



Institut des Sciences de la Terre

European Research Council

Adv. Grant Whisper



"Seismic velocity changes and deformation of the crust: the signatures of earthquakes and transient slip events. "

Michel Campillo (with Bérénice Froment, Dimitri Zigone, Diane Rivet, Anne Obermann, Gregor Hillers, Julien Chaput, Andrea Colombi, Kentaro Emoto, Pierre Boué and colleagues from ISTerre, IPGP, USC, U. Illinois, NEID, UNAM, Tohoku U., CEA Beijing..)

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Interest in seismology for temporal changes of elastic properties since (at least) the 60s.

Laboratory experiments show that the elastic velocities are actually changing due to external sollicitations (waves, impacts e.g. TenCate and coll.) or to weak deformations (e.g. Schubnel et coll.).

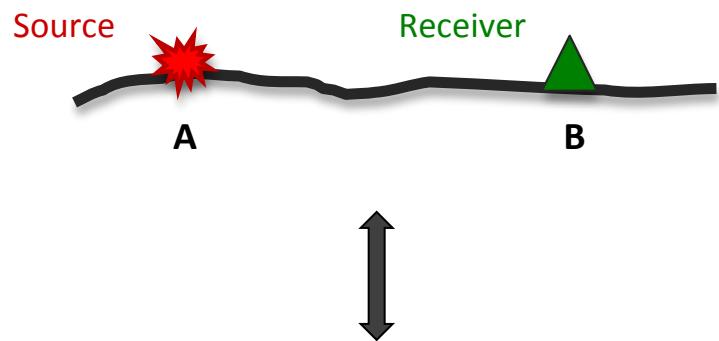
Nonlinear Mesoscopic Elasticity : fast and slow dynamics

Could we detect, and eventually image continuous temporal changes of seismic wave velocity at depth that could be used to characterize the deformation rate?

This story is about this question....

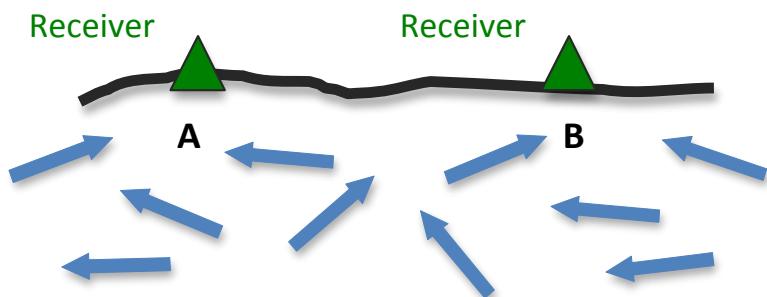
- 1- Introduction
- 2- Ambient noise correlations: what can we trust?
- 3- Imaging fault structures
- 4- Monitoring: what can we trust?
- 5- Parkfield → possible ‘non tectonic’ signals?
- 6- SSE in Guerrero, Mexico → deep deformations, tremors, (triggering)
- 7- Wenchuan imaging, delays?
- 8- Japan= mapping the susceptibility to non linear effects

Long range correlations



Source in A \Rightarrow the signal recorded in B characterizes the propagation between A and B.

→ **Green function** between A and B: G_{AB}



G_{AB} can be reconstructed by the correlation (C_{AB}) of 'noise' from randomly distributed sources
or
« diffuse » (equipartitioned) fields recorded at A and B

A way to provide new data with control on source location and origin time

Experimentally verified with seismological data:
Coda waves: Campillo and Paul, 2003,.....
Ambient noise: Shapiro and Campillo, 2004,.....

Mathematical basis

Arbitrary medium: an integral representation written in the frequency domain

$$G_{12} - G_{12}^* = \frac{4i\omega\kappa}{c} \int_V G_{1x} G_{2x}^* dV + \oint_S [G_{1x} \vec{\nabla} (G_{2x}^*) - \vec{\nabla} (G_{1x}) G_{2x}^*] \vec{dS}$$

FT of $G(-t)$ Volume term Surface term
 FT of $G(t)$
 Absorption coefficient
 Source average over « correlation terms »

Surface term:

$\kappa = 0$ (no attenuation)

$$G_{12} - G_{12}^* = \oint_S \left[G_{1x} \vec{\nabla} \left(G_{2x}^* \right) - \vec{\nabla} \left(G_{1x} \right) G_{2x}^* \right] d\vec{S}$$

If the surface is taken in the far field of the medium heterogeneities

$$G_{1x} \sim \frac{1}{4\pi |\vec{x} - \vec{r}_1|} \exp(-ik|\vec{x} - \vec{r}_1|) \text{ and } \vec{\nabla}(G_{1x}) \sim ik G_{1x}$$

and we obtain a widely used integral relation:

$$G_{12} - G_{12}^* = -2i \frac{\omega}{c} \oint_S G_{1x} G_{2x}^* dS$$

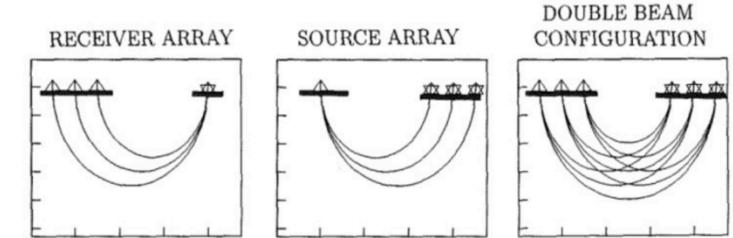
→ Derode et al., 2003: Analogy with Time reversal mirrors

→ Wapenaar 2004

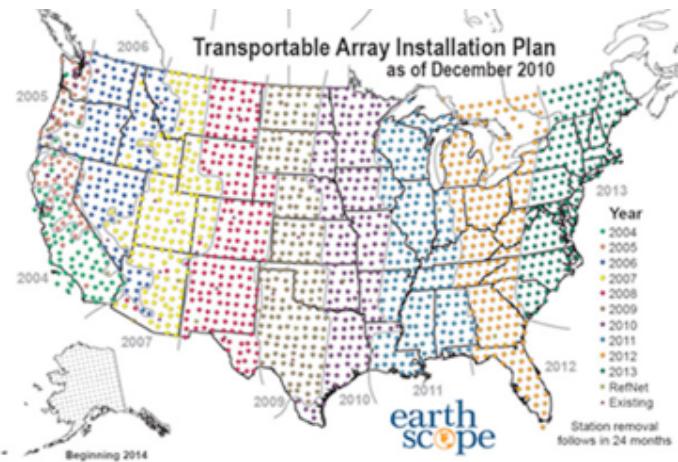
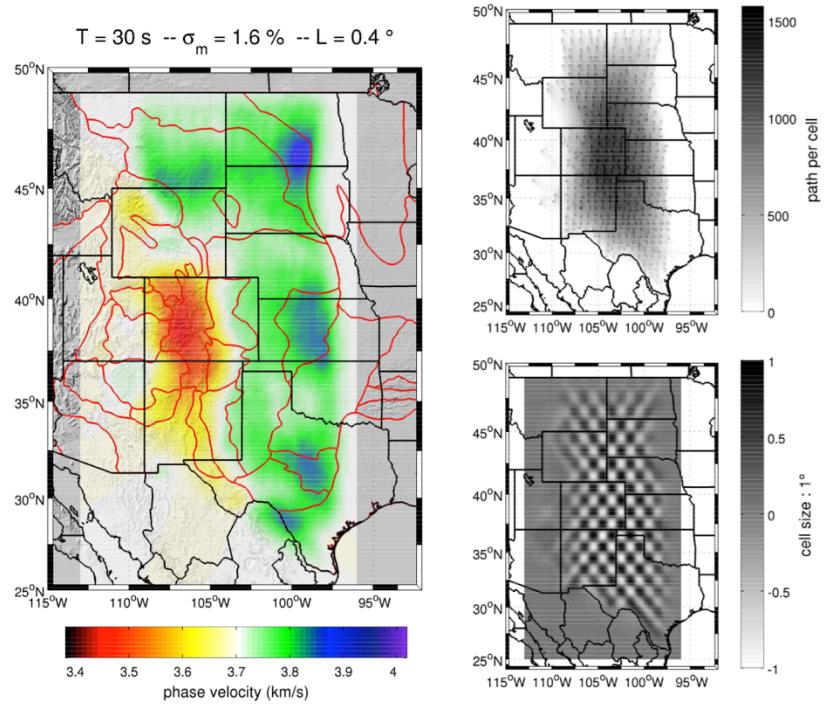
For surface waves: distant sources of noise at the surface of the sphere (2D problem)

Surfave wave reconstruction within a large array

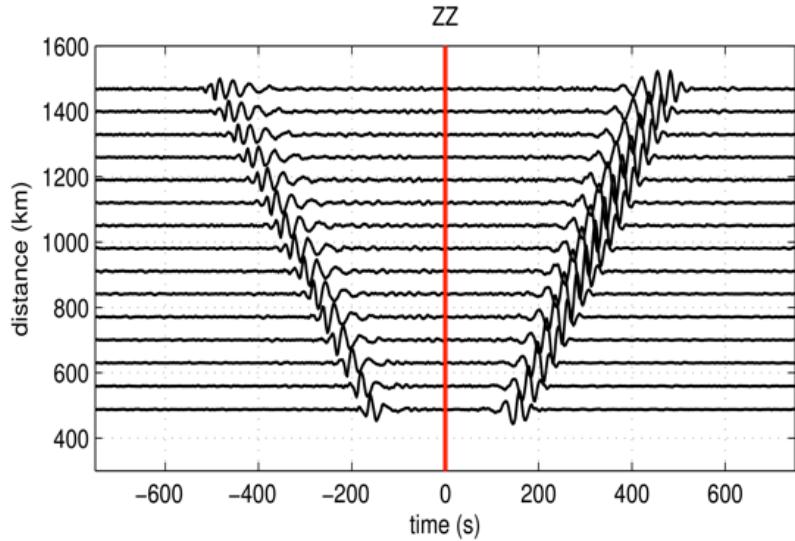
(Boué et al. 2014)



Weber et al., 1996



Noise correlation= $GF(t)-GF(-t)$
(Rayleigh waves)



Several hundreds of applications in the last 10 years!

An issue for surface wave tomography:

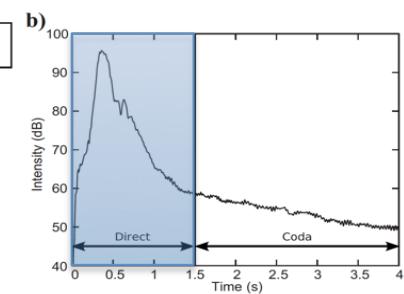
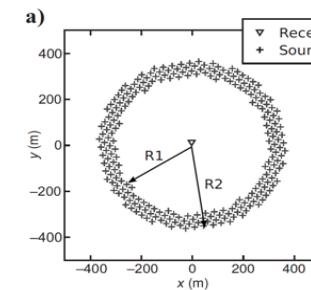
In practice, the noise sources are not evenly distributed and the field is not made fully isotropic by scattering.

We can study the effect of non isotropy of the intensity of the field incident on the receivers.

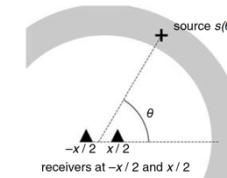
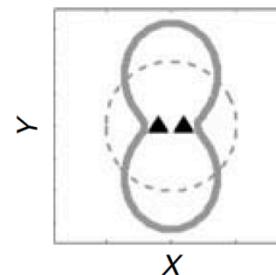
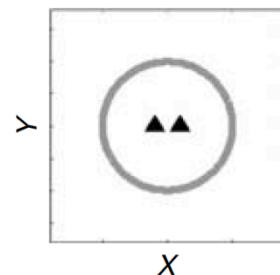
It results in a bias on the measurements of direct path travel times.

Correlation of direct waves:

Bias in the travel time

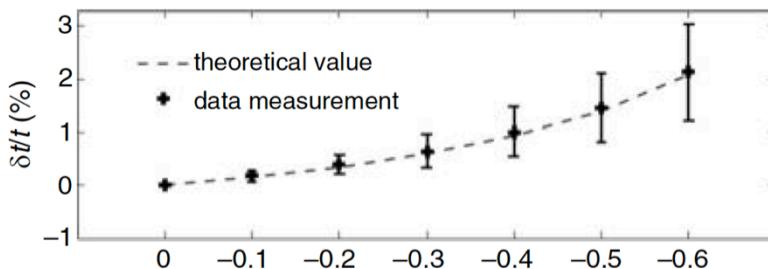


Increasing anisotropy of the source intensity B



$$B(\theta) = 1 + B_2 \cos(2\theta)$$

Azimuthal distribution of source intensity

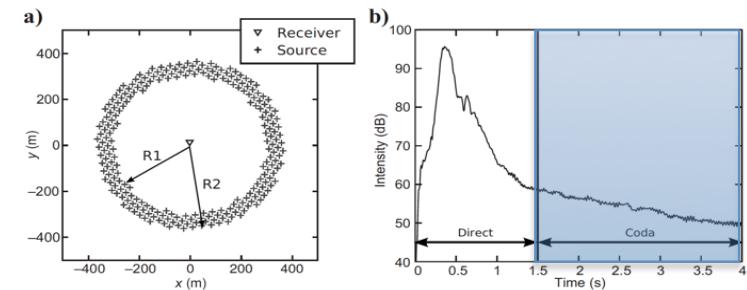
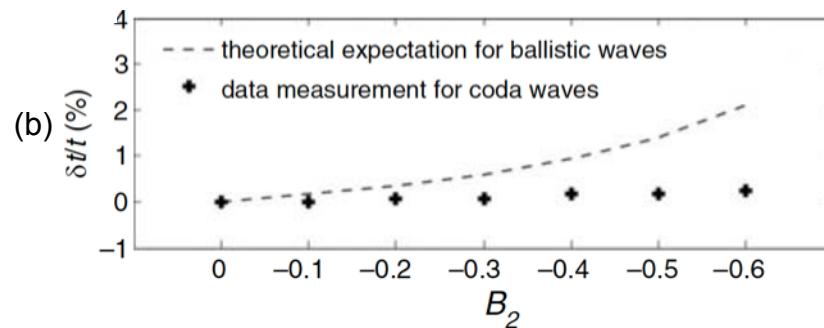
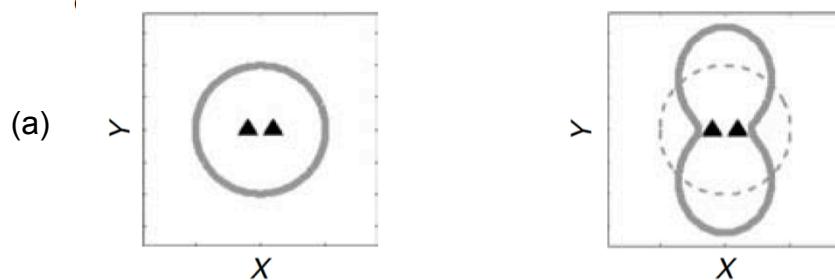


$$\delta t = \frac{1}{2t\omega_0^2 B(0)} \left. \frac{d^2 B(\theta)}{d\theta^2} \right|_{\theta=0}$$

valid with t (travel time) > T (period)

In presence of scattering:
Correlation of coda waves
-isotropy provided by multiple scattering

Increasing anisotropy of the source intensity B



$$B(\theta) = 1 + B_2 \cos(2\theta)$$

No bias in the correlation of coda waves!

An argument independant of the representation theorems
 Multiple scattering and equipartition: the simplest case (finite body)

equipartition

$$\phi(\vec{r}; t) = \sum_n a_n U_n(\vec{r}) \cos(\omega_n t)$$

$$\langle a_n a_m^* \rangle = F(\omega_n) \delta_{nm}$$

correlation

$$C_{1,2}(t) = \frac{1}{T} \int_0^T \phi(\vec{r}_1, \tau) \phi(\vec{r}_2, t + \tau) d\tau$$

Assuming a long recording interval T , this reduces to:

Compare with:

$$C_{1,2}(t) = \frac{1}{2} \sum_n F(\omega_n) U_n(\vec{r}_1) U_n(\vec{r}_2) \cos(\omega_n t)$$

$$G(\vec{r}_1, \vec{r}_2; t) = \sum_n U_n(\vec{r}_1) U_n(\vec{r}_2) \frac{\sin(\omega_n t)}{\omega_n} \Theta(t)$$

1 derivative 2 causality

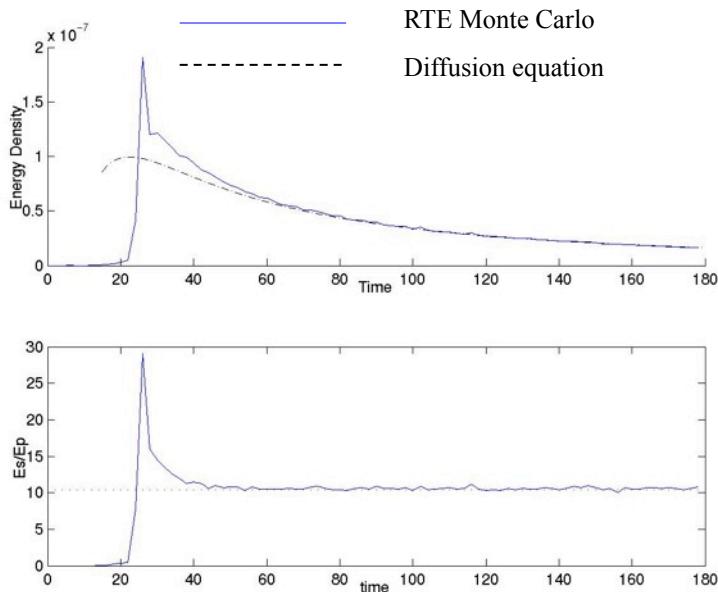
→ Long range correlation in seismic coda= Green function (Campillo and Paul, Science 2003)

Multiple scattering and equipartition

Equipartition principle for a completely randomized (diffuse) wave-field: in average, all the modes of propagation are excited to equal energy.

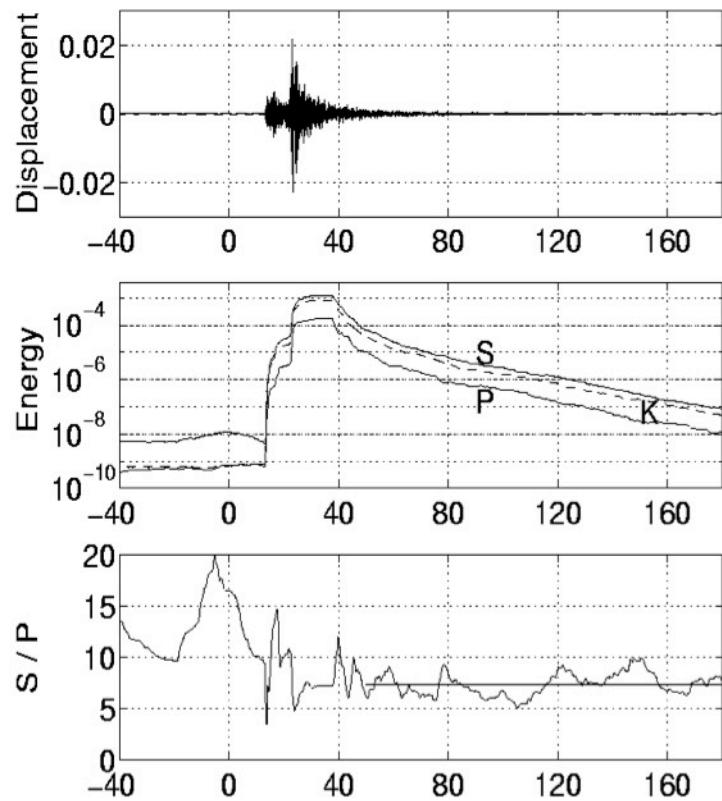
Implication for diffuse elastic waves (*Weaver, 1982, Ryzhik et al., 1996*): P to S energy ratio stabilizes at a value independant of the details of scattering.

