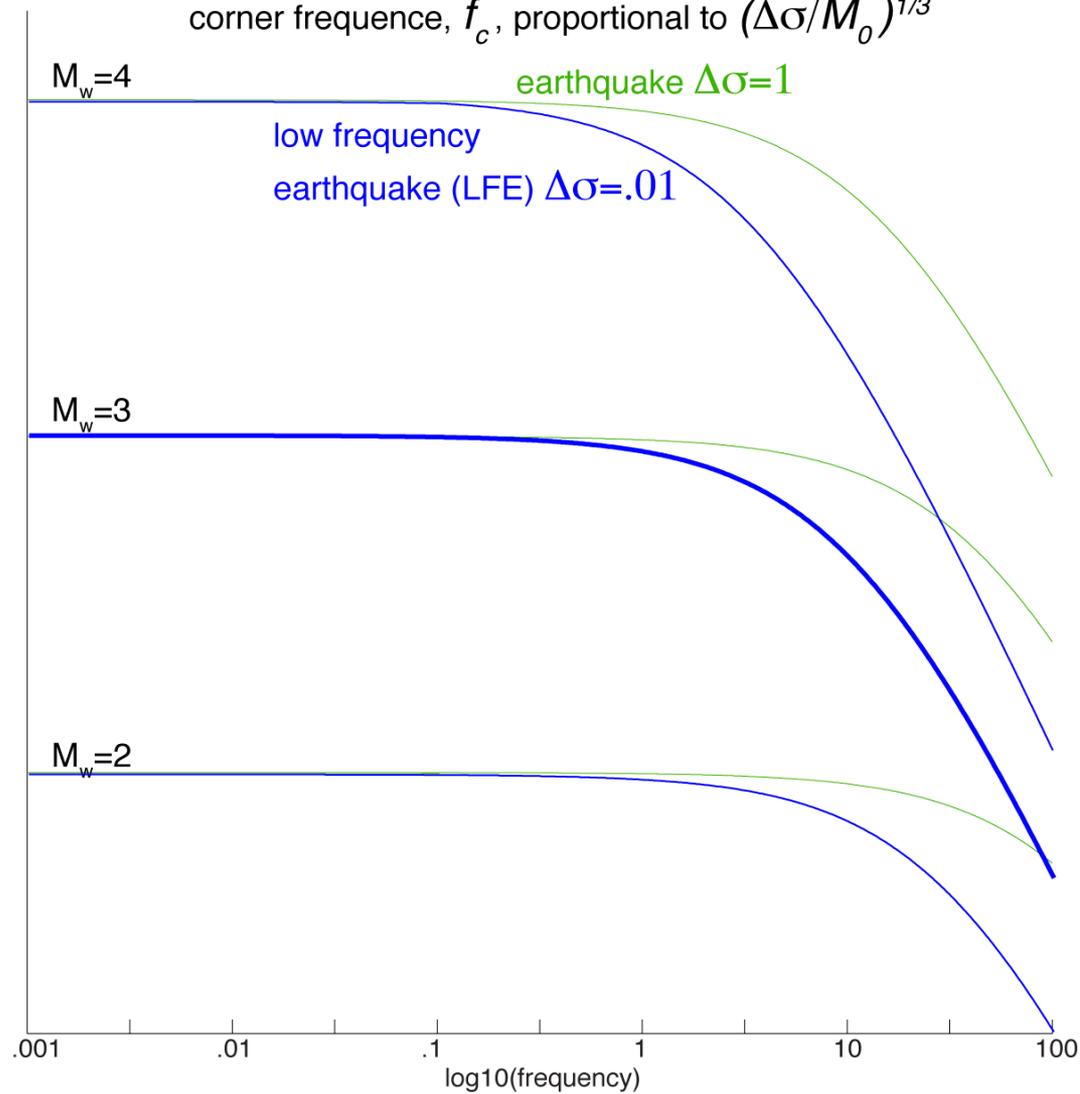


Low frequency events may have low stress drops.