Numerical simulation (*Margerin et al. 2000*)



Observations (*Hennino et al., 2001*)

Event 11

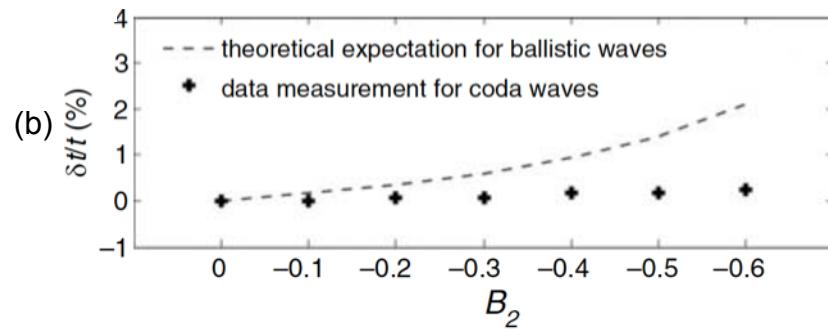
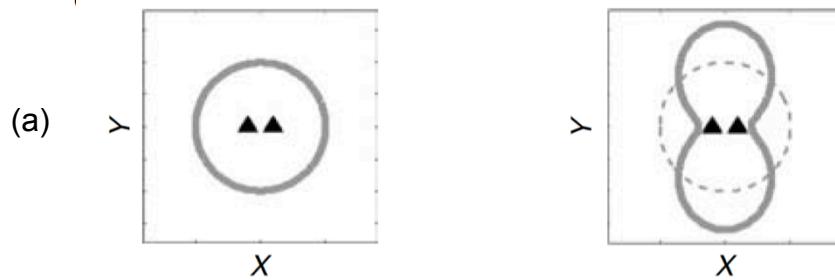
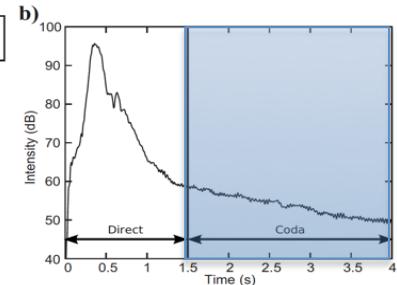
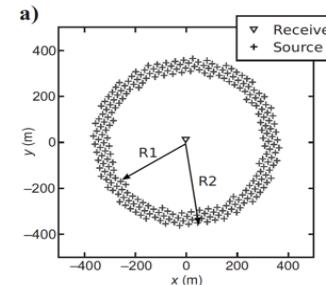


In presence of scattering:

Correlation of coda waves

-isotropy provided by multiple scattering

Increasing anisotropy of the source intensity B



$$B(\theta) = 1 + B_2 \cos(2\theta)$$

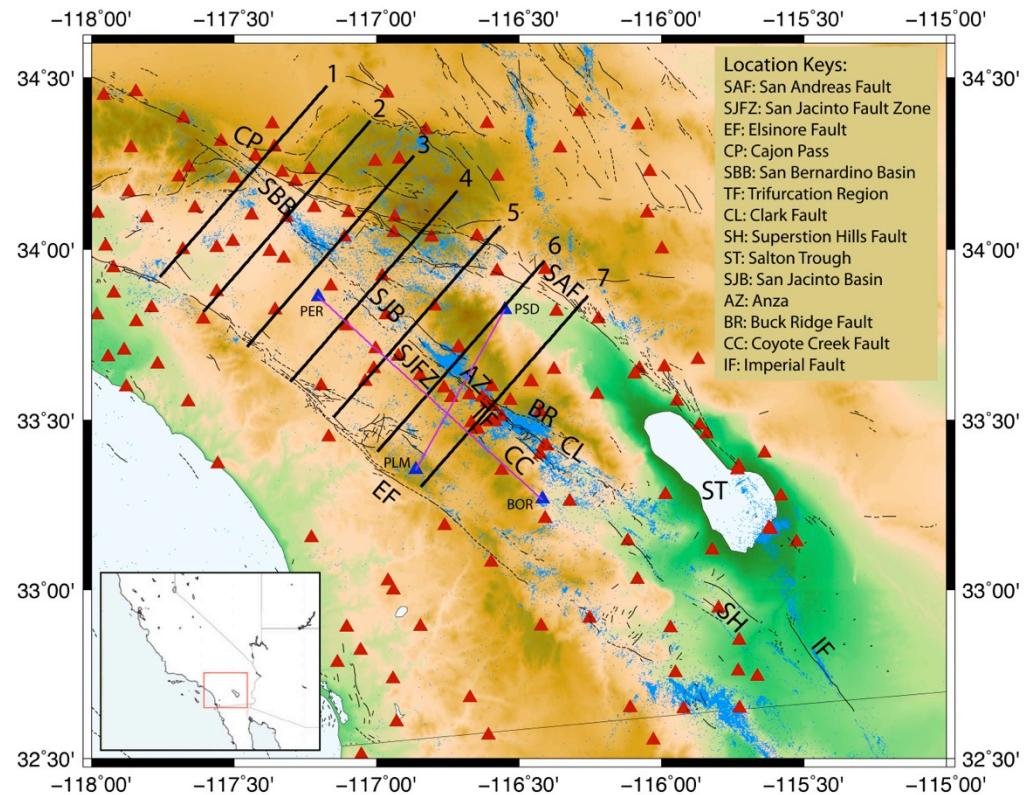
No bias in the correlation of coda waves!

Noise records contain direct and scattered waves:

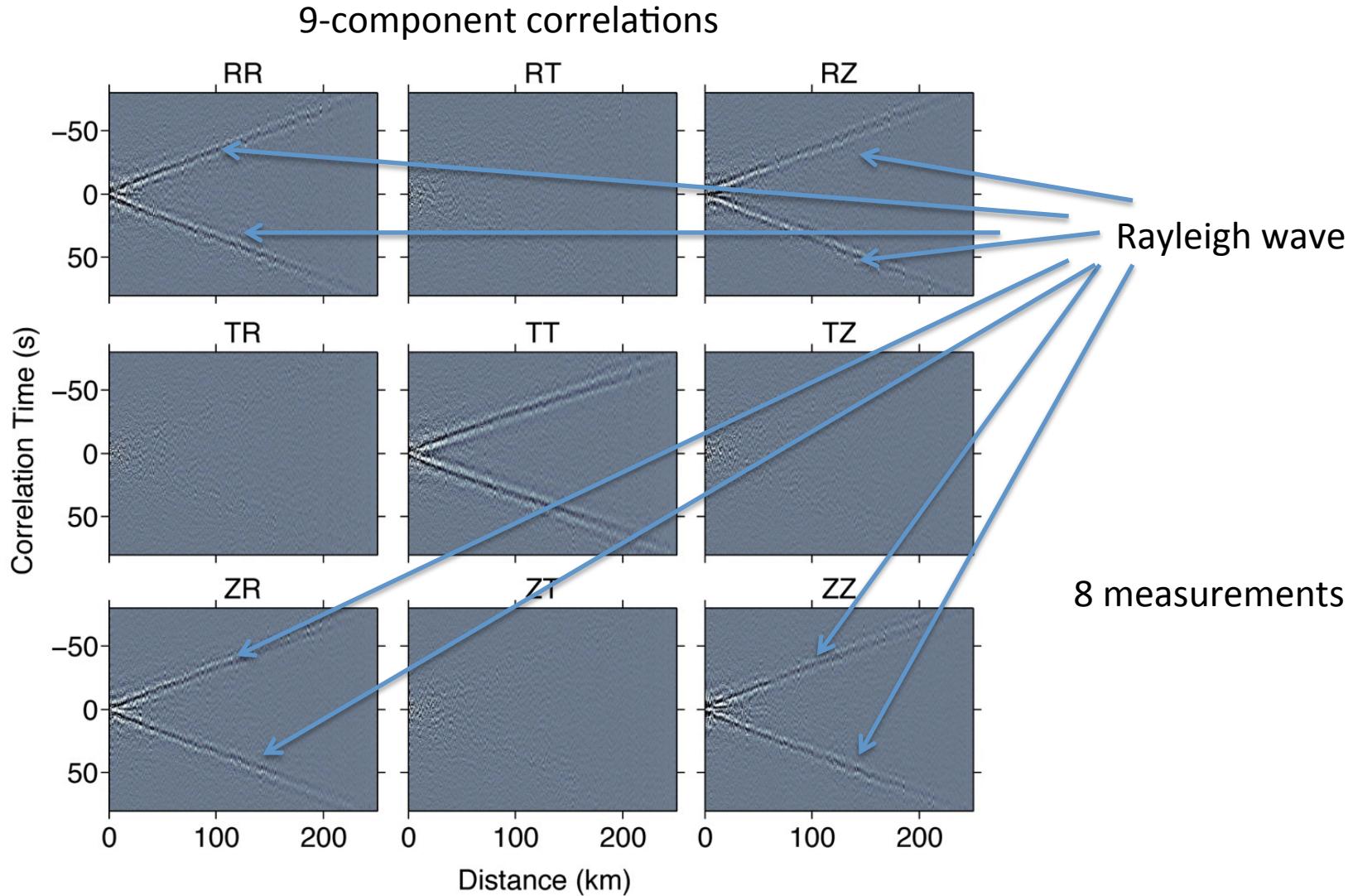
→ the biases of direct wave travel times are generally small enough for imaging purpose
→ Importance of processing strategies

Fault zone structures imaging

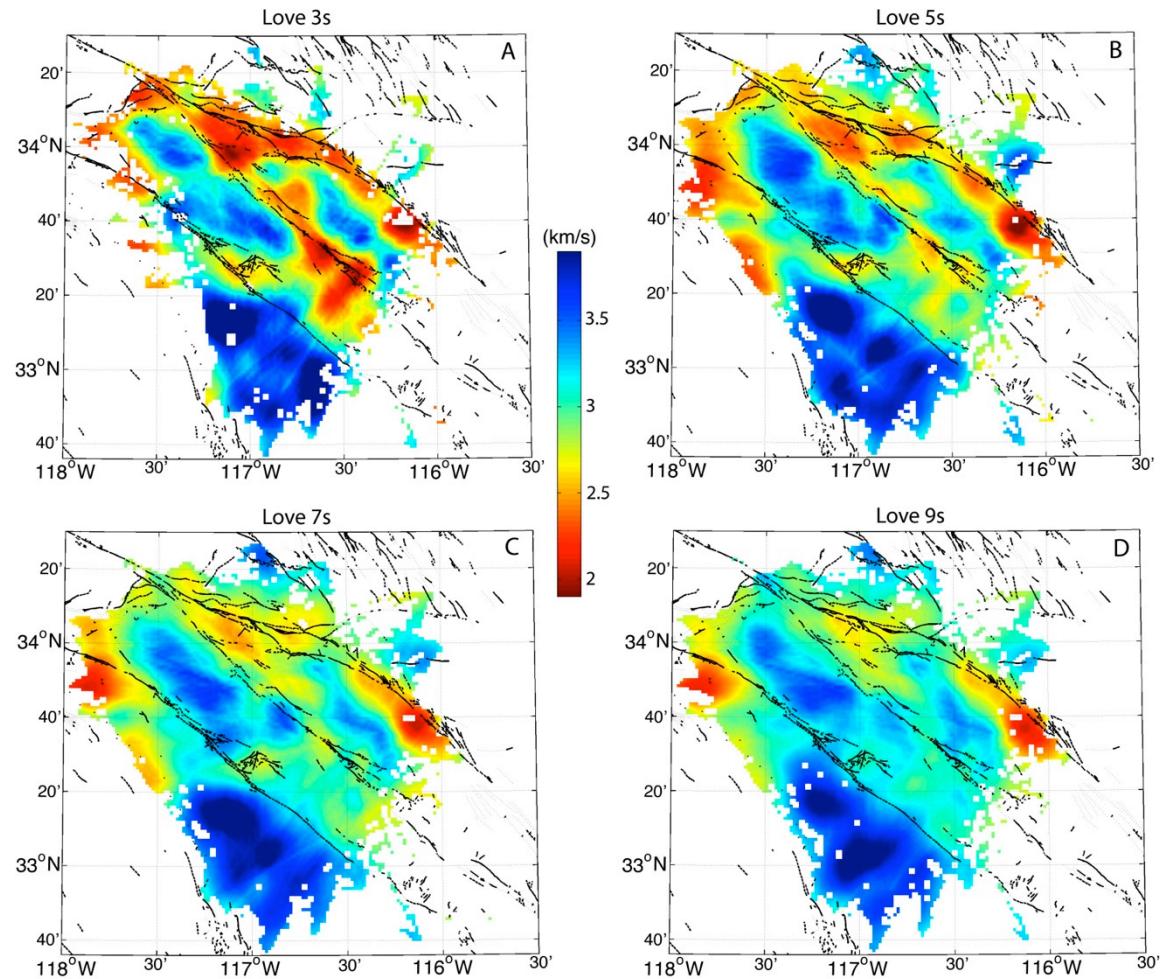
- fault segments, complexity (rupture speed)
 - bi-material interfaces: preferential direction of rupture propagation
 - amplification effects
- lack of resolution for shear wave in the first kilometers for traditional tomography



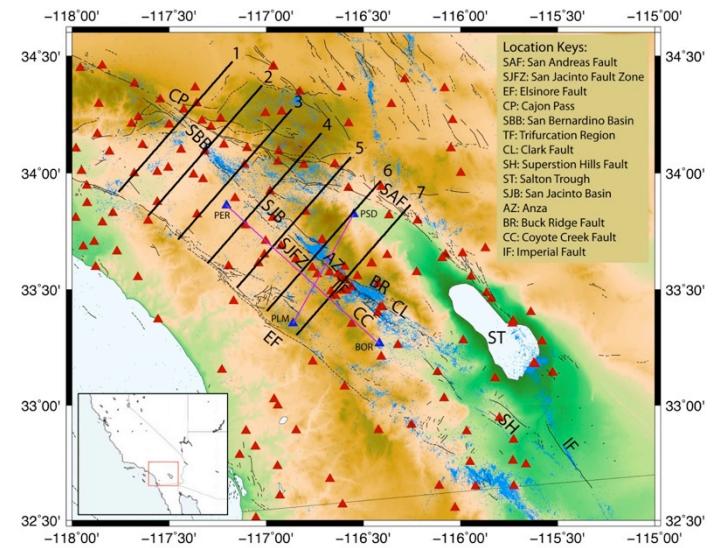
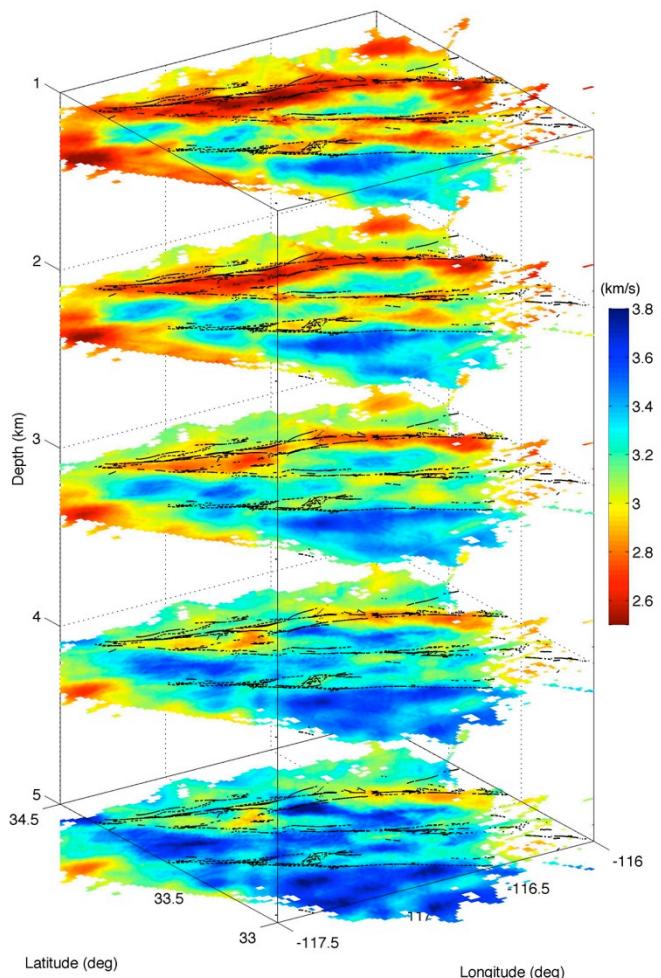
Surface wave tomography with noise correlation



Group velocity maps at different periods



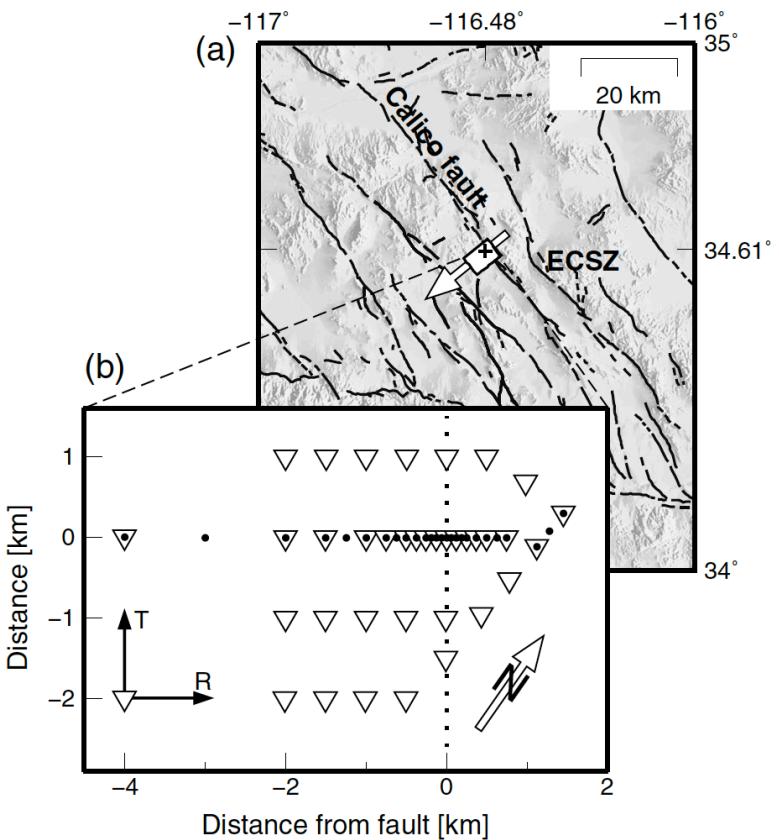
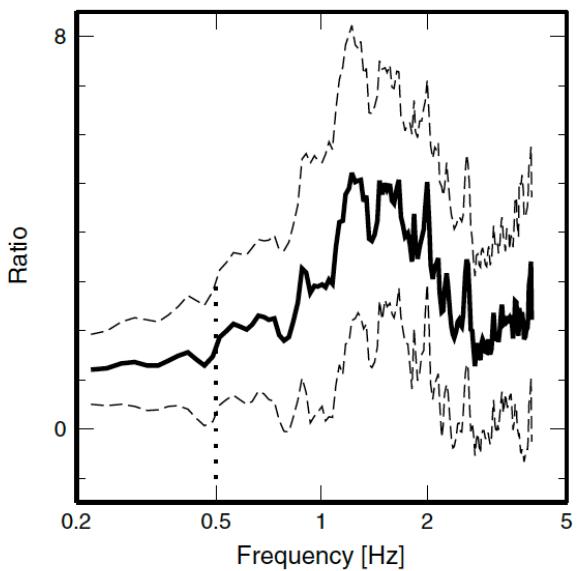
3D shear velocity