## Spectral Scaling

$$\text{spectral amplitude} = \frac{M_0}{(1+f/f_c)^2}$$

corner frequency,  $f_c$ , proportional to  $(\Delta\sigma/M_0)^{1/3}$

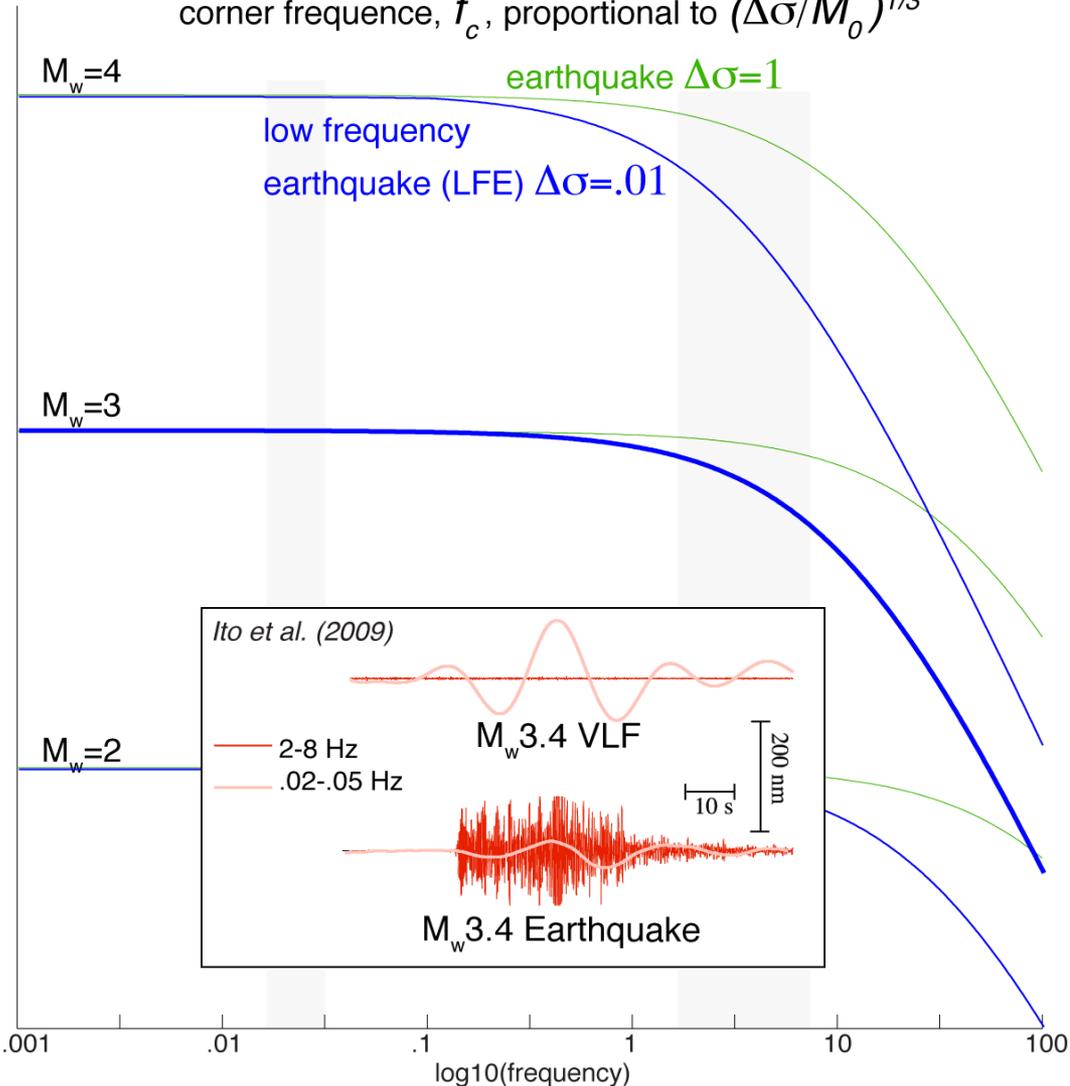


# Explains comparisons of VLFs & LFEs with earthquakes.

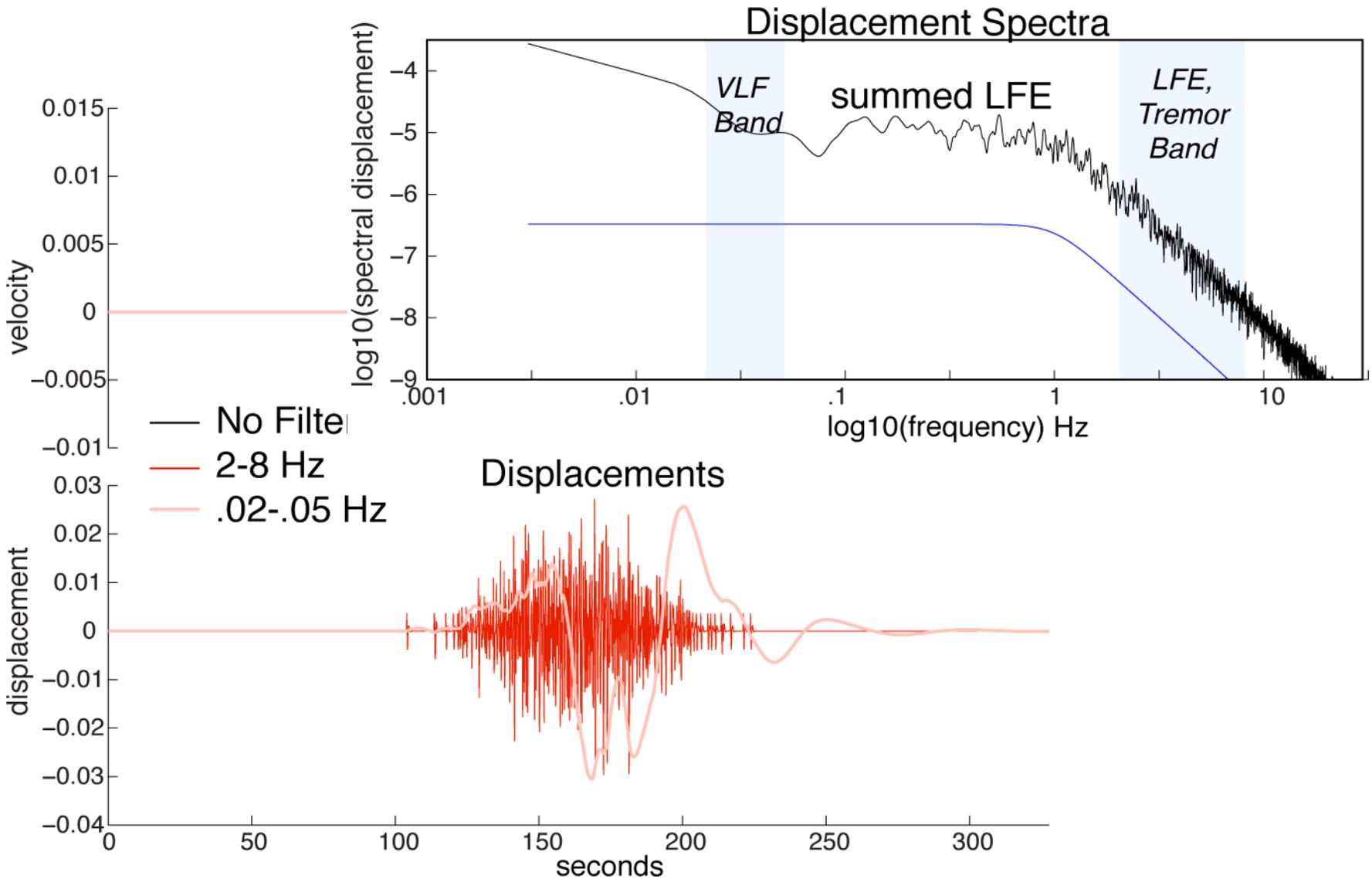
## Spectral Scaling

$$\text{spectral amplitude} = \frac{M_0}{(1+f/f_c)^2}$$

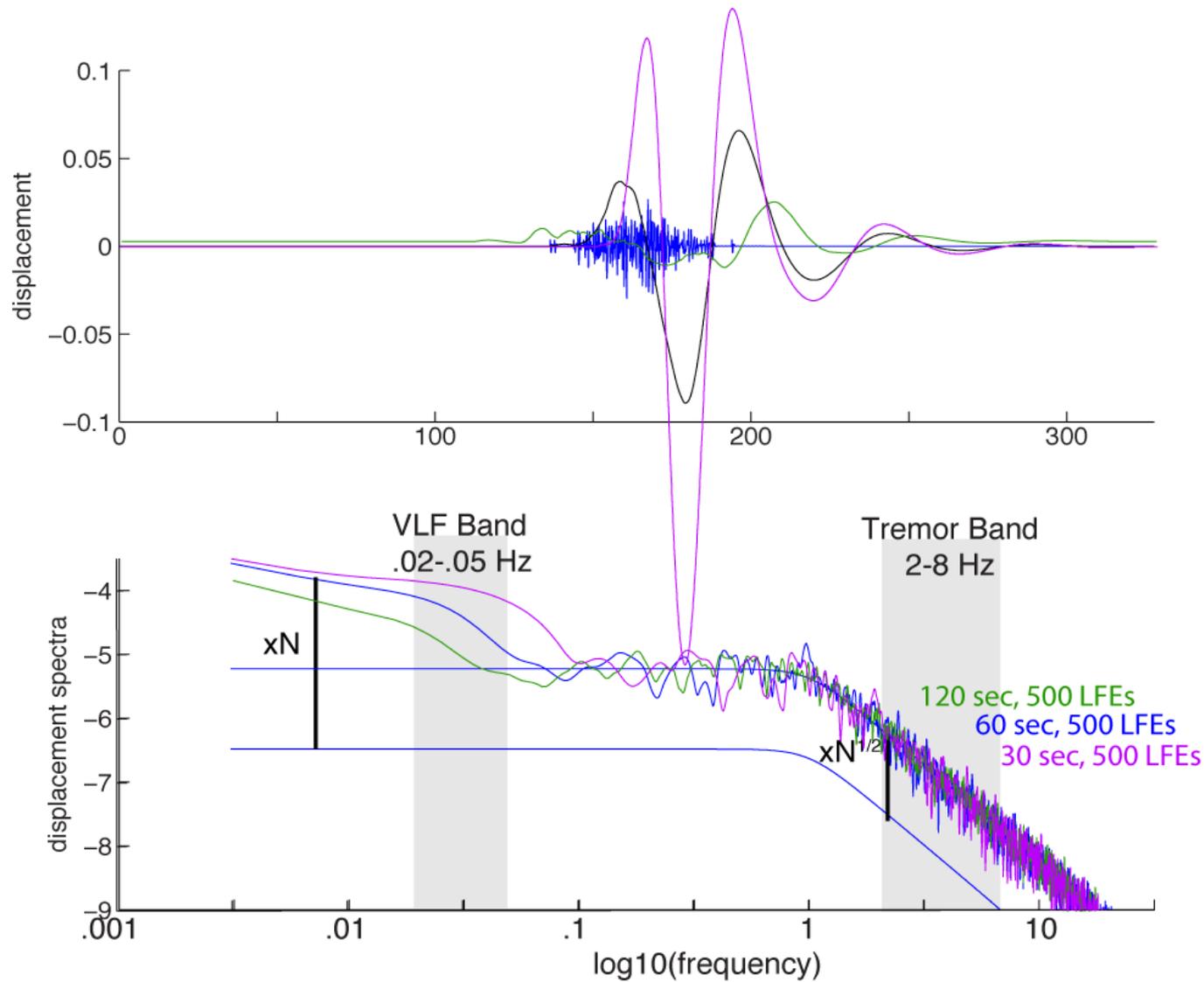
corner frequency,  $f_c$ , proportional to  $(\Delta\sigma/M_0)^{1/3}$