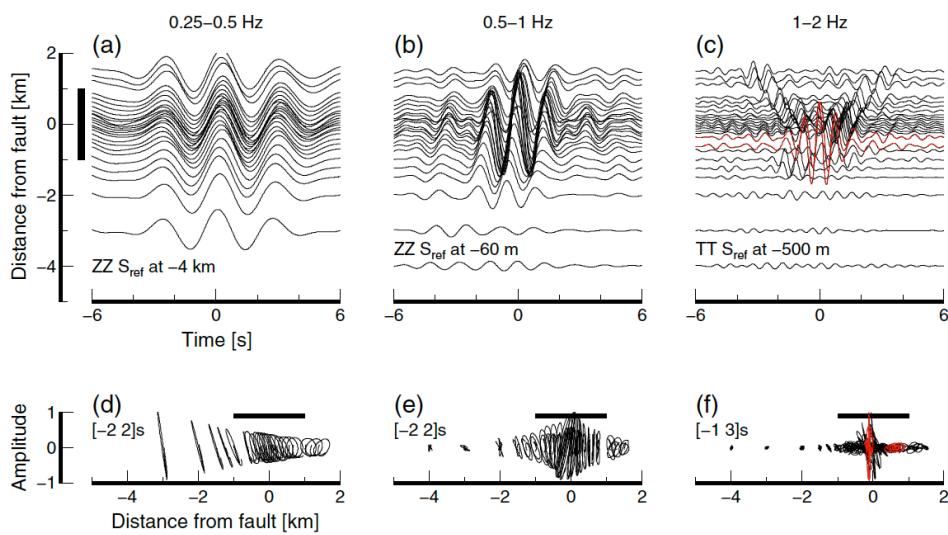


- Damaged fault zone
- Flower-like patterns
- Diffuse seismicity associated with low-velocity (damaged) area between SAF and SJFZ

Seismic fault zone trapped noise

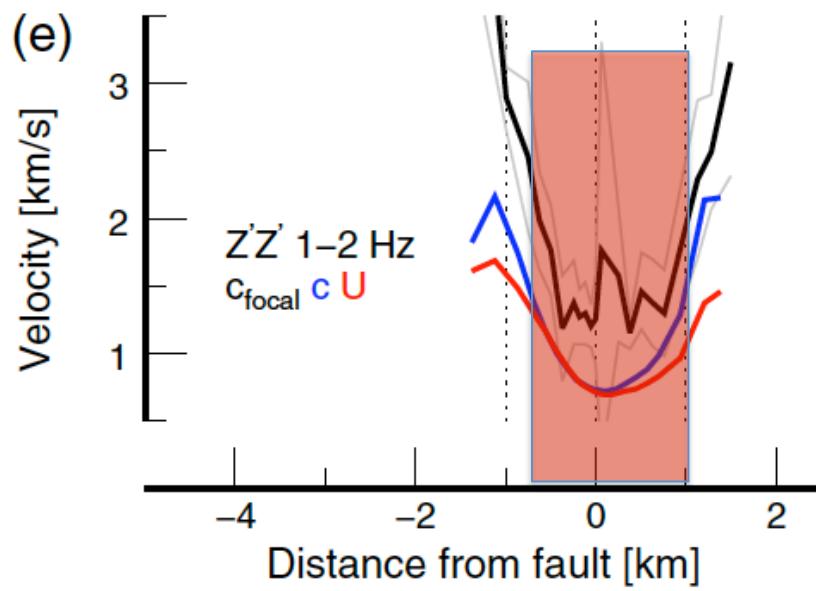
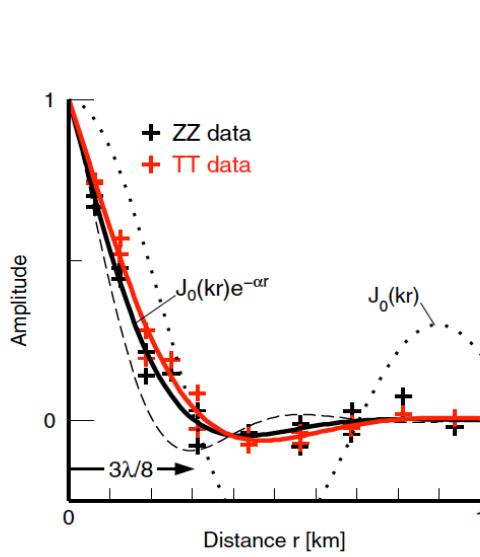
Spectral ratio between ZZ CC for pairs in fault and outside





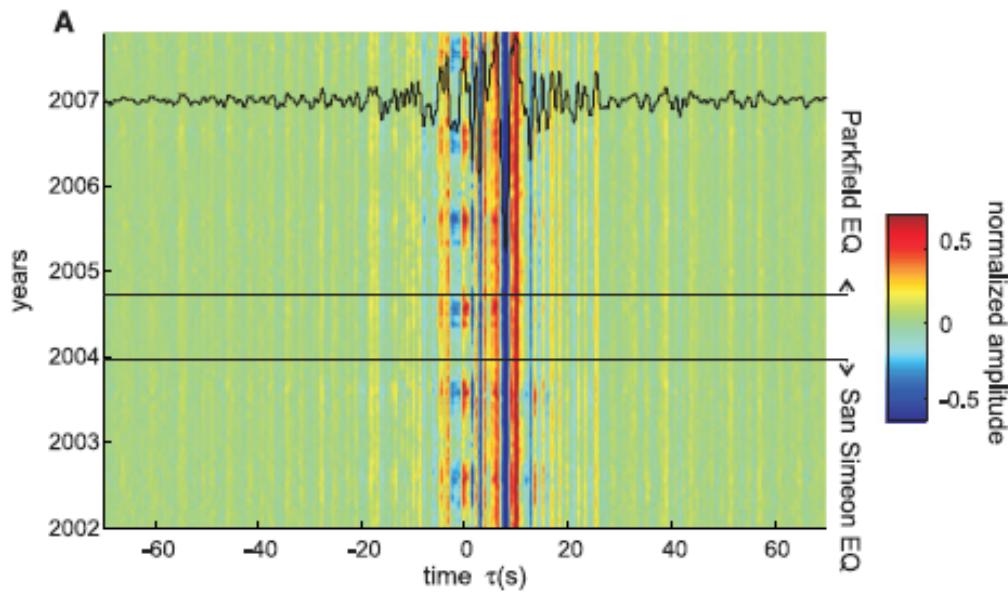
Focusing

Using the width of the focal spot: a technique developed in medical imaging (elastography)



Perspectives: imaging and monitoring

Correlation functions as approximate Green functions

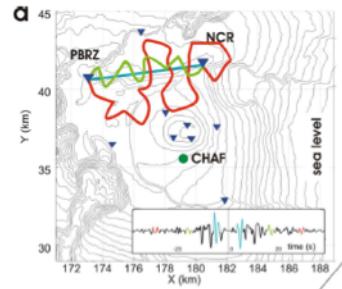
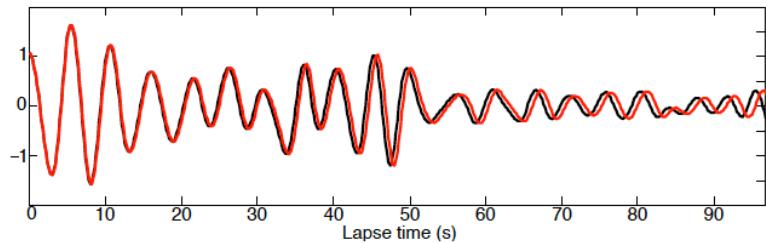


Direct waves are sensitive to noise source distribution (errors small enough for tomography ($\leq 1\%$) but too large for monitoring (goal $\approx 10^{-4}$)

Stability of the ‘coda’ of the noise correlations ?

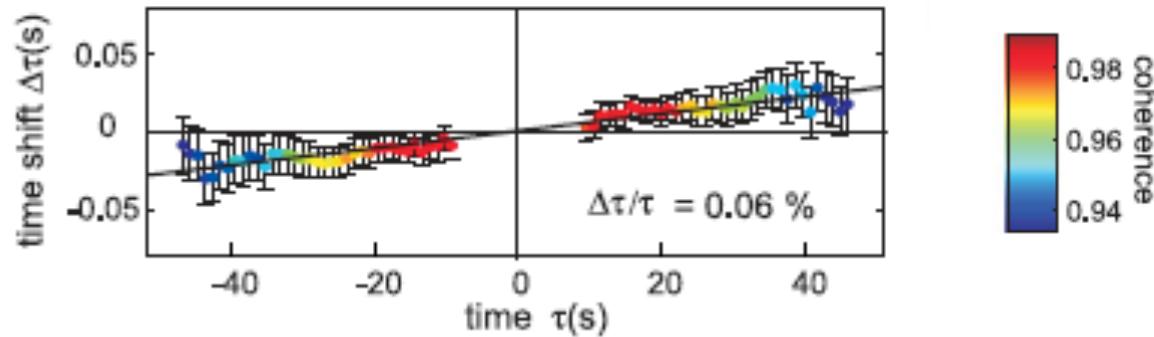
Detecting a small change of seismic speed with coda waves

Comparing a trace with a reference under the assumption of an homogeneous change



The ‘doublet’ method: moving window cross spectral analysis (phase measurements)

(Poupinet, Ellsworth, Fréchet, 1984)

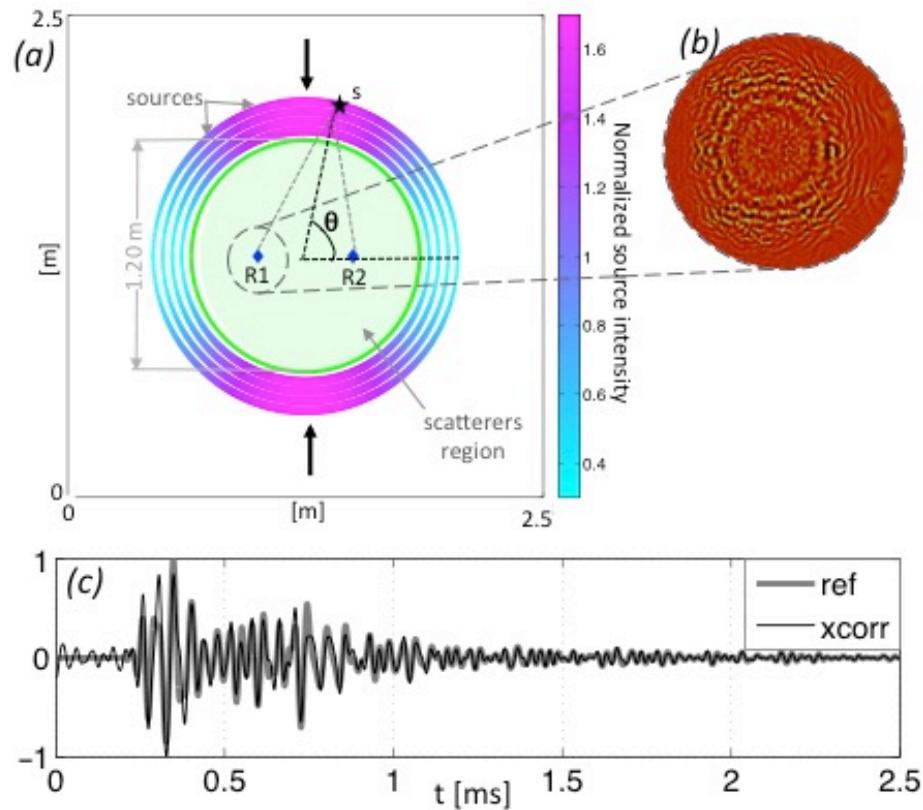


Alternative technique: stretching

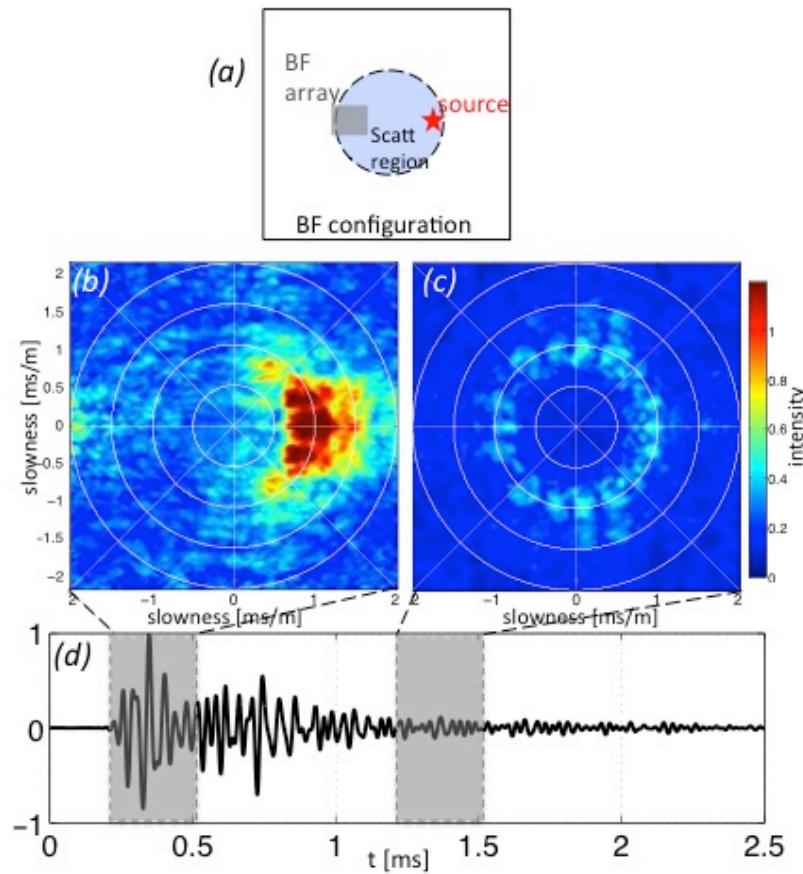
Sensitivity of coda waves in cross-correlations to changes of the noise sources

Specific to passive imaging and monitoring

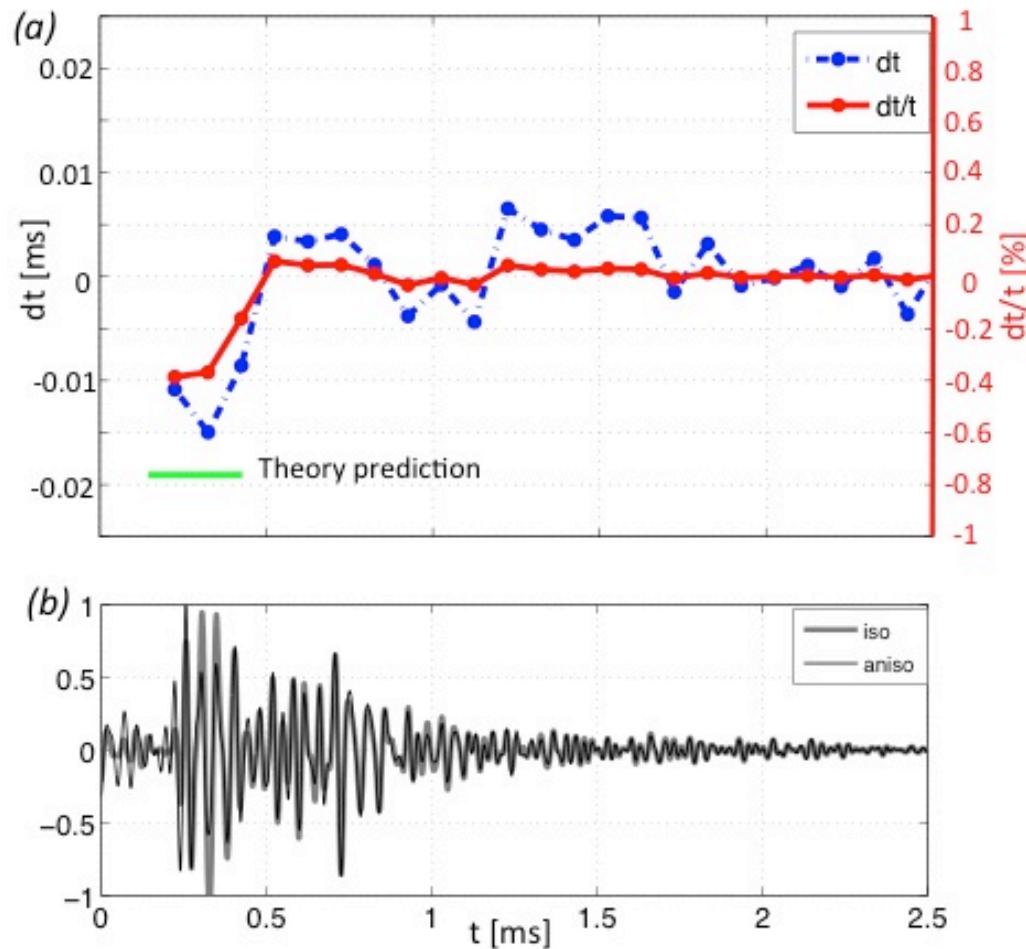
Numerical simulations in a scattering medium



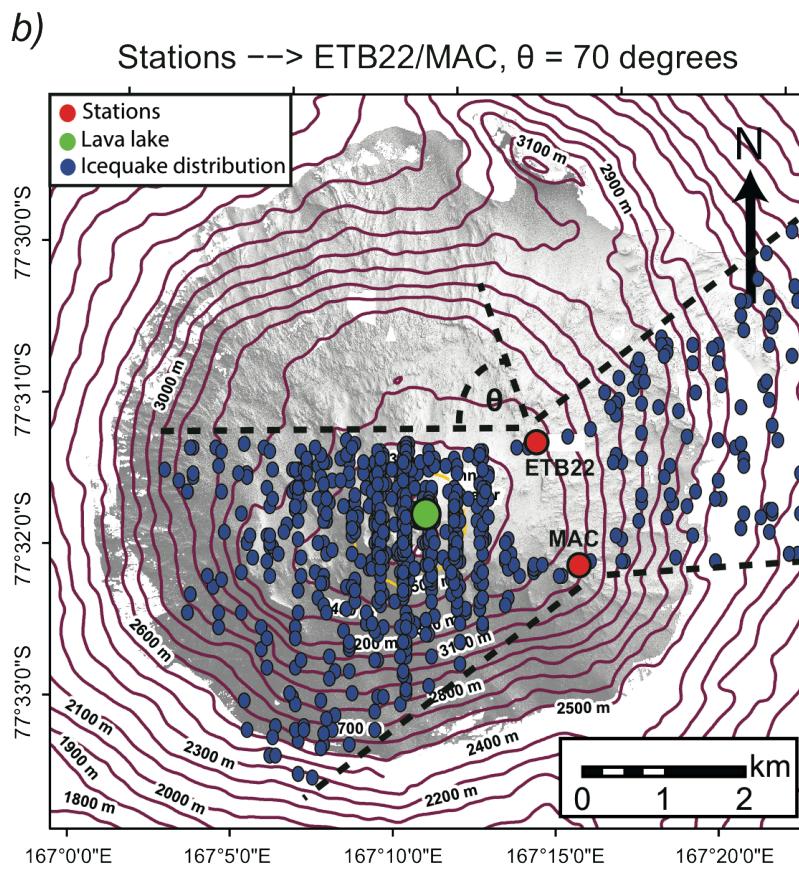
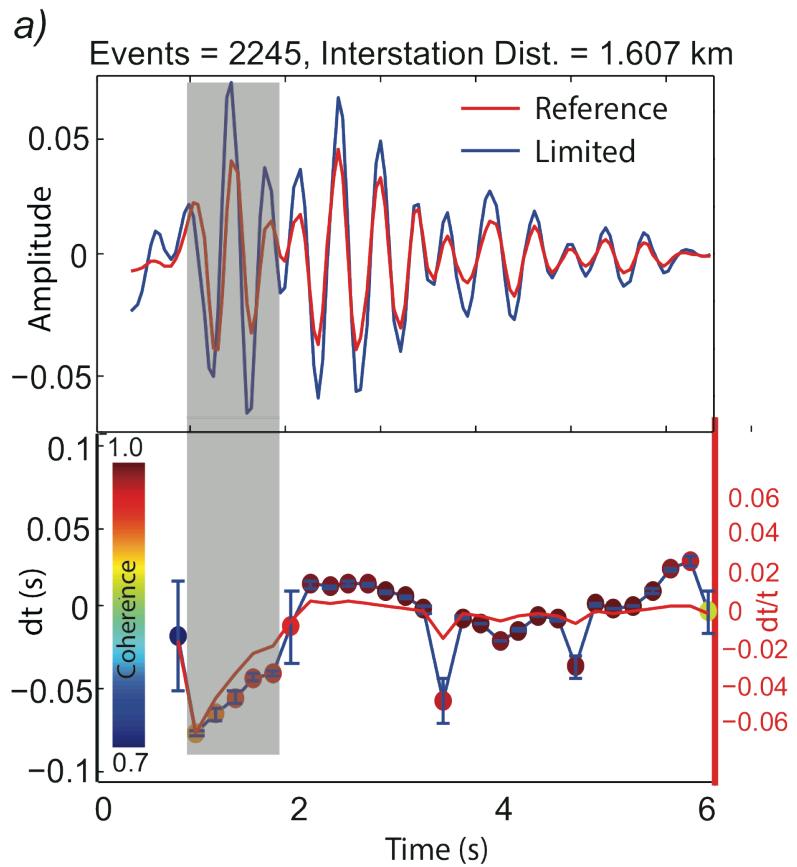
Effect of scattering single source



Measure of the bias induced by a strong anisotropy of the wave field

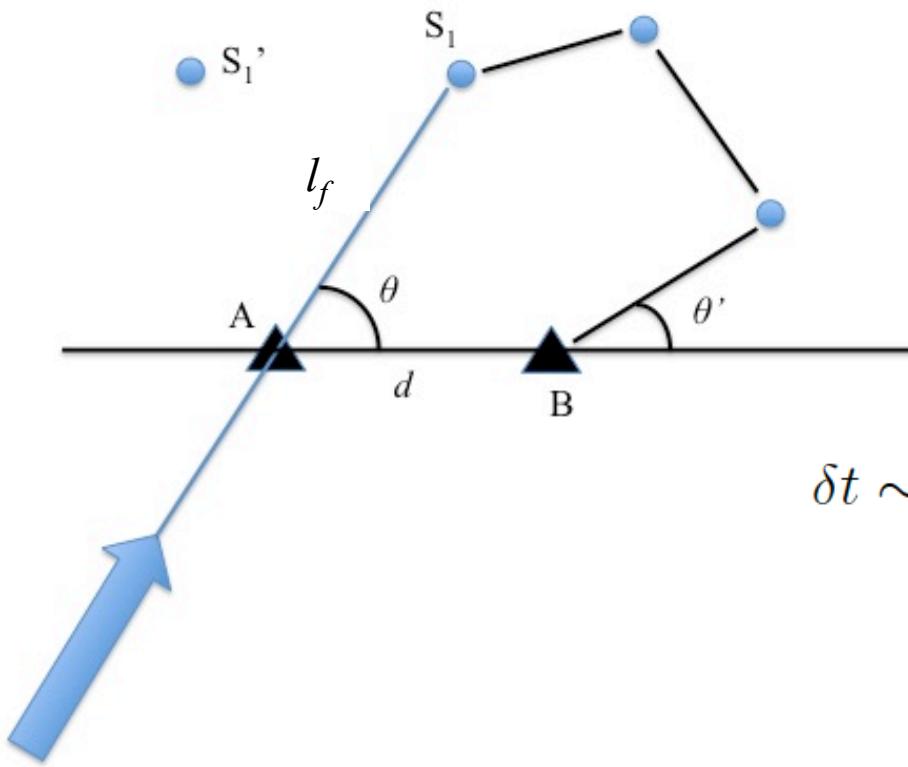


Real data: icequakes from Mount Erebus



Representation of coda waves as the sum of contributions of numerous paths

For a single path:



$$\delta t \sim \frac{B''(\theta)}{2 t_f \omega_0^2 B(\theta)}$$

We have to compute the contributions of paths with first scatterers at all distances l_f and all azimuths θ

The distribution of distance between scattering events is exponential:

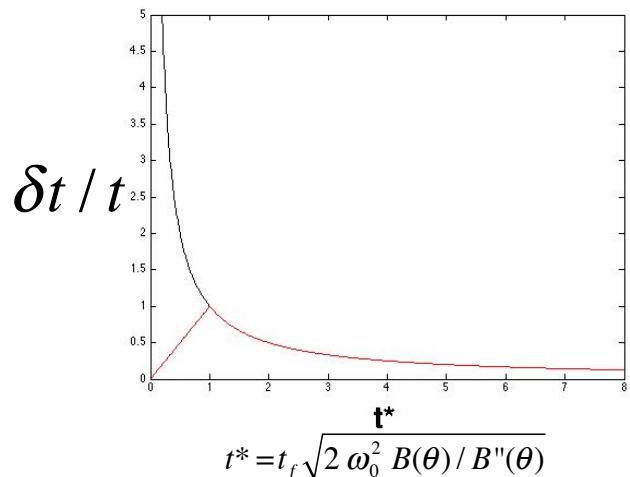
$$P(l_f) = \frac{1}{l} e^{-\frac{l_f}{l}} \quad \text{where } l \text{ is the mean free path}$$

$$\langle l_f \rangle = l \quad t_f = l_f / V$$

$$\delta t \sim \frac{B''(\theta)}{2 t_f \omega_0^2 B(\theta)}$$

valid for $l_f > \lambda$

We remove the singularity for l_f to 0 in a conservative way.



$$R = \frac{\langle \delta t \rangle_{max}}{\delta t|_{t_l}}$$

ratio of max average δt over
 δt of the average l_f ($=l$ the mfp)

Finally we consider all directions:

$$\langle \delta t \rangle = \frac{R}{2\pi} \int_0^{2\pi} \delta t(\theta) d\theta = \frac{R}{4\pi t_l \omega_0^2} \int_0^{2\pi} \frac{B''(\theta)}{B(\theta)} d\theta$$

Applications

Numerical simulations

$$l = 0.5m, c = 2000\text{m/s},$$

$$f_0 = 30000\text{Hz}, B_2 = -0.6 \text{ and } \tau_m = 0.002\text{s}$$

→ fractional error $\frac{\delta t(\tau_m)}{\tau_m}$ of 10^{-4} .

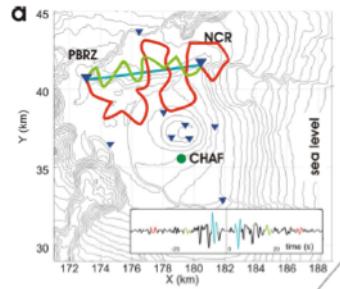
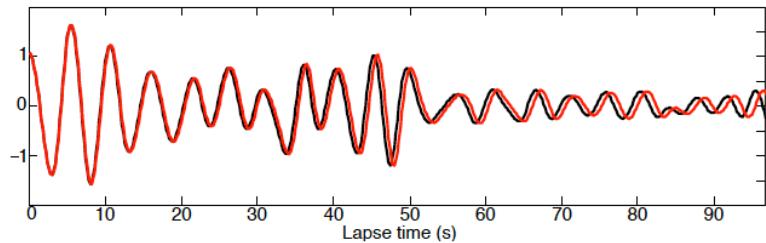
Japan (same change of anisotropy)

$$l = 60 \cdot 10^3 m, C = 3000\text{m/s}, f_0 = 0.3\text{Hz} \text{ and } \tau_m = 100\text{s}$$

→ fractional error of $2 \cdot 10^{-4}$.

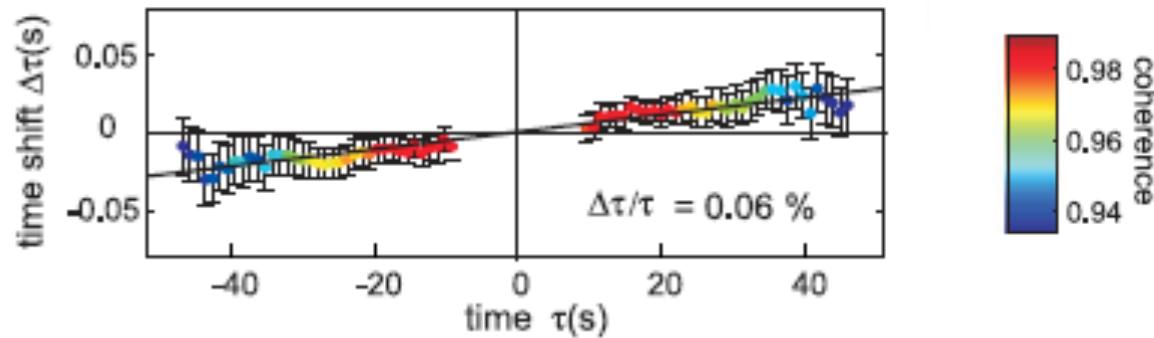
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Comparing a trace with a reference under the assumption of an homogeneous change



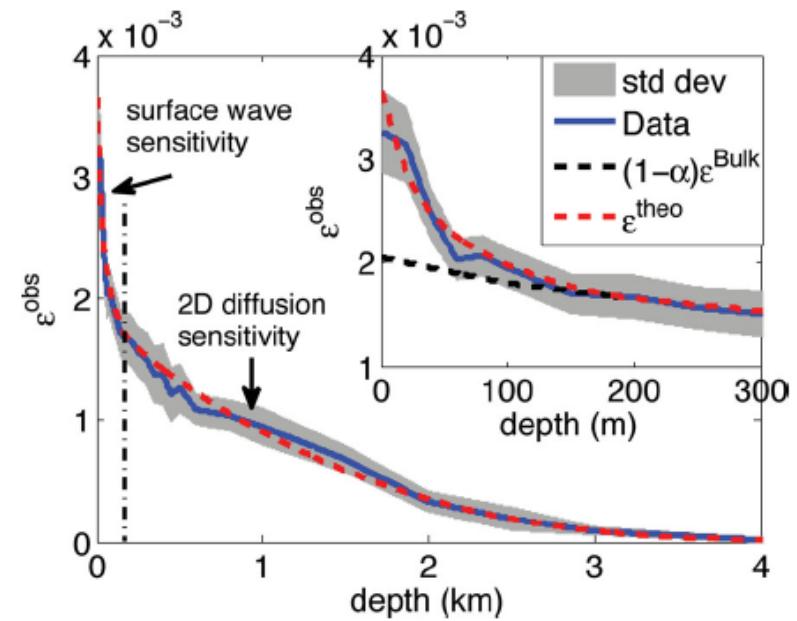
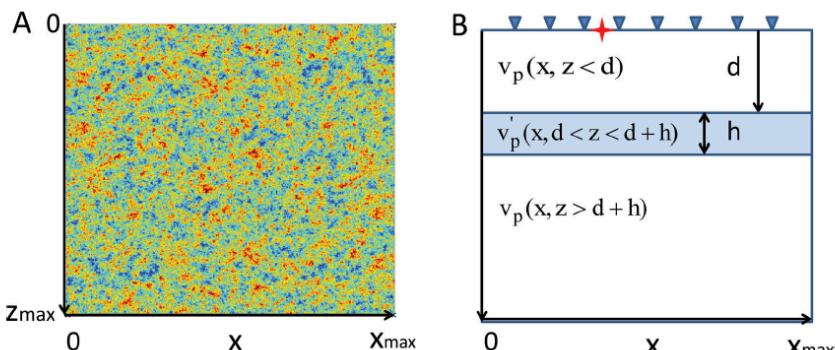
The ‘doublet’ method: moving window cross spectral analysis (phase measurements)

(Poupinet, Ellsworth, Fréchet, 1984)



Alternative technique: stretching

Sensitivity of coda to a change in the medium 1: wave type and depth sensitivity



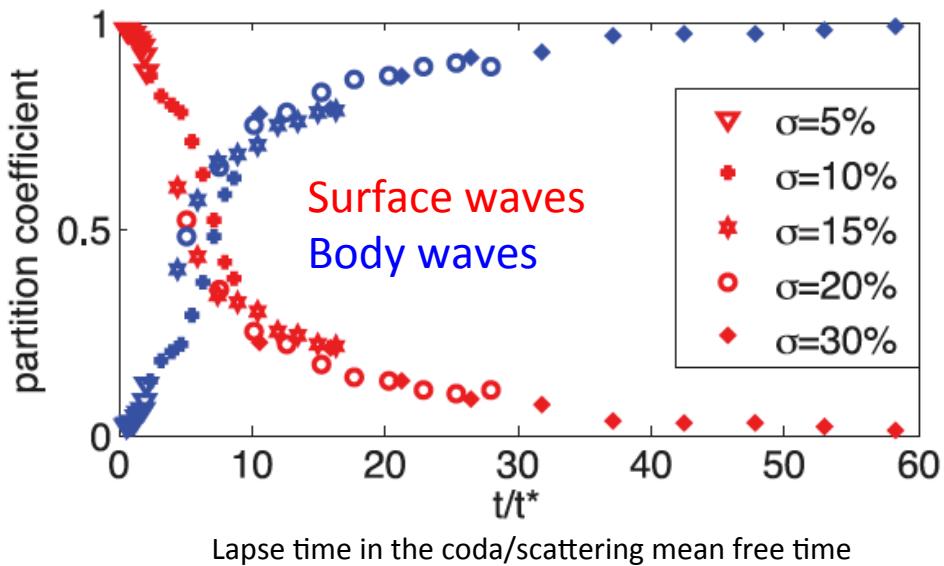
$$\varepsilon^{\text{theo}}(d, t) = \alpha(t)\varepsilon^{\text{Surf}}(d) + (1 - \alpha(t))\varepsilon^{\text{Bulk}}(d, t)$$

Partition coefficient

Obermann et al., 2013a

Sensitivity of coda to a change in the medium 1: wave type and depth sensitivity

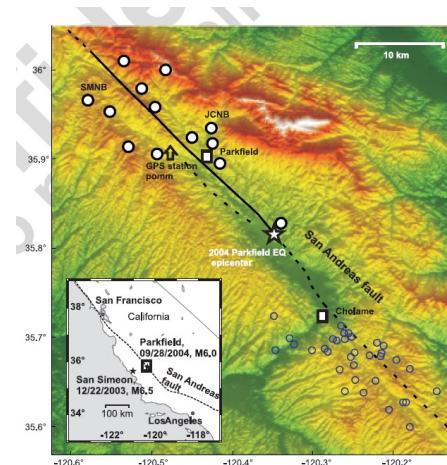
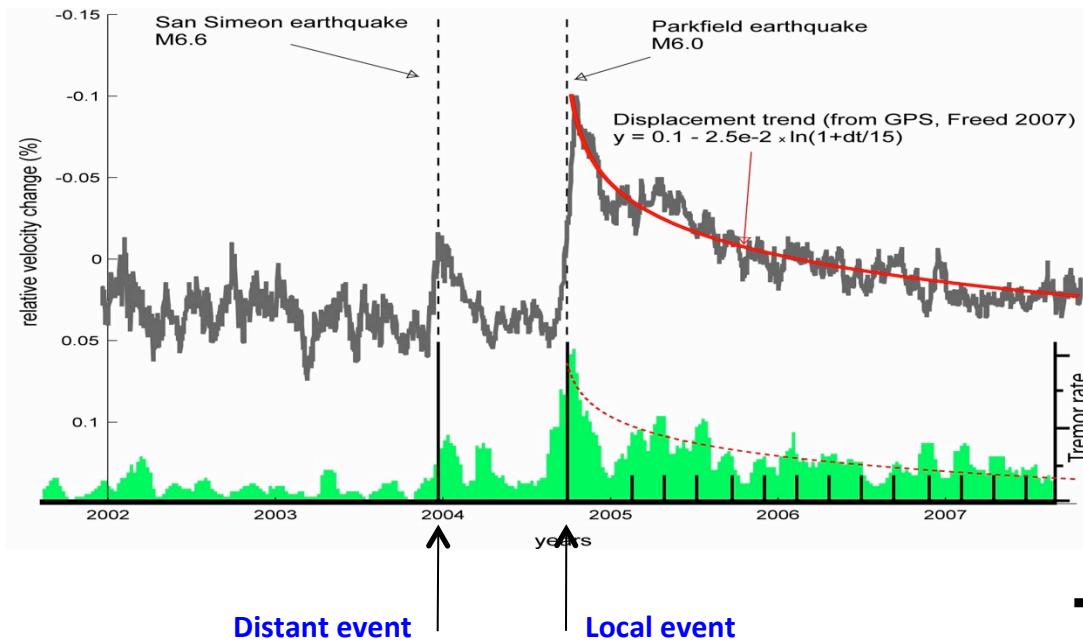
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Obermann et al., 2013a