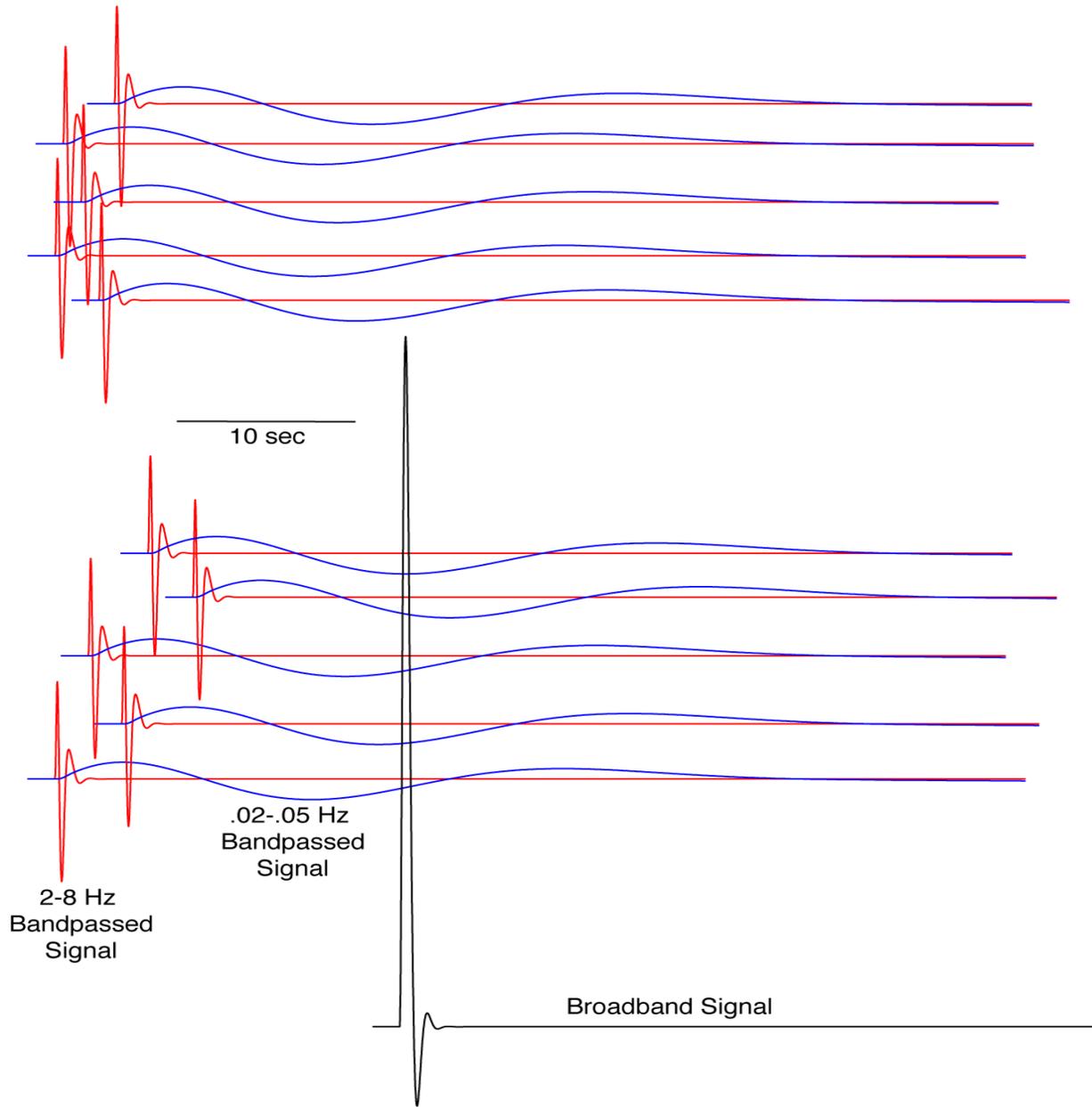
# Summed LFEs = larger VLF, almost...



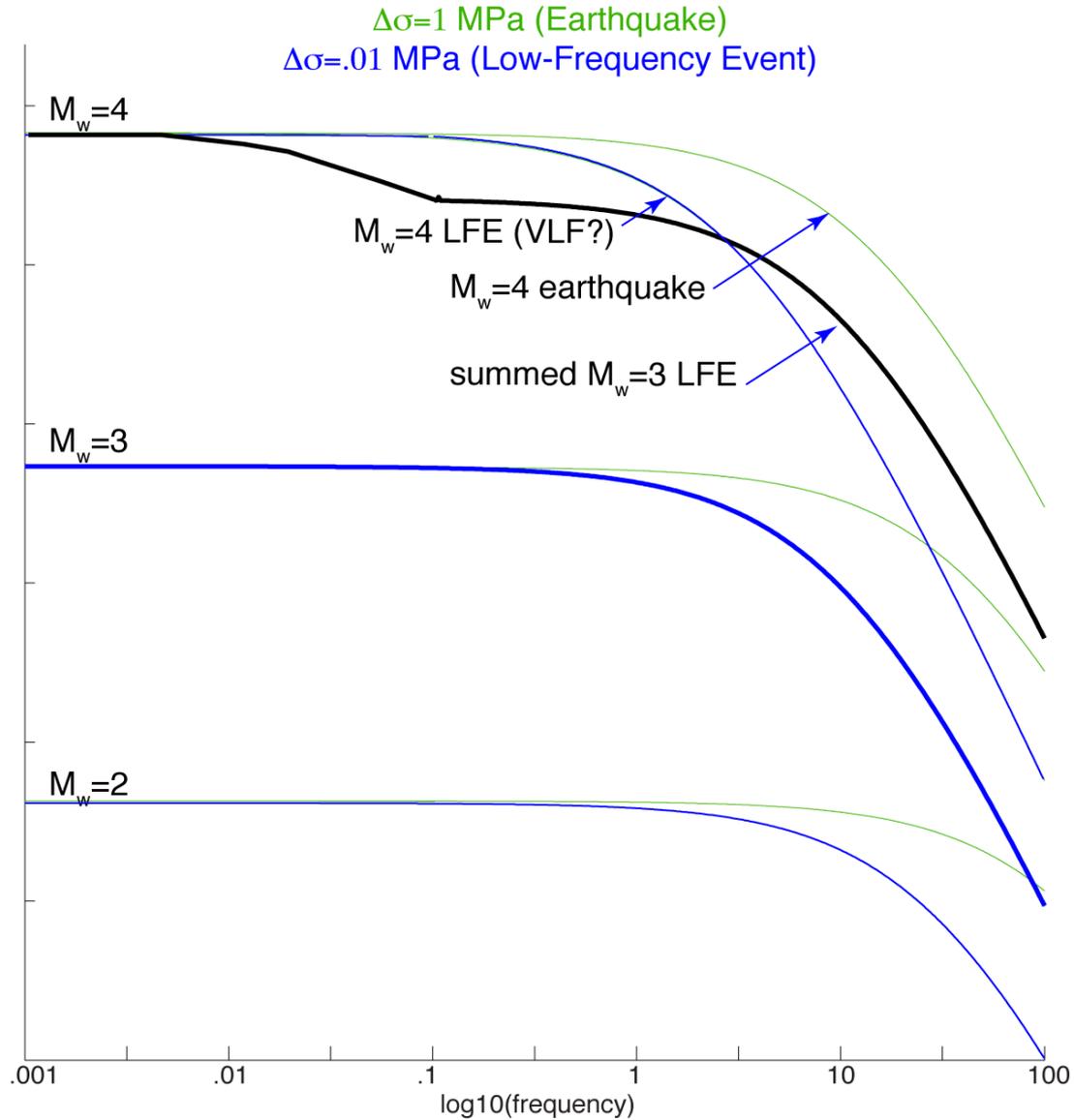
The more clustered LFEs are, the more coherently low frequencies add (sum  $\sim$ linearly). High frequencies always add incoherently (sum as  $\sqrt{N}$ ).



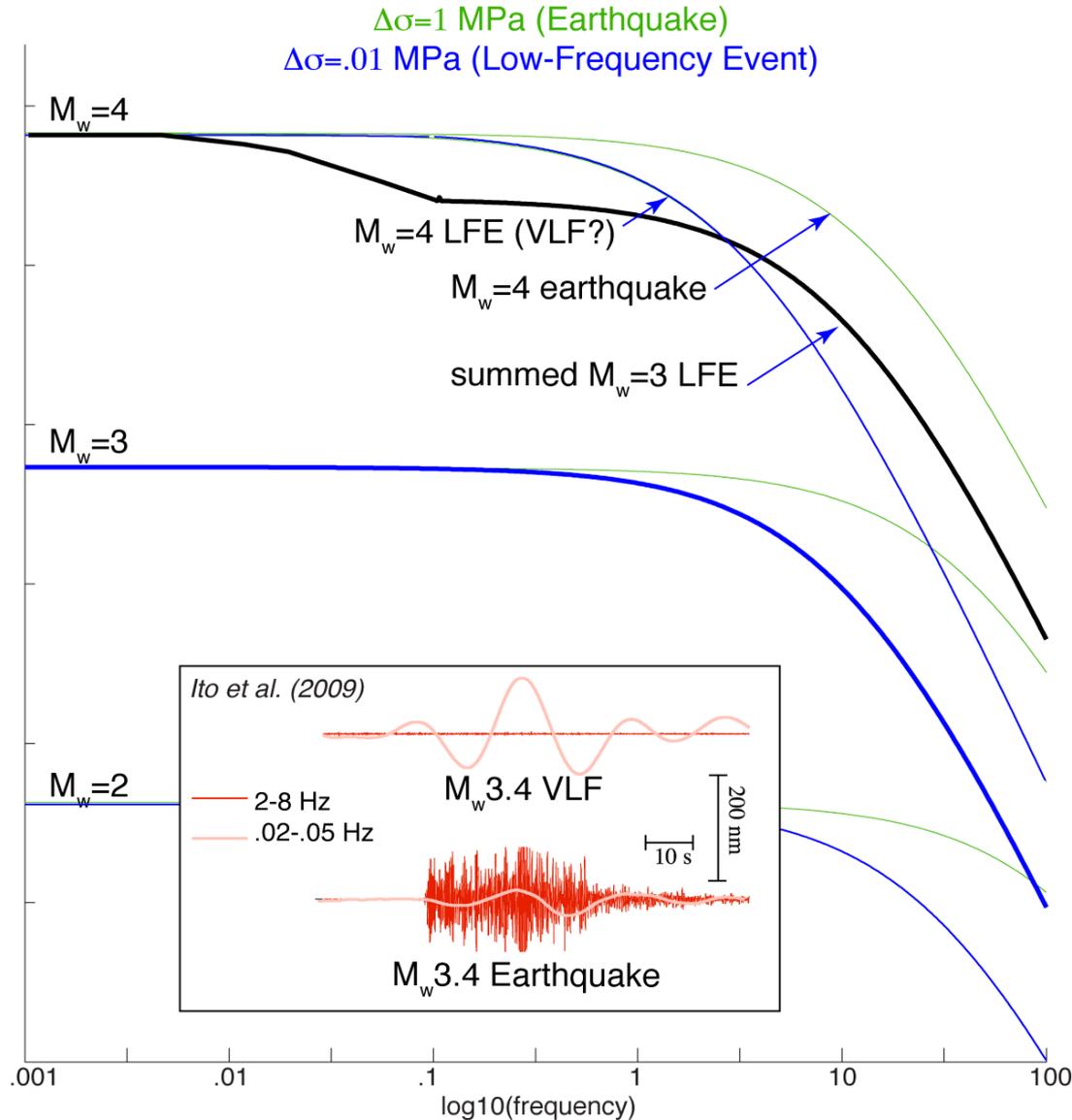
The more clustered LFEs are, the more coherently low frequencies add (sum  $\sim$ linearly). High frequencies always add incoherently (sum as  $\sqrt{N}$ ).