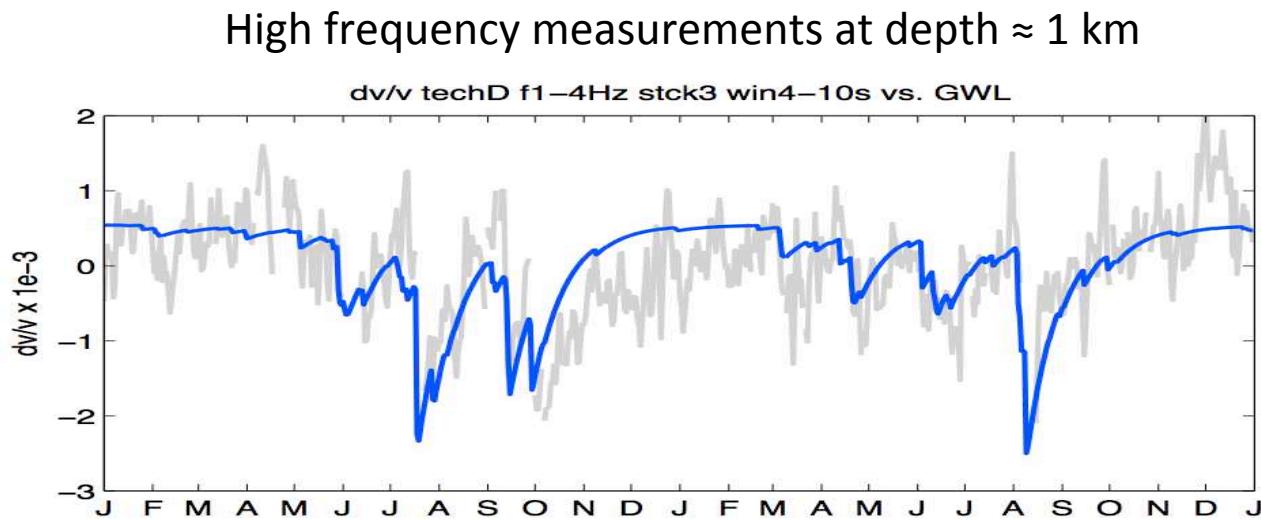
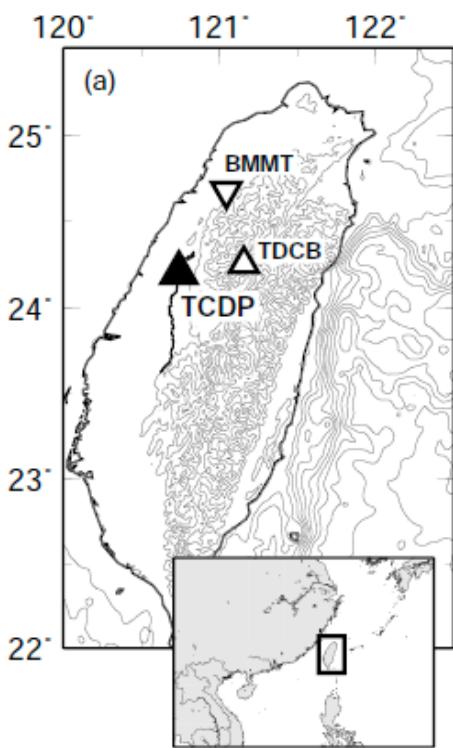
In the applications presented here, we analyze early coda (a few mean free times) so our measures concern mainly surface waves

Application to Parkfield (*Brenguier et al. 2008*) Short period sensors / Processing in the period 1-10s



- ➔ GPS trend
- ➔ tremor activity
- ➔ dynamic response of shallow layers

Evidence of hydro-meteorological effects



grey: variations of seismic speed

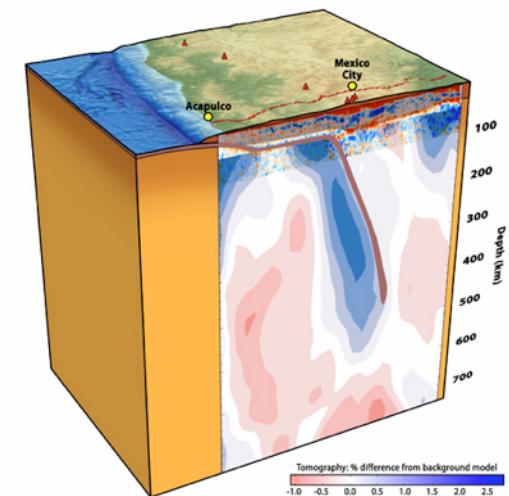
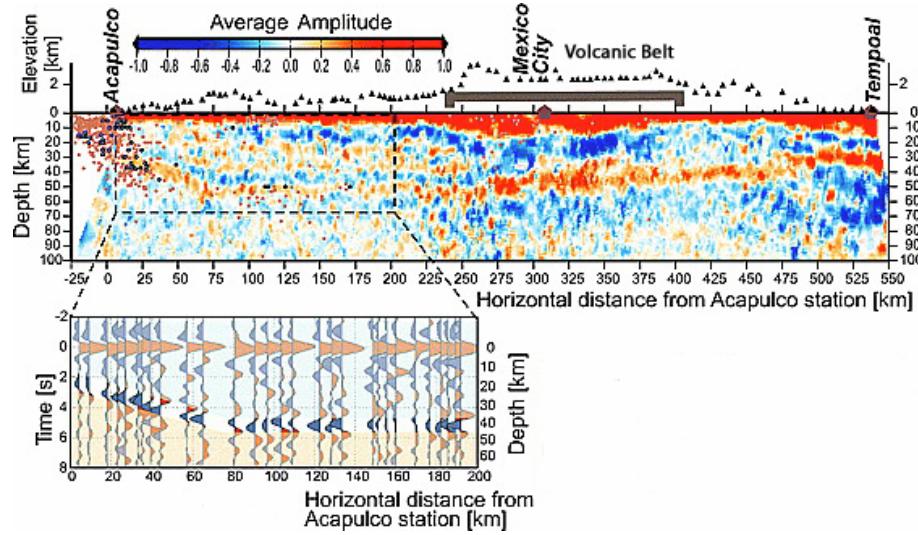
blue: model of the effect to the level of water table deduced from meteorological data

Slow slip events in Guerrero, Mexico

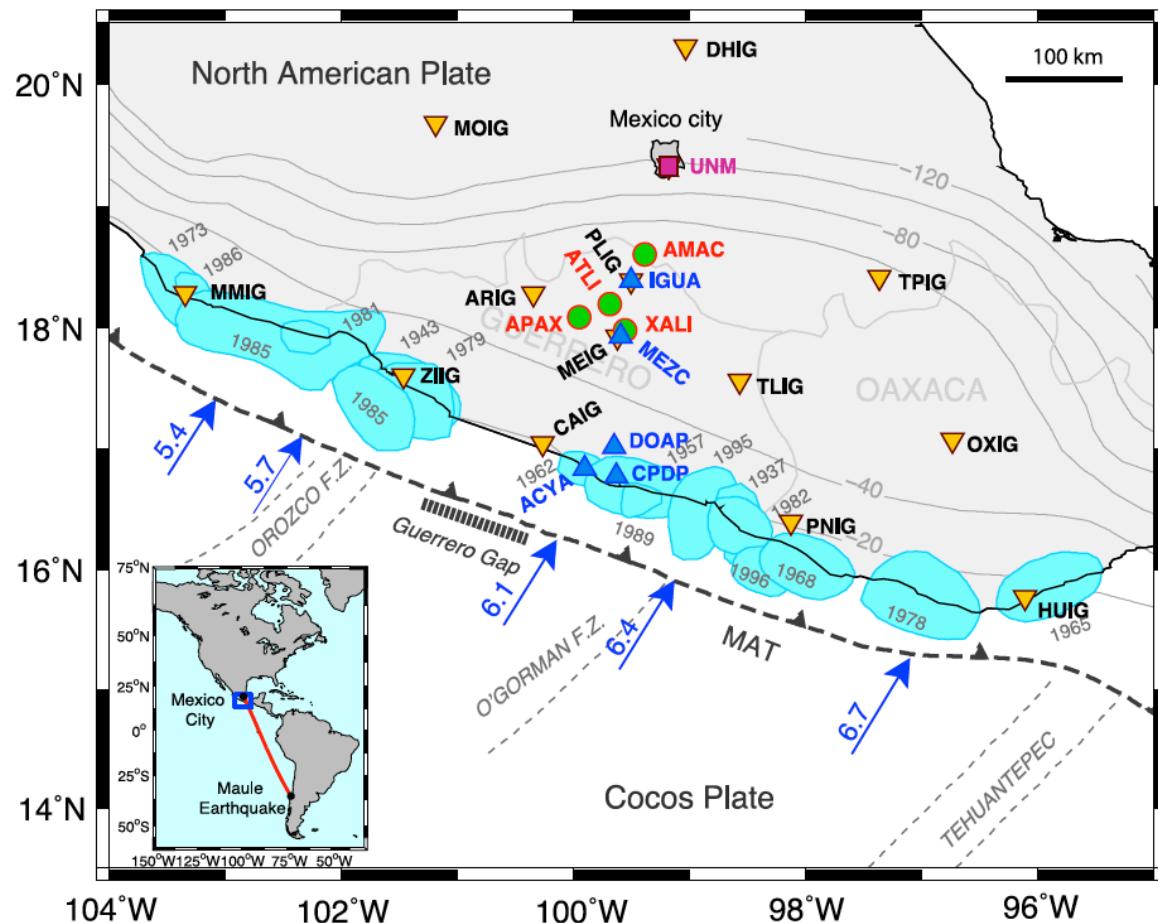


MASE project (US-Mexico)

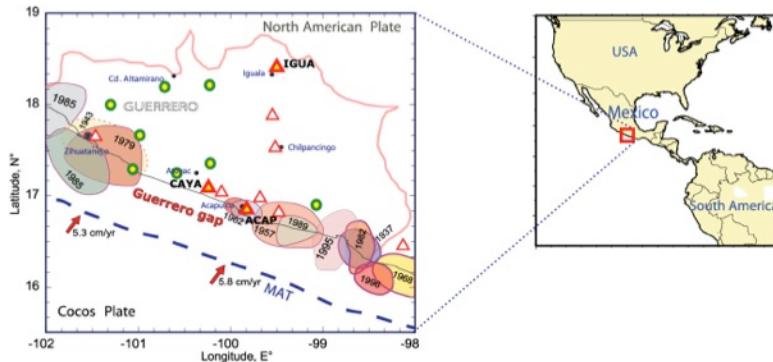
[Modified from Chen and Clayton, JGR 2009]



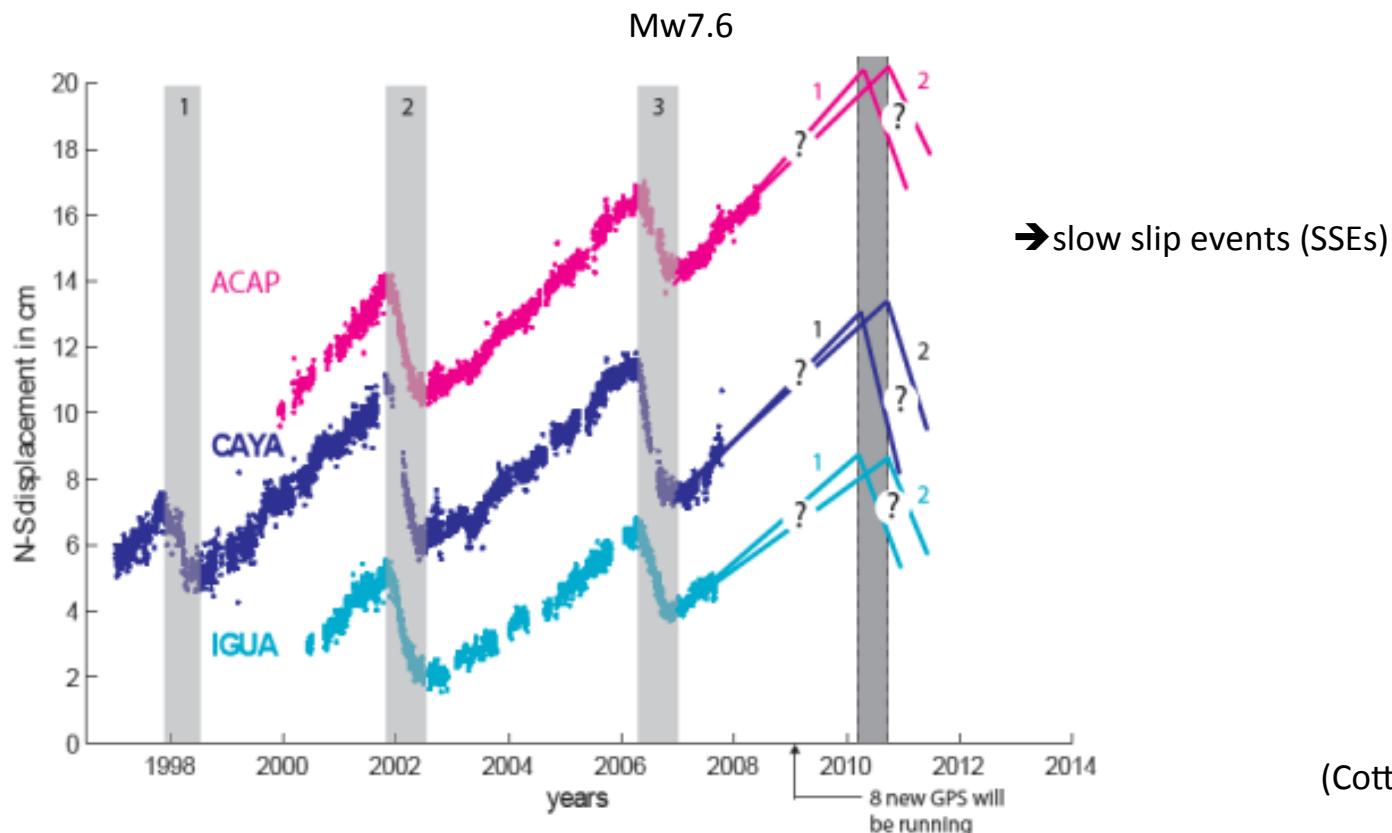
[From Perez-Campos et al., GRL 2008]



'Silent' event of slip on the Subduction plane (40km deep)

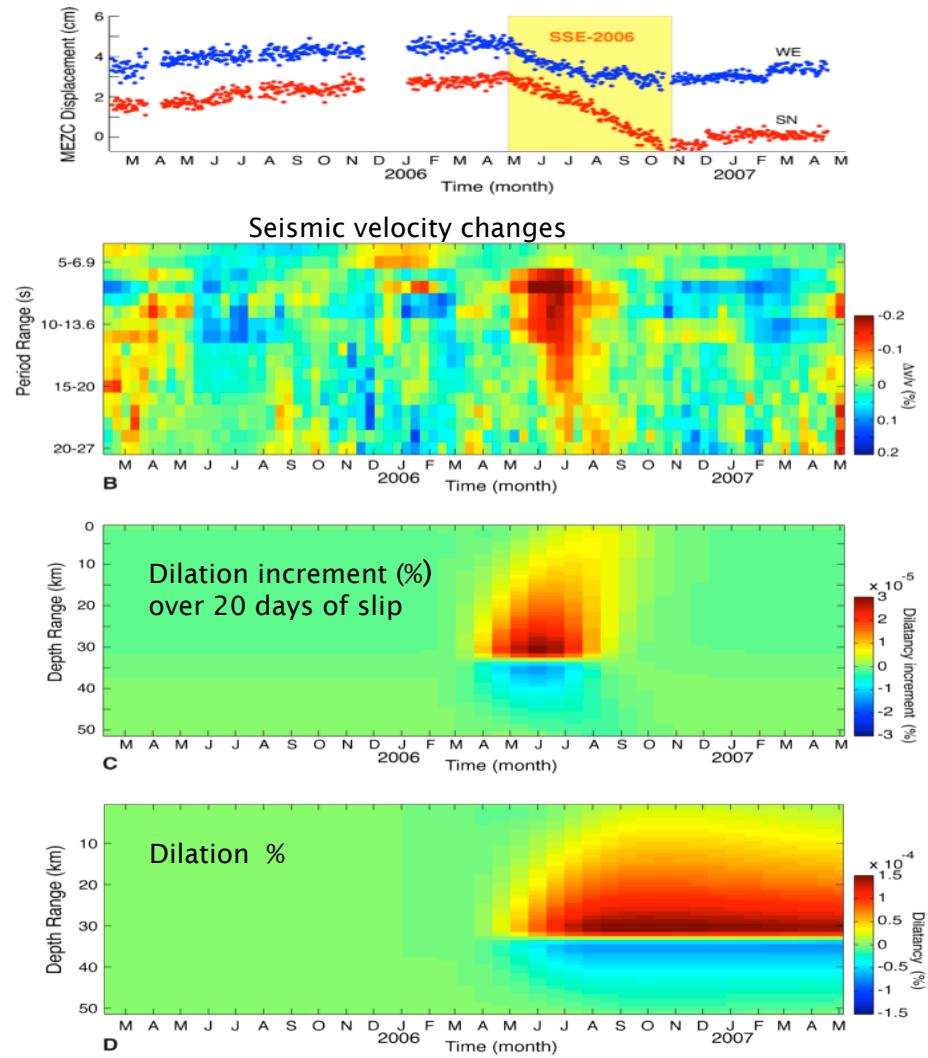
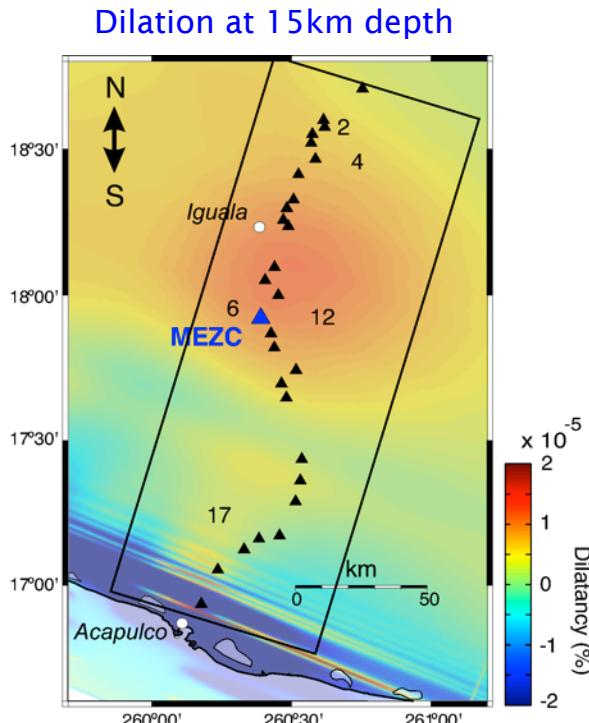


GPS motion towards the North during interseismic periods (NO significant events)



(Cotte et al., 2009)

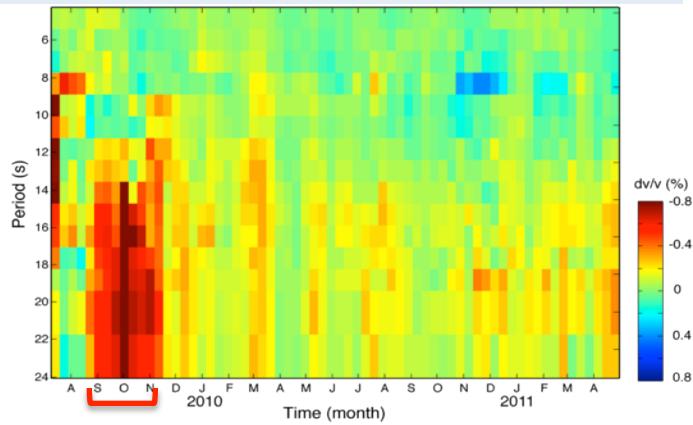
Temporal relation between velocity change and dilatation



Rivet et al., 2011:
Deep velocity drop
Depth sensitivity (Obermann et al.; 2013)

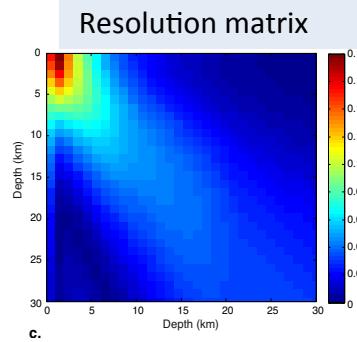
2009-2010 Slow Slip Event

Apparent temporal change of velocity (t, T)

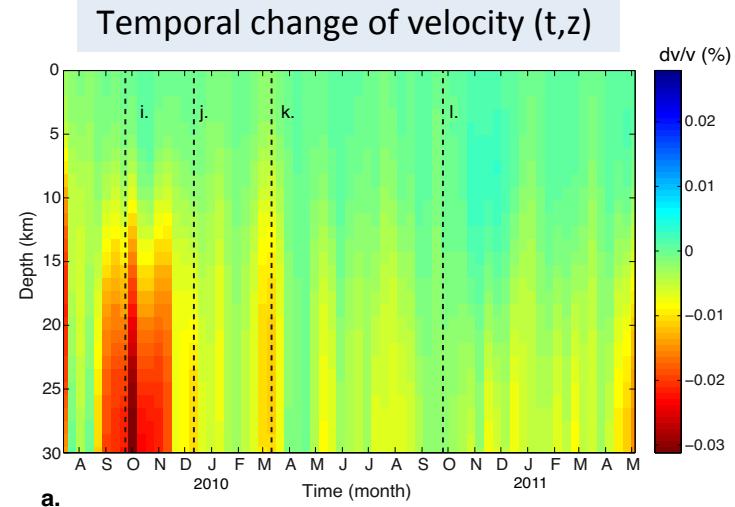


With the period band available, we conclude that the change occurs in the lower crust or below.