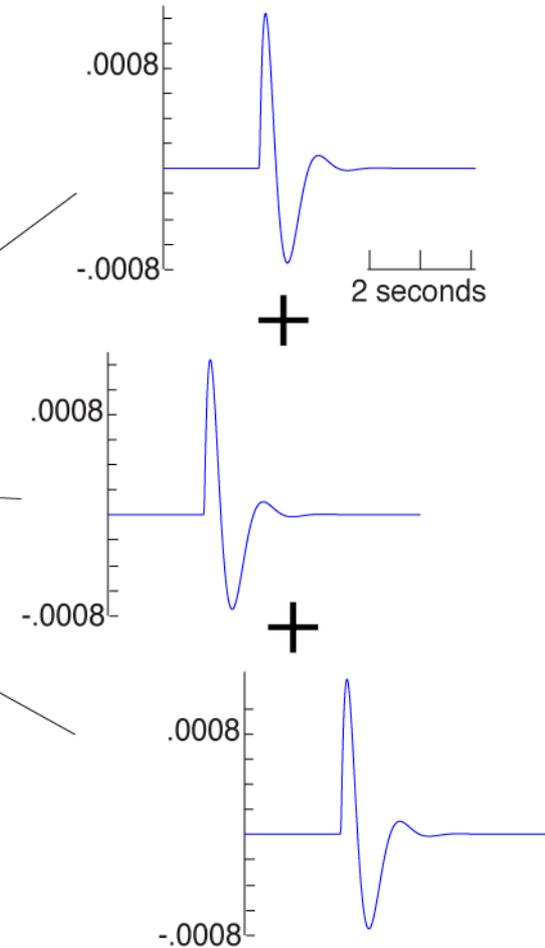
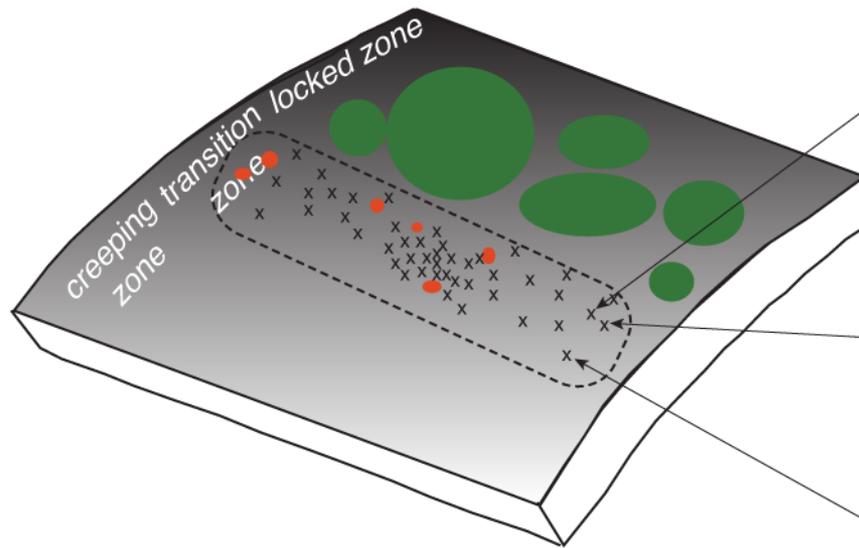
# Summed LFEs = larger VLF, almost... *has excess high frequencies*



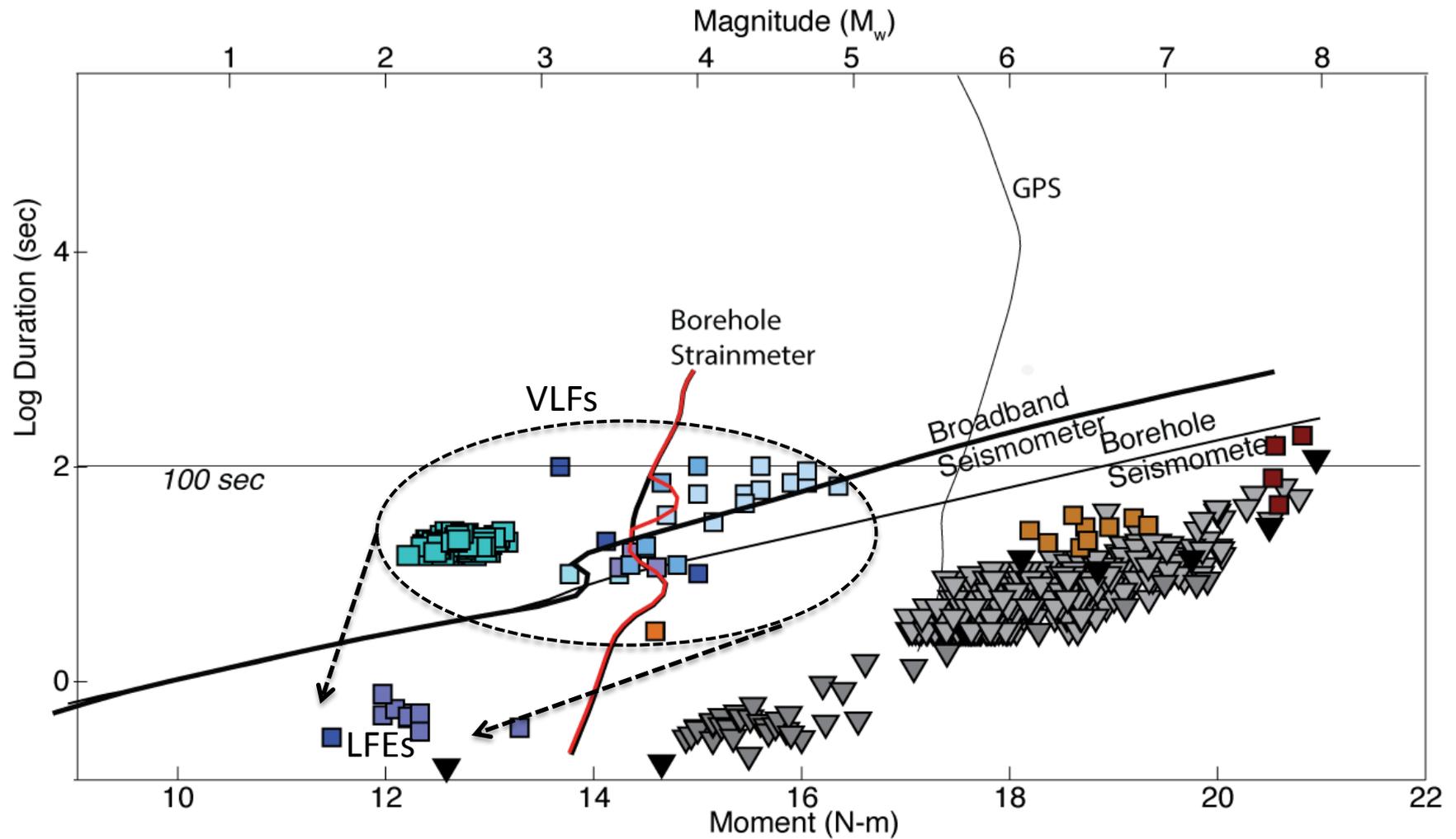
# Summed LFEs = larger VLF, almost... has excess high frequencies *but still less than an earthquake.*



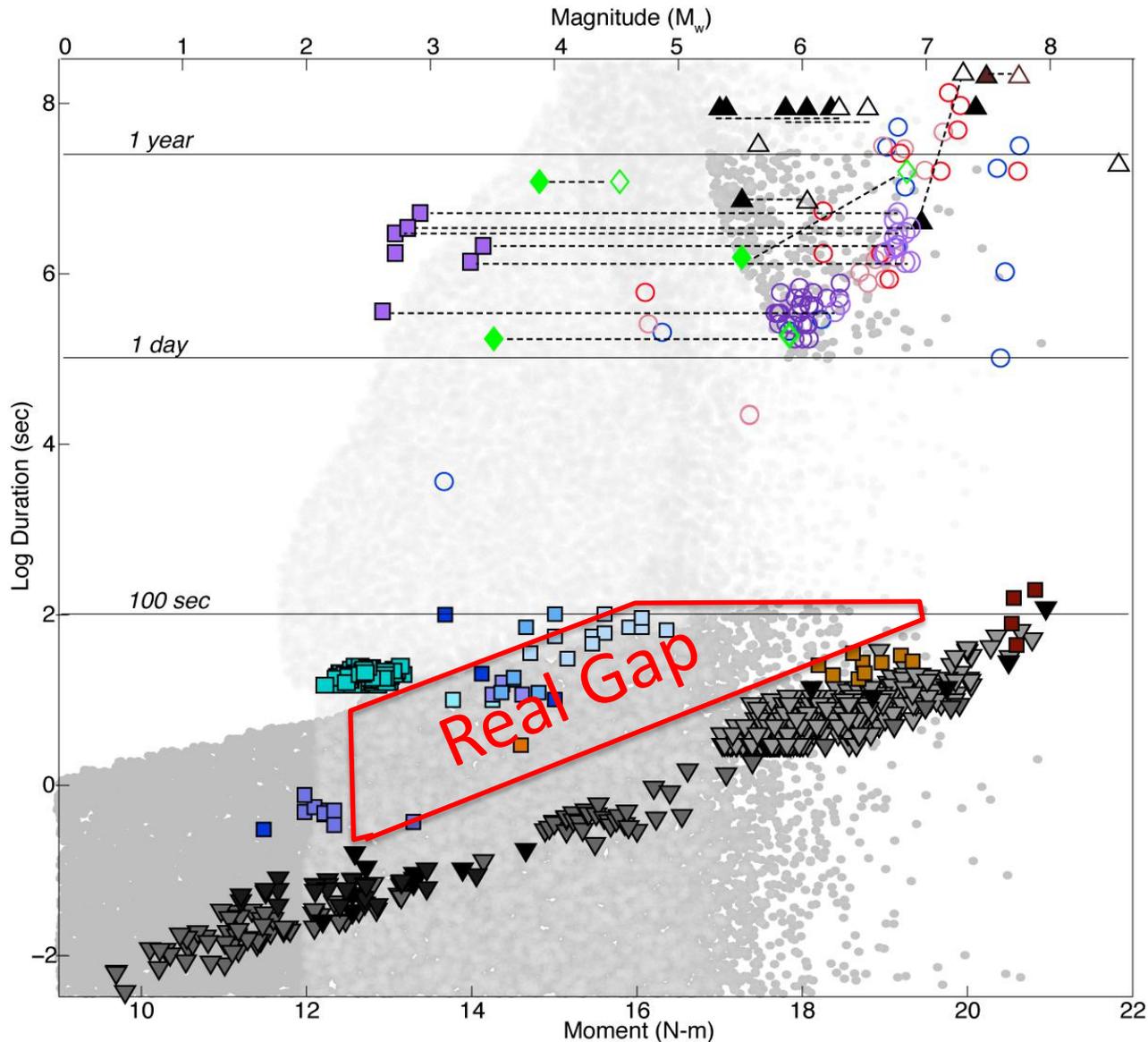
# VLFs may just be tremor 'bursts', comprised of clusters of randomly summed LFEs