Linearized Rayleigh wave inversion

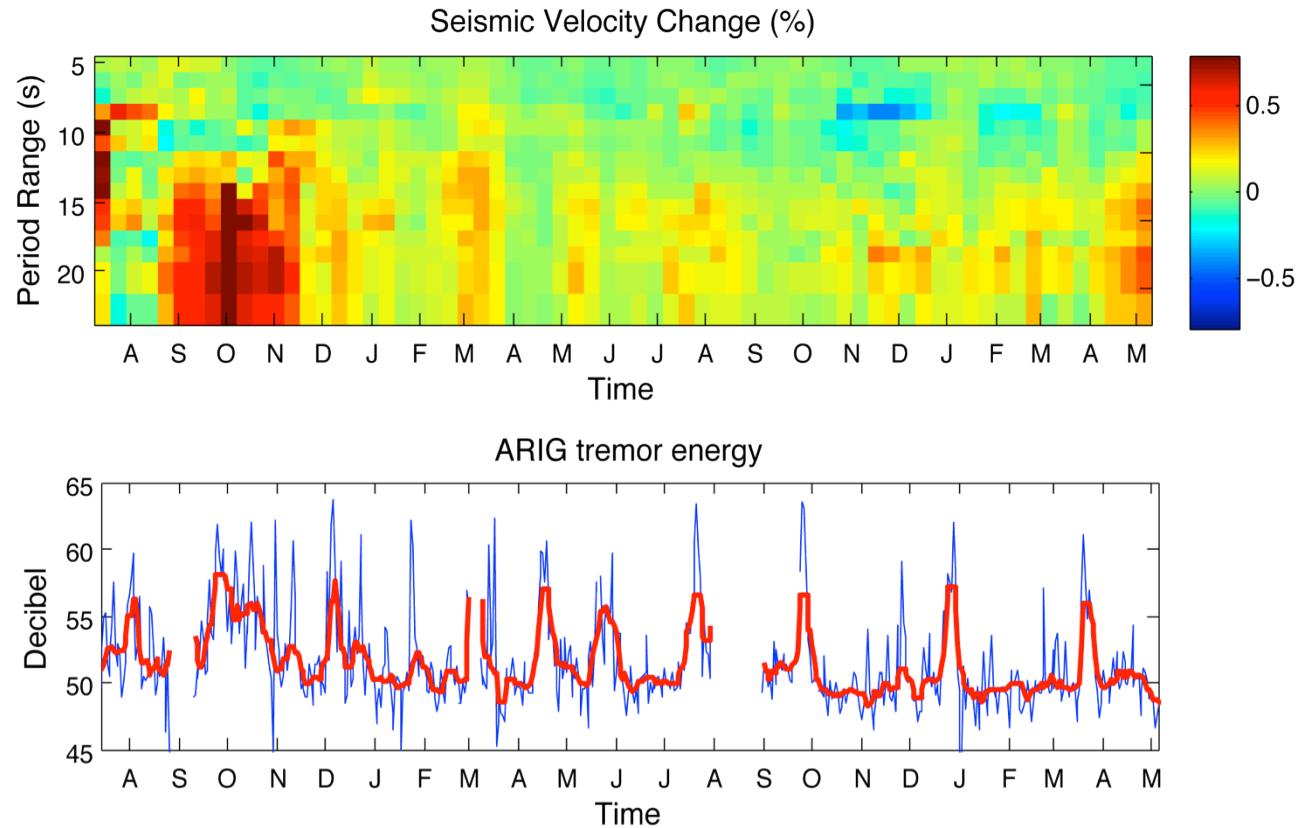


Monte Carlo inversion



Rivet et al., 2012

Velocity change and Tremors



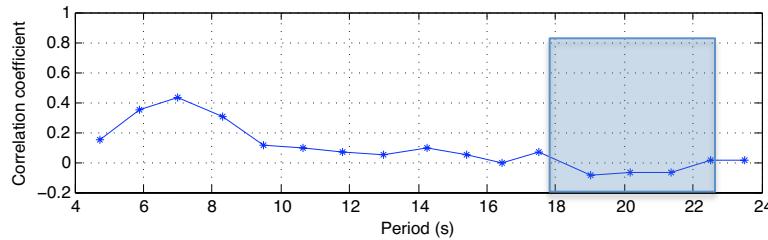
Rivet et al., 2012

Is there a measurement bias between $\Delta v/v$ and NVT activity?

Different frequency ranges (10-20s vs 0.12 -0.2s)

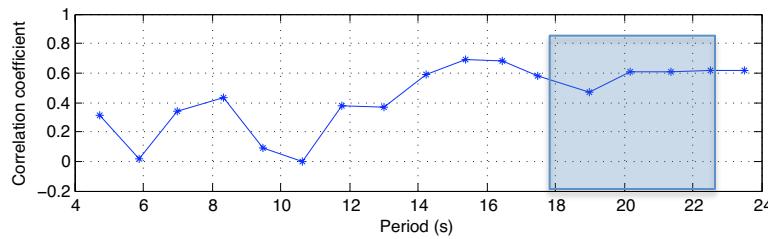
Comparison between temporal variations of velocity measured at period T and of spectral energy in the band **10-20s**:

Temporal correlation



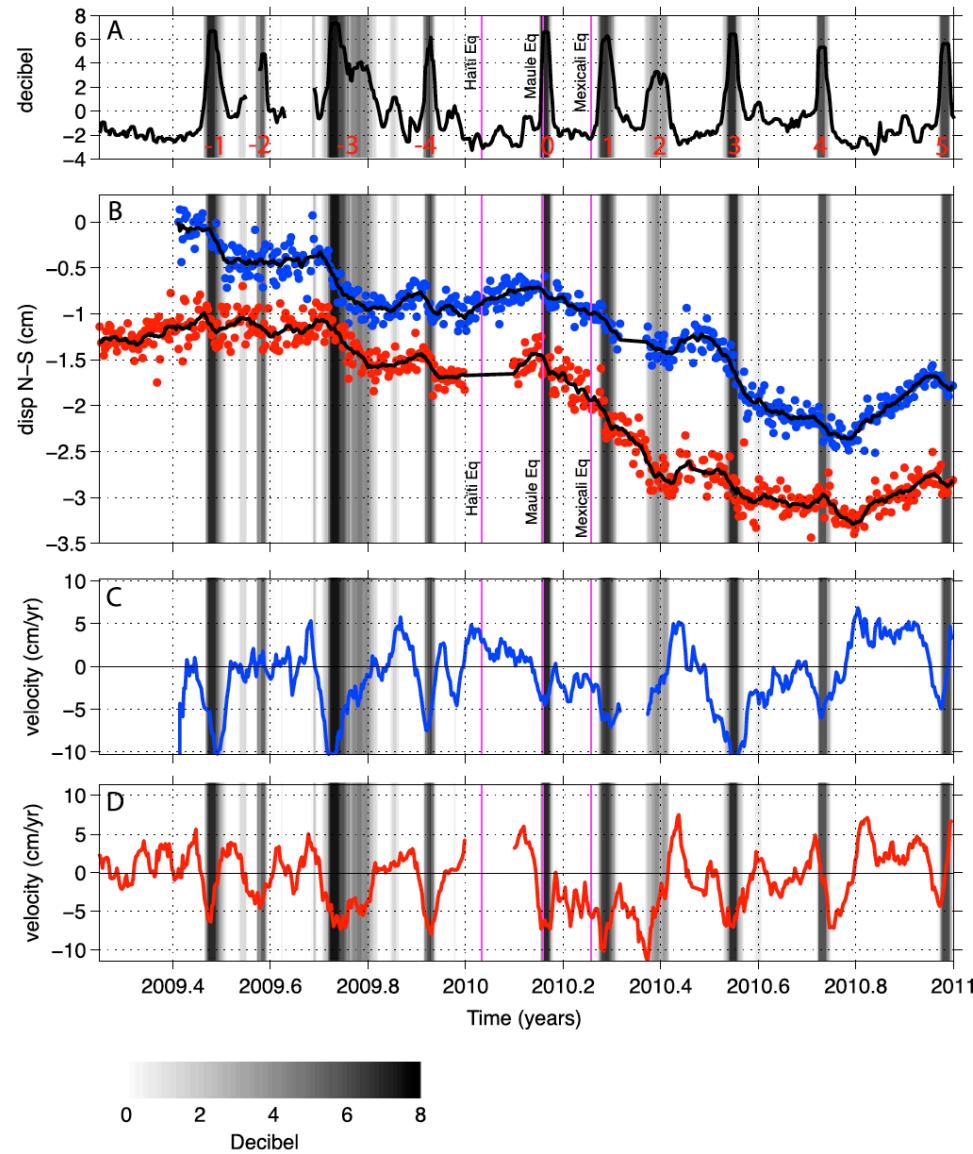
Comparison between temporal variations of velocity measured at period T and of spectral energy in the band **0.2-0.12s** (non-volcanic tremors)

Temporal correlation



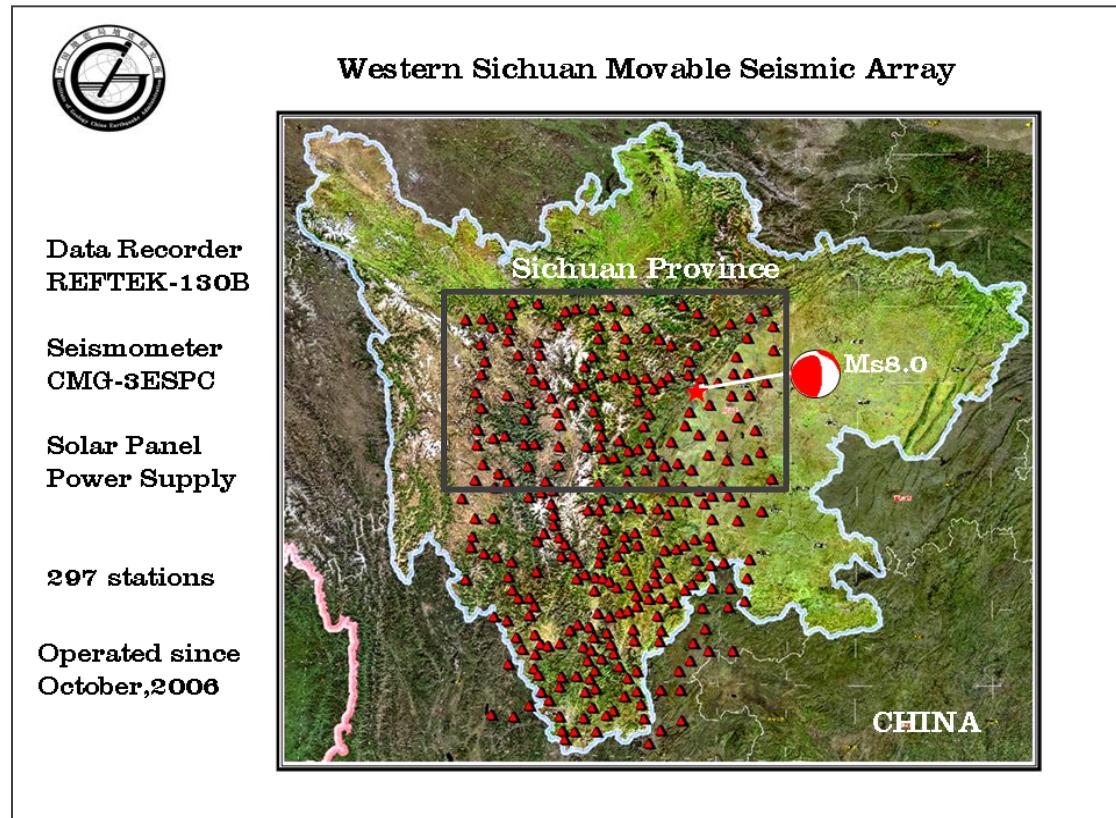
Low frequency dv/v measurements correlates with NVTs (not a bias) → low Mw SSE?

GPS positions and Tremors



Application to Wenchuan (*Chen et al. 2010, Froment et al., 2013*)

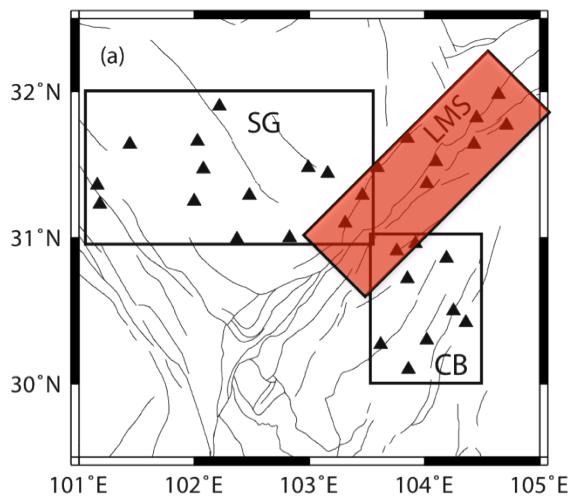
A magnitude 7.9 event occurring within a temporary (2 years) **broad band** network



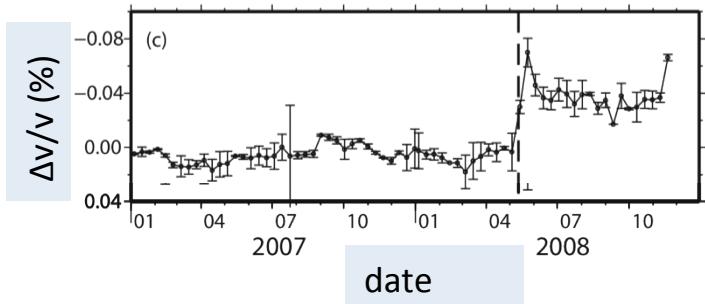
with: Bérénice Froment, Anne Obermann, Jiuhui Chen, Qiyuan Liu, Laurent Stehly,..

Short period band (1-3s)

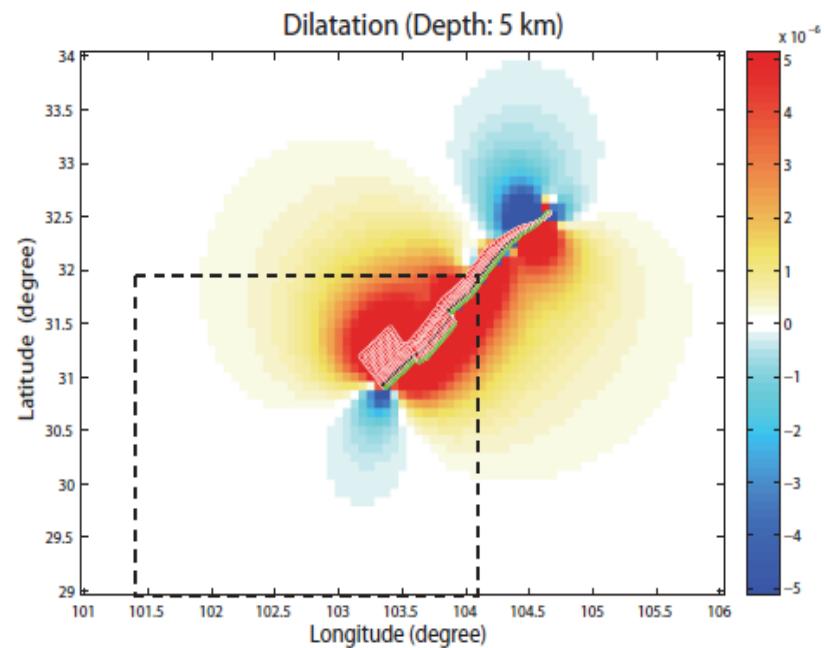
(Chen et al., 2010, Zhao et al, 2012)



Longmen-Shan (LMS)

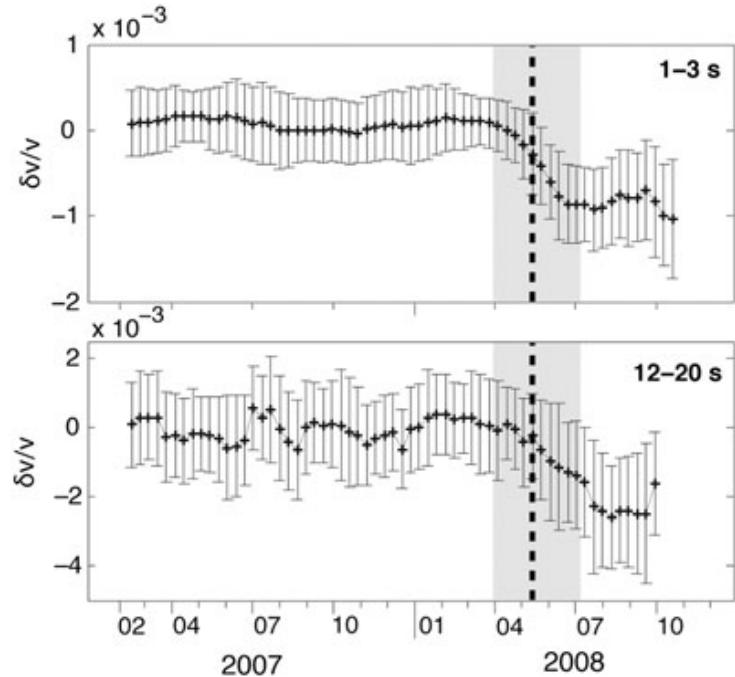


-amplitude of the velocity change is similar to Parkfield



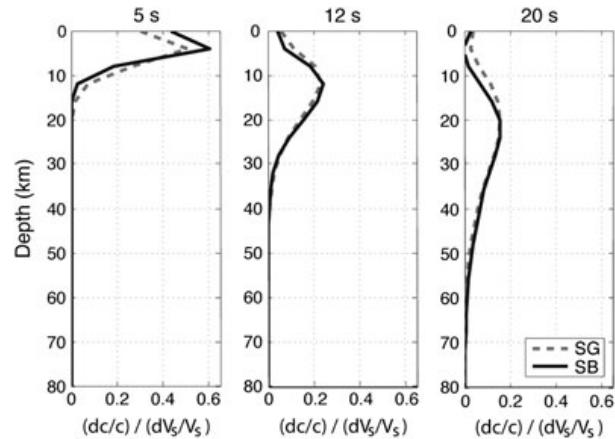
- no strong mark of the sedimentary basin
- regional effect
- correlation with deformation