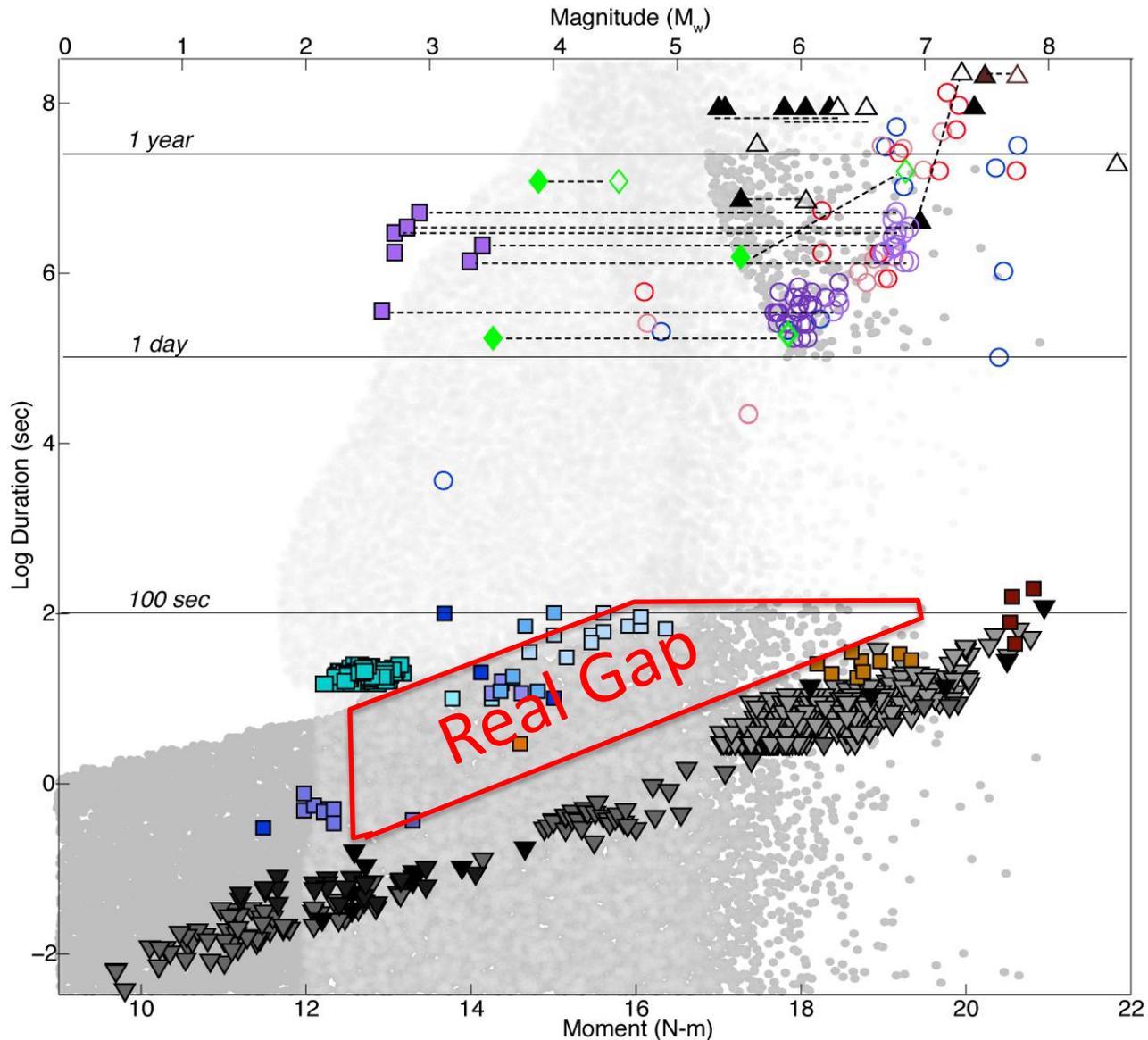
# Consider how you interpret what you're measuring!



What we 'see' may just reflect our observational windows.  
We need bigger windows before making scaling inferences.



New measurement types may open new windows. We also need to uniquely determine what's being measured!



Thank you!