Deep origin of the temporal change (Froment et al., 2013)



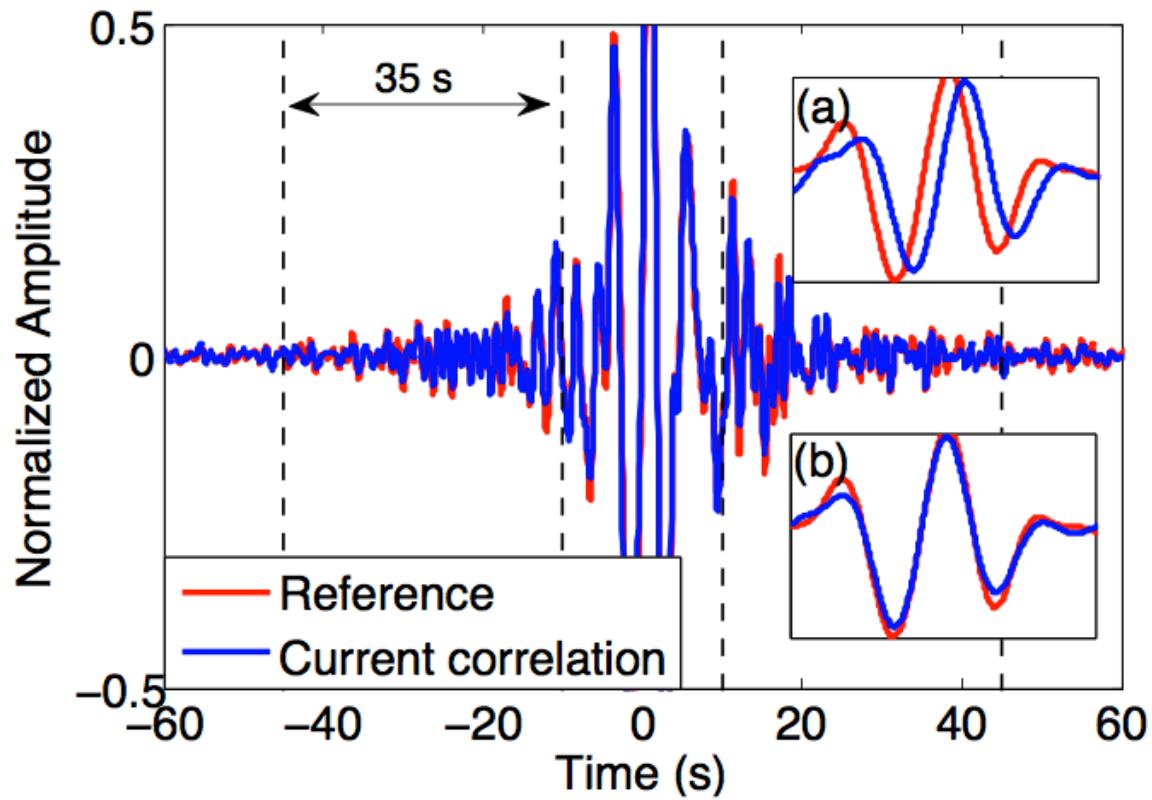
Measures in different period bands
-large amplitude at long period
-delay at long period

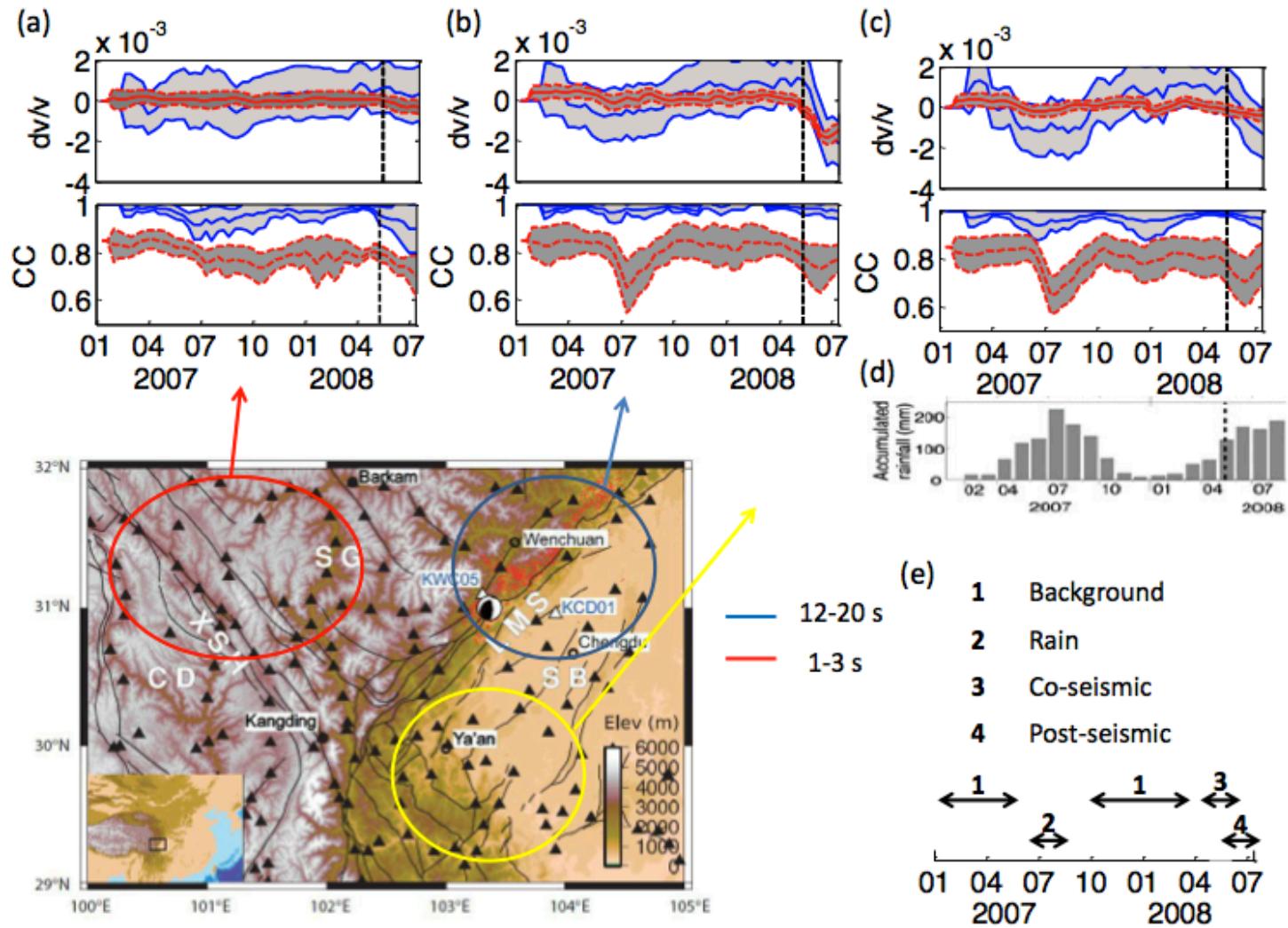
Depth sensitivity for Rayleigh waves



Changes in the mid or lower crust, with short time scale post seismic evolution

Two different measures of the temporal changes: delay and decorrelation





Need for spatial characterization

Sensitivity of coda to a change in the medium 2: lateral distribution of the changes

Mapping the change in the medium from the delays $\delta t(\tau, r_1, r_2)$ or the decorrelation

Kernels from transport equations (probabilities of presence)

$$K(x, r_1, r_2, \tau) = \frac{1}{P(r_1, r_2, \tau)} \int_0^\tau P(r_1, x, \tau - t') P(x, r_2, t') dt'$$

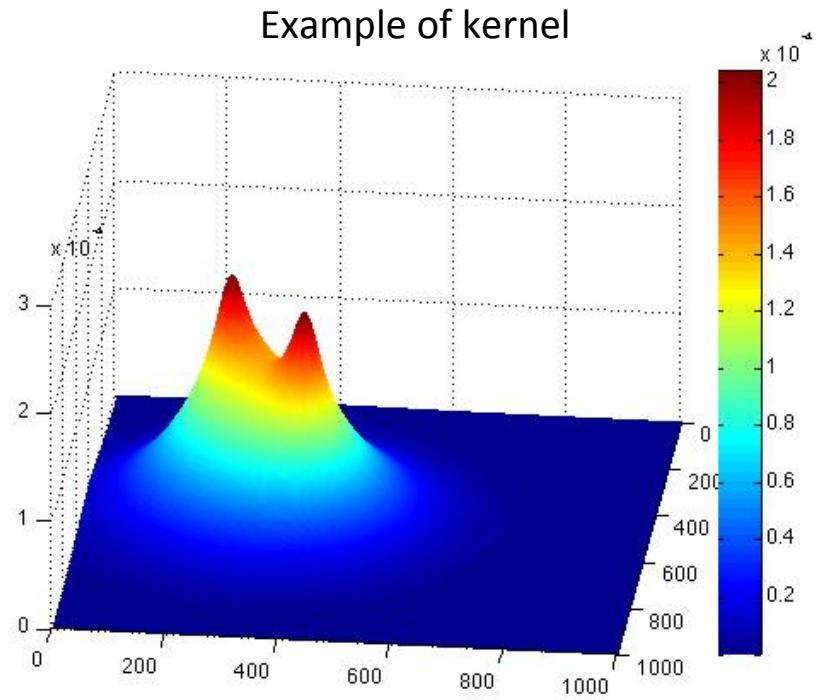
Linear formulation

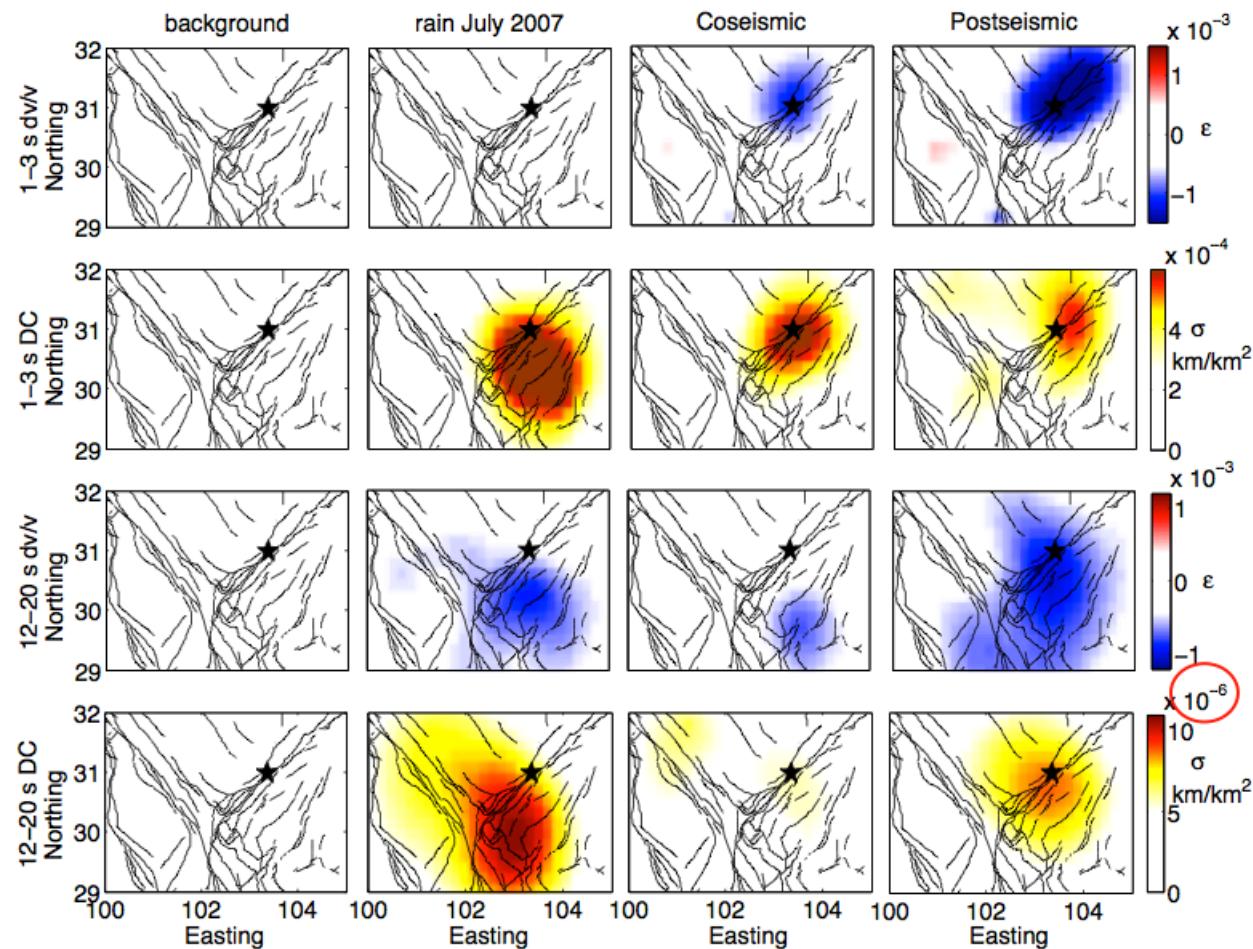
$$\delta t(\tau, r_1, r_2) = - \int_V K(x, r_1, r_2, \tau) \frac{\delta v}{v}(x) dV(x)$$

↑
unknown

P from diffusion approximation (late coda?)
or radiative transfer equation

Need for realistic modelling

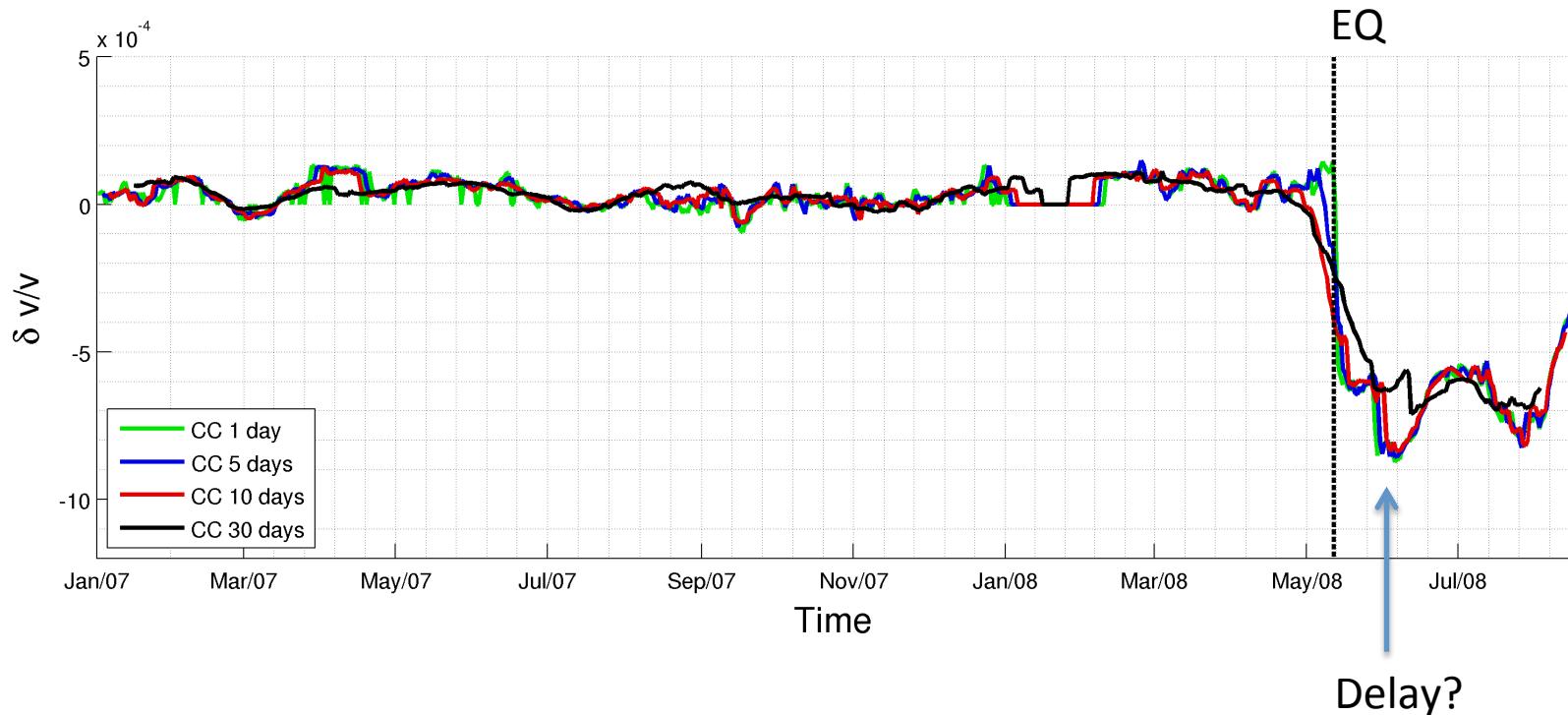




Postseismic response
Instantaneous response to hydraulic load at depth

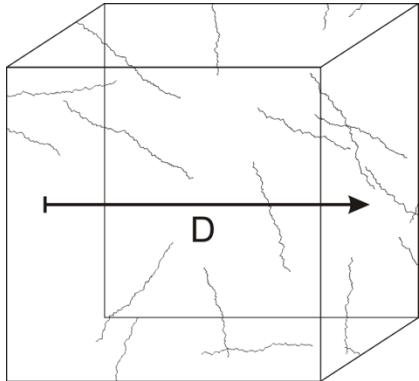
Improving the time resolution with curvelet processing (L. Stehly)

Short period (1-3s)



Superposition of the effect of waves (main shock+aftershocks) and of bulk deformation?

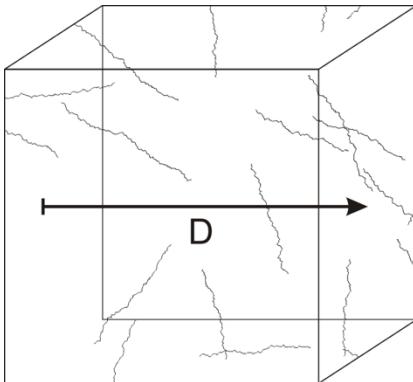
Traditional Seismic velocity tomography



$$\text{Local seismic velocity } (V) = D / (\text{travel time})$$

Seismic velocity is a proxy for **stiffness** (high velocities) and **compliance** (low velocities) of rocks

Traditional Seismic velocity tomography

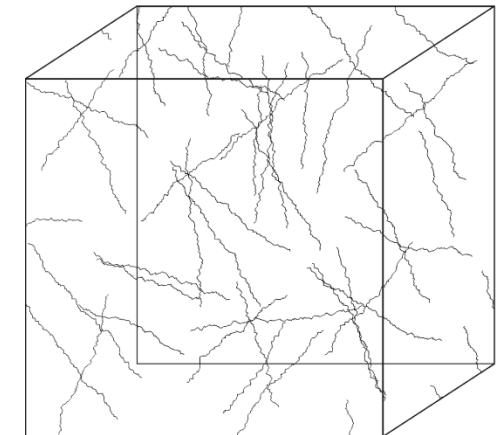
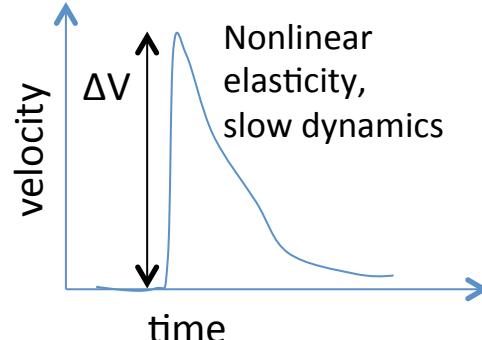
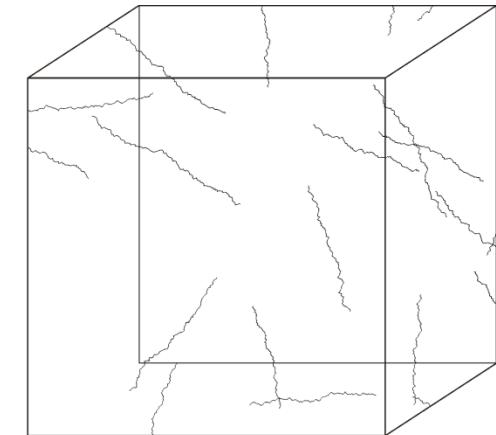
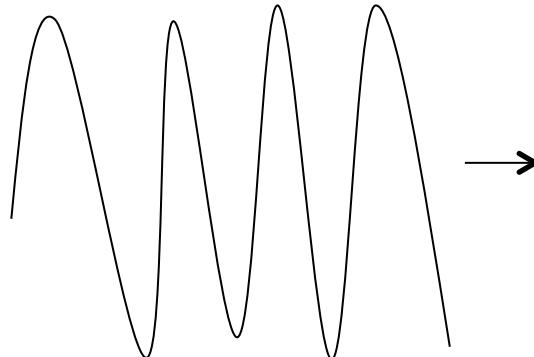


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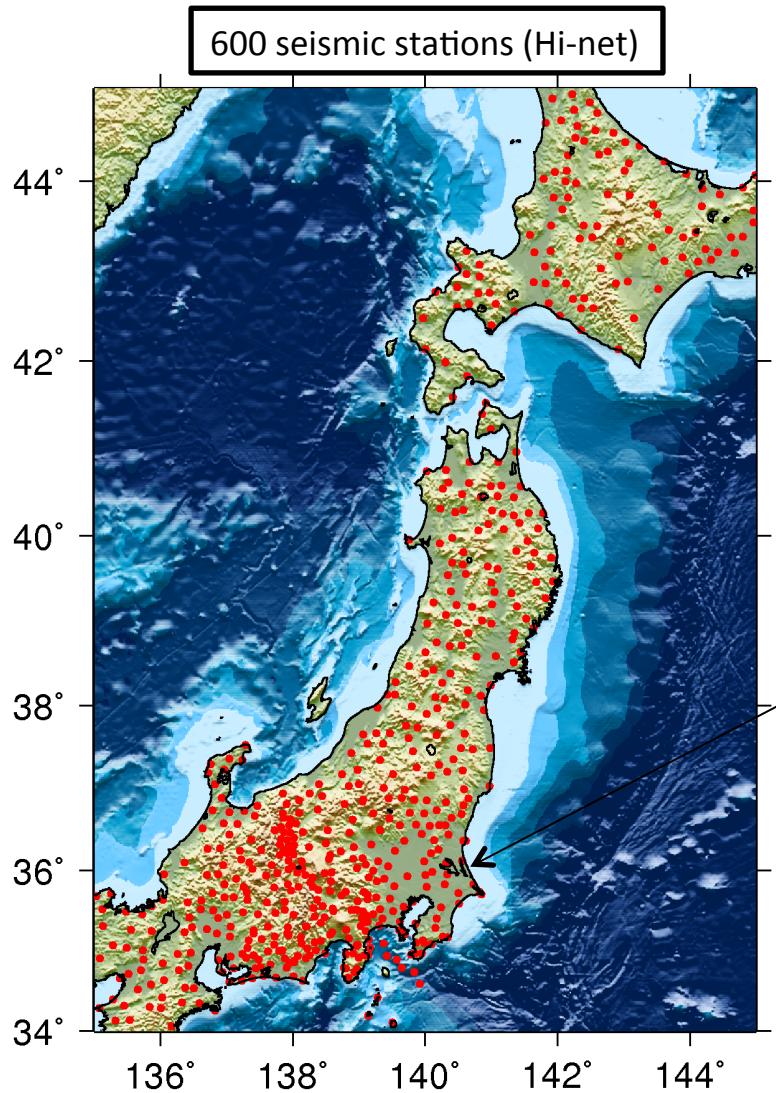
New Seismic susceptibility tomography

Dynamic stress ($\Delta\sigma$)

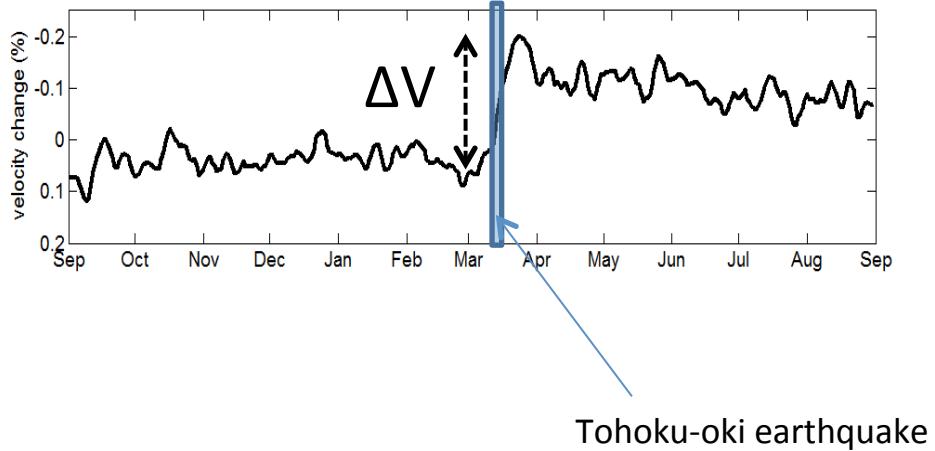


Seismic susceptibility ($\Delta V/\Delta\sigma$) is sensitive to fractured, damaged or pressurized rocks

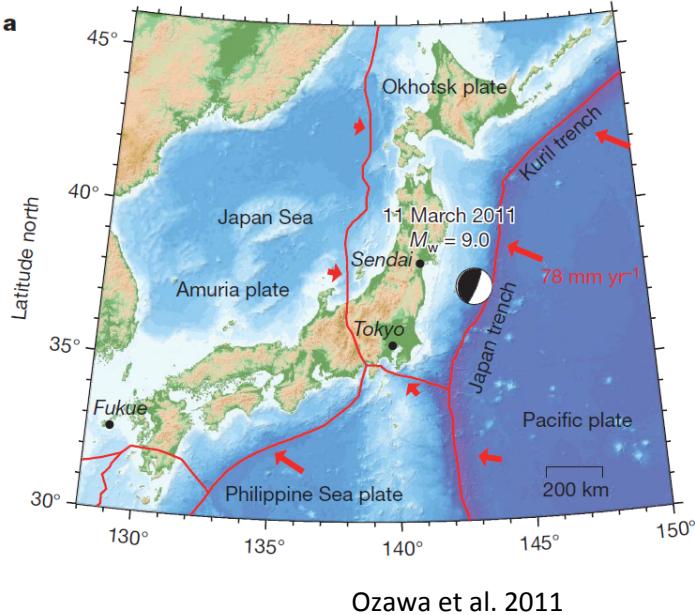
Monitoring seismic velocities before and after the M9 Tohoku-oki earthquake



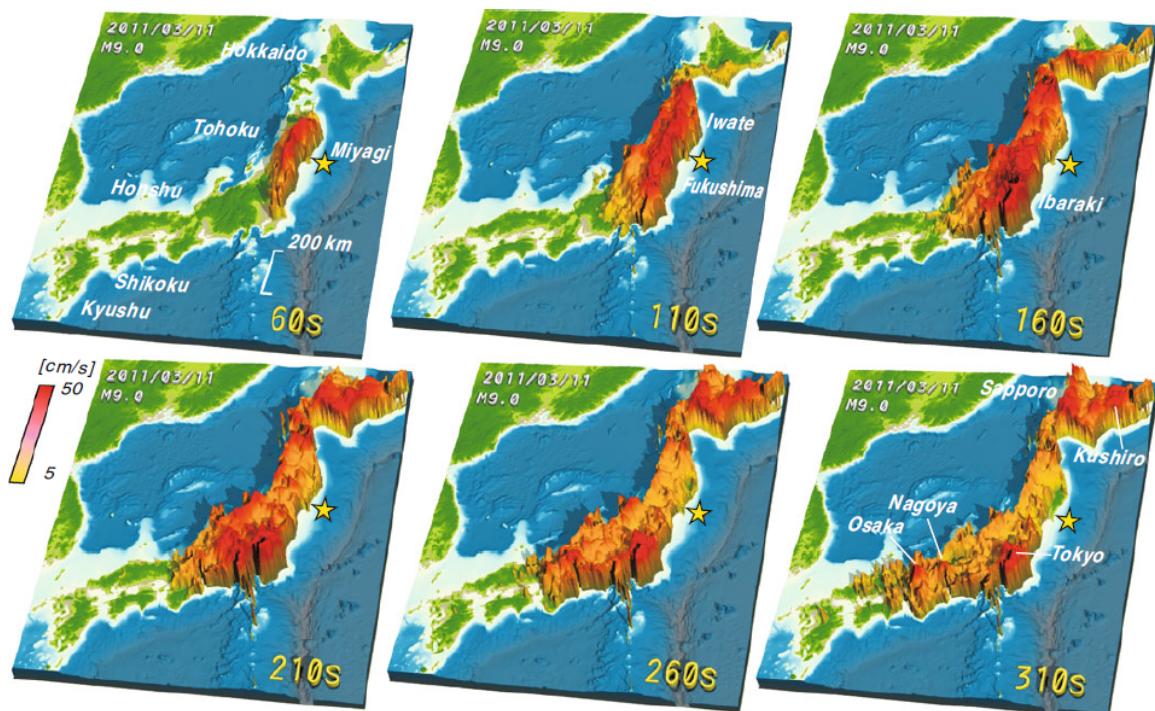
For each seismic station, we obtain a **continuous seismic velocity change time series**



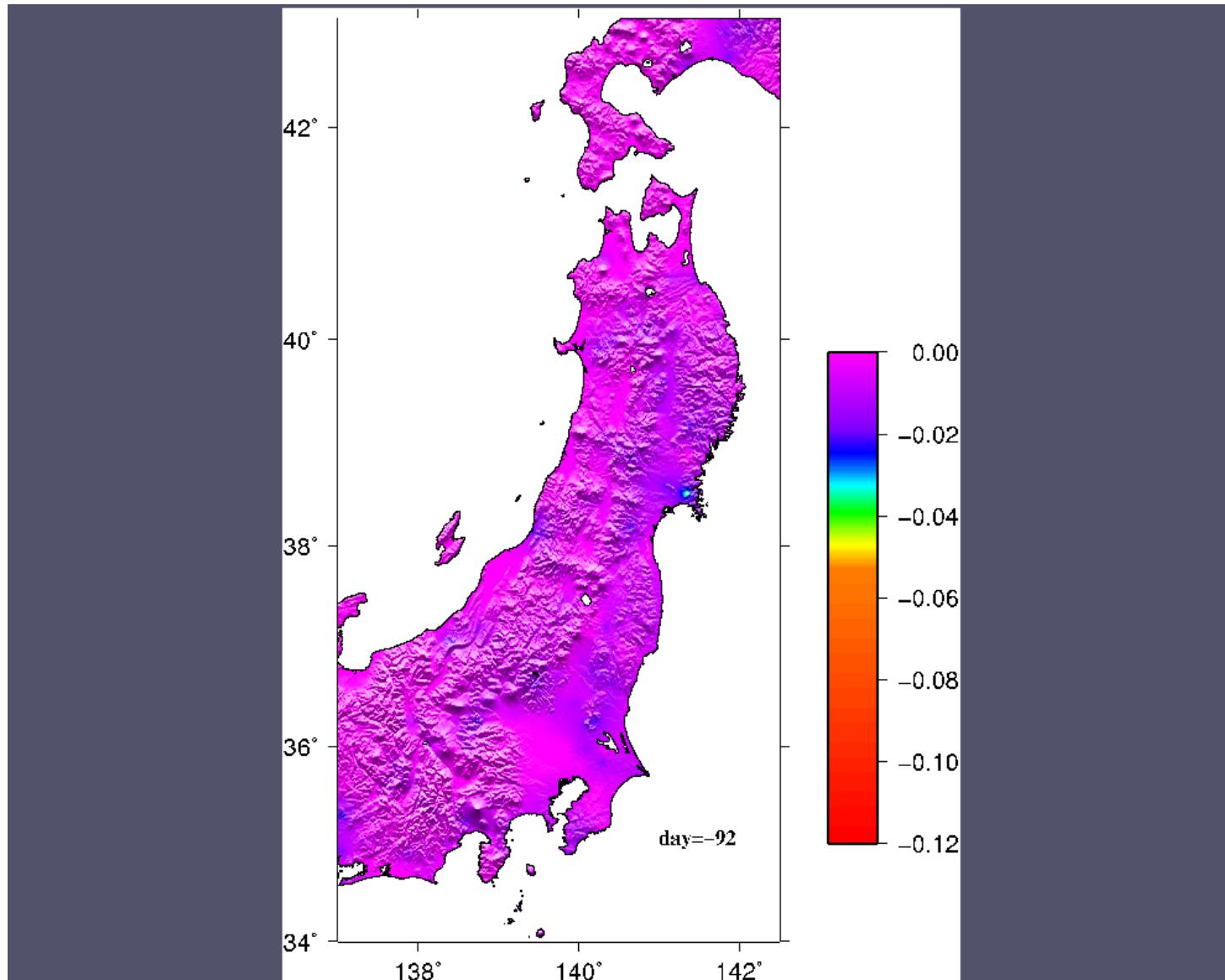
Seismic susceptibility tomography of Japan



We use **seismic waves** caused by the 2011 Tohoku-oki earthquake as **dynamic stress perturbations**

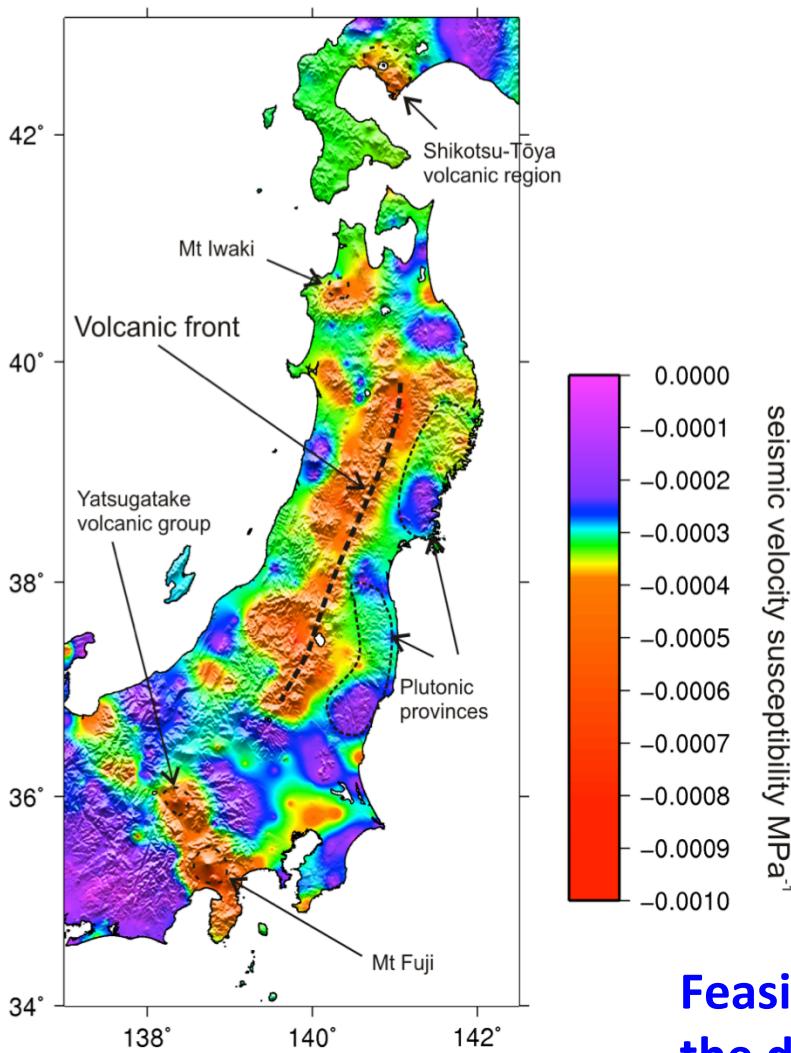


Relative velocity change (in %) measured in the band 0.1-0.9 Hz



Calendar time measured in days with respect to March 11 (M9 Tohoku EQ)
(a movie provided by F. Brenguier)

Tomography of seismic susceptibility (velocity change/dynamic stress)



- Delineates volcanic regions characterized by **high volcanic fluid pressure** (low effective pressure) and sedimentary basins
- **Maximizes below Mt Fuji volcano** where a **M6 earthquake** occurred 4 days after the Tohoku-oki earthquake
- **Minimizes in stiff old plutonic regions**

Feasibility of imaging new parameters relevant for the dynamics of eruptions and earthquakes

Tentative interpretation for dv/v at depth:

-

- 1) Associated with 'high' deformation rate (SSE)
- 2) Strong change in middle深深 crust (SSE, Eqs)
- 3) Post seismic, maximum is delayed, spatially extended (short time scale : 10^{-1} year)(Wenchuan, Tohoku, ..) → non elastic deformation at intermediate time scales
- 4) According to Schubnel et al. 2006, 2011, large sensitivity of seismic speed to deformation rate in cataclastic flow (with an analogous of the transition brittle/ductile)
- 5) Short time scale viscoelastic response of the layered crust including multiple time scales (e.g. Ivins, 1996, Hedland and Hager 2006)
- 6) Using external forcing (earthquake, tides,...) to probe properties related to the dynamics of the crust...

Conclusions:

Long range field correlations of seismic records contains deterministic information on the structure and the evolution of the Earth.

Temporal changes occur at various depths, likely associated with various physical mechanisms.

The charm of experimental studies: the new observations are not always coherent with our prejudices.